This article presents a design and experimental study of navigation integration of an intelligent mobile robot in dynamic environments. The proposed integration architecture is based on the virtual-force concept, by which each navigation resource is assumed to exert a virtual force on the robot. The resultant force determines how the robot will move. Reactive behavior and proactive planning can both be handled in a simple and uniform manner using the proposed integration method. A real-time motion predictor is employed to enable the mobile robot to deal in advance with moving obstacles. A grid map is maintained using on-line sensory data for global path planning, and a bidirectional algorithm is proposed for planning the shortest path for the robot by using updated grid-map information. Therefore, the mobile robot has the capacity to both learn and adapt to variations. To implement the whole navigation system efficiently, a blackboard model is used to coordinate the computation on board the vehicle. Simulation and experimental results are presented to verify the proposed design and demonstrate smooth navigation behavior of the intelligent mobile robot in dynamic environments. © 1999 John Wiley & Sons, Inc.

1. INTRODUCTION

To be useful for accomplishing practical tasks, a mobile robot must be able to navigate smoothly in the real world, where unexpected changes in its surroundings occur. There are many prospective applications for such an intelligent, autonomous robot: a few examples include transferring material in automated factories, cleaning in hotels, or delivering meals or patient records in hospitals. In such applications, the robot must reach one or more destinations and perform some kind of task there. While traveling to the destination, it must take care to avoid collisions with various fixed or moving obstacles.

* To whom all correspondence should be addressed.
objects (such as people or other mobile robots). The sensor-based navigation algorithm is, therefore, very important for using mobile robotic systems.

Early approaches to mobile-robot navigation broke the overall job into subtasks that could be handled by sense-model-plan-act (SMPA) functional modules. The main problem with such approaches is high computation costs, especially in the perceptual portions of the systems. Brooks believed that intelligence could be achieved without traditional representation schemes, so he proposed a framework called the subsumption system, often referred to as the behavioral system. In Brooks’ approach, navigation was first decomposed into task-achieving behaviors controlled by an algorithm tying sensing and action closely together. Control-system layers were built up to let the robot operate at increasing levels of competence. Although Brooks proposed that intelligence can be achieved without representation, he did not rule out representation and admitted that it is sometimes needed to build and maintain maps. For instance, planning a shortest path based on a map can help the robot reach its destination more efficiently. Therefore, researchers have recognized that representational and behavioral systems should be combined to deal with more complicated tasks.

A representational system often plans paths for mobile robots according to a world model. Commonly used world-modeling approaches include grid maps, cell trees, and roadmaps (which are often constructed from geometric maps). In planning paths, search methods such as A* or bidirectional search algorithms can be used in conjunction with these representations. Jarvis proposed the distance transform (DT) methodology for path planning with a grid map. Borenstein and Koren proposed a vector-field-histogram method based on a histogramic grid map. The potential field method can work with a world model for path planning, especially with a grid map.

The behavioral approach lets a mobile robot deal with unexpected obstacles in the immediate environment by using onboard sensory information. This is usually considered a reactive scheme. Recently, researchers have been interested in how to prevent robots from colliding with other moving objects. Several methods have been proposed to solve such dynamic motion-planning problems, but most of them have not been actually implemented in real mobile robots. It might be that sensory systems can hardly provide desired motion information in real time. The frequently used ultrasonic sensors provide little information and cannot obtain the comprehensive obstacle-motion information required for these proposed reactive navigation methods. CCD cameras provide far more sensory information, but the longer times required for image processing make real-time operation very difficult. To resolve the sensor-system problem, Chang and Song proposed extracting simple implicit motion information from multiple rangefinders. A neural network predictor was developed to estimate the next-time readings of a ring of ultrasonic sensors. This information is equivalent to the next-time position of an obstacle’s nearest point relative to the robot. Using such projected information, they proposed applying a virtual-force method to change the robot’s motion. This prediction-based virtual-force guidance was found to be quite useful in navigating a mobile robot among multiple moving obstacles.

As can be seen from the description above, there are two different strategies for autonomous navigation: representational and reactive; an optimal combination of them is therefore important. Some researchers have proposed using a hierarchical architecture with layers of SMPA modules. Lower SMPA layers provide quicker reaction, and higher layers perform more complicated sensor processing and world modeling based on lower-layer results. Vandorpe et al. developed a hierarchical navigation system in which lower-layer action decisions depended on the higher-layer ones. Hu and Brady let every control layer generate commands and then used a command selection module to determine the final motion commands. Stentz and Hebert used a weighted average method to combine the results from a global navigator and a local navigator. Some other systems extended the behavioral approach by elaborately incorporating suitable representations and planning. Mataric integrated a topological representation into a subsumption-based mobile robot. Payton et al. transformed an internalized plan (a gradient field) and reflexive behaviors into fine-grained actions with activation values. The action with the highest weighted-sum activation value was chosen as the command. Arkin used world models to select motor schemes (behaviors). Each schema is associated with a potential field, and the resultant potential navigates the robot. Although integrating reactive navigation and representation-based planning for intelligent mobile robots has been the object of considerable research attention, no specific approach can yet be recognized as being optimal in terms of generality and
effectiveness. Therefore, designing a suitable architecture for integrating the two strategies deserves further attention.

This article presents a new integration method that can navigate a robot in an unstructured environment, build and update maps, plan and execute actions, and adapt the robot’s behavior to environmental changes. The proposed integrated navigation system is based on a virtual-force concept. In this method, navigation resources related to desired behaviors and constraints are converted to virtual-force sources (Fig. 1). The resultant force changes the robot’s motion to the desired manner. Virtual-force guidance was originally used for reactive navigation in dynamic environments. Its principal force sources come from an ANN sensory predictor, which provides implicit information about obstacles’ motions. In the integrated navigation system, a path planner is another resource for navigation. Subgoals are extracted from the planned path and each produces a virtual force in sequence. In this article, a bidirectional distance-transform method is proposed for path planning. It is based on a grid map that uses a digital filter to fuse sensory data. This method is fast and thus aids in developing an on-line path modifier.

The next section presents an efficient method for world modeling. The bidirectional distance-transform method and on-line plan modification are presented in Section 3. Section 4 describes how the virtual-force approach integrates reactive navigation and path planning. Section 5 shows simulation results with an emulated fast mobile robot. Section 6 presents experimental results with a laboratory-constructed robot, and Section 7 offers the conclusion.

2. GRID MAP BUILDING

A mobile robot should maintain a world model to navigate efficiently. If a mobile robot does not have a map of the external world, it can only react to its immediate surroundings without considering overall navigational performance. Two types of world models are used extensively: symbolic or categorical representation and analogical representation. In the authors’ system, an analogical representation, a grid map, is used. Grid maps are easy to plan with and maintain.

Grid maps are commonly used with sonar data and maintained by certainty values. In formal probabilistic approaches, two maps are needed: an occupied map and an empty map. This approach requires much calculation and memory space. Oriolo et al. proposed using fuzzy reasoning instead, but it also needs two maps. Borenstein and Koren’s method is fast, but it considers fewer ultrasonic sensor characteristics. Song and Chen proposed the heuristic asymmetric mapping (HAM), a compromise between computational cost and probabilistic meaning.

The method described below is extended from the HAM approach and uses a ring of ultrasonic sensors. A cell in the grid map has a value showing the probability of that cell being occupied by an obstacle. The values range from −1 to 1; the closer to 1 a value is, the more likely the cell is occupied. When an ultrasonic sensor obtains a distance reading, it is very likely that cells within the ultrasonic beam at distances less than the distance reading are empty, and cells within the beam at distances around the distance reading are occupied. Therefore, empty regions and occupied regions can be represented as shown in Figure 2. The mapping algorithms for cells in these two regions are similar. First, a sensor reading indicates a possibility of a cell in these regions. Then, it is merged into the map through a digital filter to generate a certainty value.

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**Figure 1.** Integrated navigation structure using virtual-force concept.
Figure 2. Occupied region and empty region.

For an occupied cell A1, the certainty value given by the kth measurement is given as follows:

\[ g_{A1}(k) = k_d \cdot k_{\theta_1}, \]  

(1)

where

\[ k_d = \begin{cases} 1 - \frac{d - d_{\text{min}}}{d_{\text{max}} - d_{\text{min}}} & \text{for } d_{\text{min}} < d < d_{\text{max}} \\ 0 & \text{otherwise} \end{cases} \]  

(2)

and

\[ k_{\theta_1} = \begin{cases} 1 - \left( \frac{\theta_1}{\theta_b} \right)^2 & \text{for } |\theta_1| < \theta_{\text{m1}} \\ 0 & \text{otherwise} \end{cases} \]  

(3)

In the above expressions, d is the raw sensory data, \( d_{\text{max}} \) and \( d_{\text{min}} \) are the maximum and minimum effective ranges of the ultrasonic sensor, respectively, \( a \) is a parameter that keeps \( g_{A1} \) in a desired range, \( \theta_1 \) is the angle of cell A1 relative to the centerline of the sensor, \( \theta_b \) is the beam angle of the sensor, and \( \theta_{\text{m1}} \) is the maximum angle for admitting occupancy. Value \( g_{A1} \) is then merged into the map to give the certainty value for cell A1 \( (p_{A1}) \) using a first-order digital filter:

\[ p_{A1}(k) = k_{g1} \cdot g_{A1}(k) + (1 - k_{g1}) \cdot p_{A1}(k-1), \]  

(4)

where \( k_{g1} \) is the weighting factor related to the speed of convergence. Its value must be greater than 0 and less than 1 for convergence.

For the cells in the empty region, negative certainty values are used to represent empty probabilities. Two conditions are considered. First, if \( d < \text{maximum effective range} \), the certainty value of an empty cell A2 from kth measurement is

\[ g_{A2}(k) = -k_d \cdot k_{\theta_2}, \]  

(5)

where

\[ k_{\theta_2} = \begin{cases} 1 - \left( \frac{\theta_2}{\theta_b} \right)^2 & \text{for } |\theta_2| < \theta_{\text{m2}} \\ 0 & \text{otherwise} \end{cases} \]  

(6)

\( \theta_2 \) is the angle of cell A2 relative to the centerline of the sensor, and \( \theta_{\text{m2}} \) is the maximum angle for admitting emptiness. The following digital filter is then employed to merge \( g_{A2} \) into the map to give a certainty value for cell A2 in the map \( (p_{A2}) \):

\[ p_{A2}(k) = k_{g2} \cdot g_{A2}(k) + (1 - k_{g2}) \cdot p_{A2}(k-1), \]  

(7)

where \( k_{g2} \) is the weighting factor in the empty region. Second, if \( d \geq \text{maximum range} \), it means that there is either no obstacle in the detection area or that a specular reflection has occurred. Considering that it may be a specular reflection erroneous data, a modified formula must be used to update the cell-certainty value:

\[ p_{A2}(k) = k_{g3} \cdot g_{A2}(k) + (1 - k_{g3}) \cdot p_{A2}(k-1), \]  

(8)

where \( k_{g3} \) is a weight factor smaller than \( k_{g2} \).

The following considerations have been taken into account in designing the parameters in these formulas.

1. \( k_d \), the distance factor. Normally, a specular reflection leads to a measured distance greater than the actual distance. Therefore, the credit must be smaller when the measured distance is larger. Thus, \( k_d \) is set to a suitable range such that \( g_{A1} \) is from 0.4 to 1.
and $g_{A2}$ is from $-0.4$ to $-0.1$ (where the value 0.4 is the threshold for distinguishing whether or not a cell is occupied).

2. $k_{d1}$ and $k_{d2}$, the direction factors. An object is easier to detect when it is located in the centerline of the ultrasonic beam. Eqs. (3) and (6) reflect this fact.

3. $k_{g1}$, $k_{g2}$, and $k_{g3}$, the weighting factors. The weighting factor is related to the convergence of the digital filter. The smaller the value is, the slower the convergence speed. A computer simulation was used to determine suitable values. If one takes 0.7 as the average certainty value for occupied cells and -0.7 as that for empty cells, then one’s design goal can be set as follows: four consecutive data that indicate occupancy with the average certainty values will change an empty cell into an occupied cell. This can be checked by employing (4). Solving this equation by the numerical method, one finds that $k_{g1}$ is about 0.35. On the other hand, the authors hope for three consecutive data that indicate emptiness will change an occupied cell into an empty cell. Similarly, $k_{g2}$ is found to be about 0.09 and $k_{g3}$ 0.022. Note that a preference for an empty cell is adopted in this design, allowing more free space for path planning.

This digital filter reasonably interprets current as well as historical sensory data. Past measured data also contribute to the cell’s current certainty value. However, the present measurement takes relatively higher weight, while the older ones will finally take nearly zero weights. The formal structure of traditional filters, such as Kalman or Wiener filters, is not adopted here. The authors’ structure is more heuristic to match the characteristics of the sensor employed. This is also simpler compared with the formal structures. Furthermore, the Gaussian noise premise for Kalman filters does not exist in the dynamic environment. For instance, a formerly occupied cell may be identified as being empty simply because the obstacle has moved away. This map-building method can be used with other types of sensors which give range information about obstacles. However, because of different sensor models, the parameters discussed above should be modified. One merit of this present design is that its grid map does not record moving obstacles since they do not stay at fixed locations very long. It can be seen from (4) that the digital filter does not allow one or two sensor inputs to elevate the cell certainty value so high as to change its status. After moving obstacles have passed, the cell values decrease because the next sensor inputs indicate the absence. Recording only static obstacles (which may change positions, however) fulfills navigational requirements because moving obstacles do not stay at fixed locations and should not affect path planning.

3. PATH PLANNING AND PLAN MODIFICATION

In this integrated design, the path planner works to provide a reference path for the robot to travel to the goal according to the current grid map. The planned path is suboptimal in terms of distance. Before path planning begins, the grid map is first divided into occupied and empty areas, according to the 0.4 threshold value. This produces a binary map. Then, occupied areas are expanded by the radius of the mobile robot. This simplifies the path planning problem to a point on the map. The next section proposes a path planning method using the DT concept.

3.1. Path Planning Using Bidirectional Distance Transform

Distance transform is essentially the propagation of distance away from a set of core cells (zero-distant from themselves) in a tesselated space. For robot path planning, this propagation flows around obstacles (occupied areas) from the start or goal positions. In a 2-dimensional representation, each cell has eight neighboring cells to propagate the distance. The global distance of a cell from the core cell is computed from the local distance between two neighbors. The distance between horizontal/vertical neighbors is denoted $d_1$, and the distance between diagonal neighbors is denoted $d_2$. Different distance proportions between $d_1$ and $d_2$ have been utilized. Borgefors found that when $d_2/d_1$ equals about 1.351, the error between the transformed distance and the Euclidean one has a minimum upper bound.

In the authors’ method, $d_1$ and $d_2$ are set to integers 3 and 4, respectively, to speed up computation. Bidirectional DT, in which distances are propagated simultaneously from the robot’s position and the goal, is proposed to cut both search space and computation time by about half. The DT from the goal takes positive values, while the DT from the
robot's position takes negative ones. When a cell is marked as having positive and negative values, it is termed a meet cell and the propagation stops. The shortest path can be found by backtracking from the meet cell to the robot's position and goal using steepest gradient ascent and descent algorithms, respectively. Figure 3a shows an example of path planning employing bidirectional DT. In this figure, distances are propagated from S and G, where S denotes the robot's start position and G denotes the goal position. The propagation stops at the bold-lined cell, which is marked as having both positive and negative values. Subgoals, which are the turning points of the path and denoted by SG, should be extracted because they will be used for integration with reactive navigation (see next section). Note that the extraction of subgoals can be realized in the backtracking phase with little extra computational loading.

3.2. On-Line Plan Modification

The preplanned path may become invalid because the environment may change after the robot moves. If this variation is considerable, replanning is often the best policy, although reactive navigation may also be able to maneuver the robot to the goal. Nevertheless, complete replanning requires too much calculation and is not preferable. Stentz\textsuperscript{27} proposed a $D^*$ algorithm that can amend improper plans resulting from the environment changes; however, the algorithm itself is much more complicated than the DT-based approaches. Vandorpe et al.\textsuperscript{14} adopted a reactive planner that uses a DT-based approach within a local window covering two consecutive intermediate via-points (subgoals). Their method costs too much computation time because the reactive planner must be applied repeatedly. Even so, it still is not guaranteed to produce the best plan because of the limited search window.

This article's plan modification method utilizes information from the original plan since most of the world model remains the same except for the local changes detected by the sensors. In the original plan, numbers (distances) marked in the cells by applying DT from the goal are still valid if they are not larger than the positive numbers in the changed parts of cells. If all the changed cells have negative numbers, then all the positive numbers marked by the original plan remain valid. To amend the plan, it is only necessary to (1) clear improperly marked numbers, including the negative ones marked by DT from the robot's start position and positive ones that are greater than the smallest positive numbers of the changed cells and (2) propagate the negative number from the robot's current position to a cell with a positive value previously marked by DT from the goal. Figure 3b shows an example of path modification, in which a new obstacle is found on the previously planned path (Fig. 3a). In this case, the new obstacle occupies cells that were marked with 9 and 10, so the cells marked with 10 are cleared. All cells with negative numbers are also cleared. Then negative DT numbers propagate from the robot's current position until it reaches a cell with a positive value. The replanned path is therefore updated. This plan modification scheme provides the shortest path and requires much less computation time than does complete replanning.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Figure3.png}
\caption{(a) An example of bidirectional DT-based planning. (b) An example of plan modification when previous plan is found to be improper.}
\end{figure}
Because of the limitation of motion directions, path planning using the DT-based approach is inherently crude. To boost navigation performance while cutting traveling distance, check if there is a clear path between the robot's current position and the next subgoal. If the path is free from obstacles, then the robot discards the current subgoal and moves toward the next one. This way one can make up for the movement direction limitations.

4. INTEGRATION WITH REACTIVE NAVIGATION

It is desirable for the path planner to be integrated with a reactive scheme that responds to immediate obstacles to make a complete navigation system. There are, however, two problems in performing this integration: (1) the command formats are different; and (2) the proactive and reactive navigation methods are totally independent. This section proposes the virtual-force method to solve both problems. First, the planned path and reactive behaviors are transformed into virtual forces exerted on the mobile robot. Then, the two types of navigation can be merged by calculating the resultant force. This force determines the way the robot changes its motion according to Newton's second law of motion. Because the relationship between force and motion change is obvious, it is easy to design forces to match desired behaviors. In the present system, virtual forces are designed so they can deal with intelligent but possibly careless moving obstacles. This means that the moving obstacle itself can take half the responsibility for preventing collision, but might not do so because of carelessness. Moreover, if any new navigational resources are added or new behaviors desired, appropriate virtual forces can be created and added to the system. The following paragraph introduces the virtual forces for reactive navigation. Then, integration with the planned path is presented.


It is important for an intelligent mobile robot to react to previously unrecorded obstacles in the immediate environment. Moreover, to cope with moving obstacles, the robot needs to know their motions to avoid them safely. The authors' mobile robot is equipped with a ring of 16 equally spaced ultrasonic rangefinders for detecting obstacles. These sensors are fired sequentially in four groups. The error-eliminating-rapid-ultrasonic-firing (EERUF) method proposed by Borenstein and Koren\(^2\) was adopted for this study. A complete set of 16 sensor measurements takes only 140 ms. However, rangefinders have difficulty identifying obstacles, and their motion estimation will have large degrees of uncertainty. In the authors' reactive navigation scheme, rangefinders are not used to identify the precise shapes and positions of obstacles. Instead, the sensory system only tells the robot what area will be occupied by obstacles. This is an implicit form of considering the motions of obstacles. Such information can be obtained by predicting future sensor readings employing an artificial neural network.\(^{12}\) The authors' prediction theorem is based on the knowledge that the measurement from any given sensor must have a relationship to historical measurements from sensors nearby. As illustrated in Figure 4, sensor readings of present and previous sample instants are sufficient to predict the next one. Raw data from four neighboring sensors (two on the left and two on the right) and the given sensor itself are used to predict next-time sensor reading. Since the mobile robot is equipped with a ring of 16 ultrasonic sensors, the entire predictor is constructed from 16 identical ANNs. The ANN was trained off-line using training data generated by an environment-configuration simulator. At the run time, the ANNs predict future sensory data on-line in real time. Thus, future positions of obstacles are used to form virtual-force sources to let the robot respond to anticipated changes in environment.

In this design, it is assumed that a point obstacle is located in the sensory direction and at the predicted distance. For each obstacle, three force zones were established around it. When the robot enters these zones, virtual forces will be generated to make it behave in a certain manner. The resultant force is determined to change the robot's velocity and make it easily, avoid moving and static obstacles.

The first force zone around an obstacle is termed the deceleration zone. In it, the robot decreases its
speed. It is usually desirable that the robot decreases its speed to a certain range within a preset time interval. Consequently, viscous force is a suitable choice in such a situation because it has the effect of decreasing the robot’s speed in proportion to its current speed. Note that even when the robot is at a location covered by the deceleration zones of many obstacles, it is sufficient to count only one viscous force.

The second force zone is the push-away zone. When the robot somehow gets closer to an obstacle, it is necessary to exert a relatively large force against it to prevent a collision. Eventually the force will be large enough to push the robot away from the obstacle. A virtual spring installed between the robot and the obstacle is suitable for this purpose because the spring force exerted on the robot directs it away from the obstacle. Consequently, as the robot penetrates deeper into the push-away zone, an increasing push-away force will exert against it. By properly choosing the spring constant, this force guarantees the robot will never collide with a static obstacle.

The third force zone around an obstacle is the drive-aside zone, which makes the robot avoid moving obstacles moving toward it. This force also helps to avoid static obstacles more smoothly. The virtual force generated in this zone, which is termed the drive-aside force, drives the robot away in a lateral direction. Note that a drive-aside action can make the robot move left or right. The robot will choose the one that will move closer to the goal. Figure 5 depicts the forces that affect the robot’s motion in different zones. The extents of three force zones around an obstacle can be seen in this figure.

The virtual force strength should be determined according to the kinematic parameters of the mobile robot. The kinematic constraints for this study’s

Figure 5. Virtual forces used for the integrated navigation: subgoal force works everywhere, but may be suppressed; three forces from obstacles work within the corresponding zones. Robots receive different forces in different areas. Robot A is far away from the obstacle; only the subgoal force affects it. Robot B is in the deceleration and drive-aside zones of the obstacle; subgoal force is suppressed. Robot C is in the push-away, deceleration, and drive-aside zones of the obstacle; subgoal force is also suppressed. Robot D is in the drive-aside zone of the obstacle; subgoal force is not suppressed here.
experimental robot, which has two drive wheels, include maximum wheel speeds \((v_{\text{max}})\), maximum speed change \((\Delta v_{\text{max}})\) during a sampling period \((T_s)\), and maximum speed difference between the two drive wheels \((\Delta v_{\text{d, max}})\). Thus, these constraints are adopted as references when the virtual force system is designed. During derivation of the virtual force parameters, the SI unit system was used. However, the system can be more easily described by simplifying the correlation between the force and the motion command. Denoting the robot’s velocity change during a sampling period as \(\delta v\), the mass of the robot as \(m\), and the acceleration as \(a\), the force is then

\[
f = ma = m \frac{\delta v}{T_s} \tag{9}
\]

\[
\delta v = \frac{T_s}{m} f. \tag{10}
\]

One can correlate the force with the velocity by properly assigning units of virtual force such that

\[
\delta v = F, \tag{11}
\]

where \(F\) is the measure of force in the newly assigned unit.

The range of force zones depends on the robot’s motion capacity and can be set by the designer. The virtual viscosity coefficient and the spring constant are determined in an iterative manner. The drive-aside force lets the robot detour around obstacles. Its strength must be large enough to move the robot a safe distance away from its original path before the robot is too close to an obstacle. Notably, the range of each zone is expressed in terms of the predicted distances between the robot and obstacles. Thus, appropriate parameters are selected, and the resultant virtual force can guide the mobile robot through a dynamic environment. When there is no obstacle around, the robot is drawn to the goal (subgoal) by goal force. When it encounters an obstacle, the viscous force makes it slow down so it can react smoothly to prevent a collision. The spring force guarantees that the robot does not collide with an obstacle. If necessary, it will run away from the obstacle. The drive-aside force makes the robot edge off the set path to avoid an obstacle on the way. If there is more than one obstacle, the drive-aside forces from different obstacles will cancel each other if they are contradictory. Spring force from different obstacles all push the robot away, so the resultant force will guide the robot toward a free space, if one exists.

4.2. Virtual Force for Planned Paths

In an integrated navigation system, a planned path can help the mobile robot reach its destination more efficiently. However, the planned path cannot always be followed exactly because the environment is dynamic and the robot has to avoid unexpected obstacles. Consequently, in this approach the planned path is used simply as a guide from which subgoals are extracted. The mobile robot only needs to (almost) reach each subgoal in sequence; in between, the trajectory can be flexible to avoid unexpected moving and stationary obstacles. In general, the mobile robot can still reach the destination along a suboptimal yet short route. Thus, the plan is employed to provide sequential subgoals which pull the robot with virtual force.

When the robot arrives at a subgoal has a clear path to the next one, the next subgoal is then taken into the virtual force guidance system. The subgoal force is designed according to situations encountered. When no obstacle is predicted to be around the robot, this force can take any desired form. Normally a constant attraction is suitable. When the robot is close to a subgoal, the force is designed to navigate it toward the subgoal at a moderate speed so it will move smoothly from the current subgoal to the next one. On the other hand, when an obstacle is predicted to be close to the robot’s course toward the subgoal, the subgoal attraction will be suppressed by a decay factor. This factor is determined by the angle measured from the robot’s current position to the locations of the obstacle and subgoal. Examples of the normal and suppressed subgoal forces are shown in Figure 5.

5. SIMULATION RESULTS

Figure 6 illustrates the blackboard system for implementation of the proposed navigation integration. A blackboard system inherently uses its knowledge sources (KSs) very flexibly. In this application, sensors are regarded as KSs, and the sensory data can be employed easily for various functions. This architecture coordinates different functions, including new functions in the future work. The blackboard in the middle of the figure holds computational and current-state data needed by and produced by the KSs (see the data-flow paths). These blackboard
data are represented as attribute–data pairs. The KSs on the two sides of the blackboard are sets of domain knowledge used to solve subproblems in navigation. They are dispatched by an event-based control module (see the control-flow paths) according to the states shown in the blackboard.

Computer simulations have been carried out to verify the integrated navigation performance. The simulated mobile robot is cylindrical with a radius of 30 cm. It is equipped with a ring of 24 ultrasonic sensors, each having a beam opening angle of $22.5^\circ$ and an effective range from 30 to 600 cm. The simulated sensor reading is the nearest distance to an obstacle within the sensor’s beam angle, zero-mean Gaussian noise with 1% distance-proportional standard deviation plus 1 cm standard deviation. Specular reflection is also simulated. It occurs when the wave incident angle is larger than $23^\circ$. In this case, the ultrasonic wave may echo back after multiple reflections or may not come back at all, which depends on the configuration of obstacles around. However, because it is difficult to model the actual specular reflection among real-world objects, the authors adopted a stochastic model according to their experimental data. It is assumed that there is a 10% chance the distance measurement is the real one multiplied by a random number with a Gaussian distribution of mean 3.5 cm and standard deviation 0.5 cm and a 90% chance the measurement is the maximum sensing range. In the simulation, the robot’s maximum speed is 200 cm/s, but it is limited to 160 cm/s when not avoiding an obstacle. The sampling time for navigation is 500 ms. The simulation results presented below are for an indoor environment measuring $33 \times 21$ m.

The simulation environment is depicted in Figure 7a, which originally was not recorded for the mobile robot. Given 11 reference paths as shown in the figure, the robot moved along these paths employing the integrated navigation system four times.
It then built the world model shown in Figure 7b from learning. Figure 7c depicts a path planned for a given task based on the binary map. Note that in Figure 7d, five moving obstacles denoted by Mo1 to Mo5 appeared, static obstacle Ob1 changed its position, and the originally recorded Ob2 disappeared. In Figure 7d, the positions of the robot and moving obstacles are depicted in black and gray circles, respectively, at every sampling instant. The robot positions at every 10 samples are depicted in solid.

Figure 7. Simulation showing that the integrated system can build and update maps, deal with moving obstacles, and adapt to environmental changes. (a) Original environment and exploration path. (b) World model built on-line for the originally unknown environment.
lines. The numbers in the figure indicate the sampling moments at which the positions of the robot and moving obstacles were recorded.

The robot first accelerated to pass Mo1 because of goal attraction and the drive-aside force from Mo1. Note that the robot found there were straight clear paths to the second and third subgoals at the first and second sampling instants, so the source of subgoal-force moved to the second and third subgoals. At the 8th sampling instant, the force from

Figure 7. (c) Initial planned path. (d) Trajectory of motion shows the robot can avoid moving as well as static obstacles smoothly and safely (speed of Mo1 was 100 cm/s, of Mo2 was 130 cm/s, of Mo3 was 90 cm/s, of Mo4 was 88 cm/s, and of Mo5 was 165 cm/s).
Mo2 made the robot turn right. At the 13th sampling instant, the force from Mo3 made the robot turn left to prevent a collision with Mo3. At the 17th sampling instant, the robot passed Mo3 and turned back toward the third subgoal. At the 18th sampling instant, Mo4 was predicted to be in the robot’s path, and its force made the robot begin to turn right to pass it. At the 22nd sampling instant, the drive-aside force from Mo4 accelerated the robot so it left Mo4’s course quickly. The robot continued curving around

Figure 7. (e) Updated world model, from which the tracks of moving obstacles can be seen. (f) Binary map converted from (e), which is close to the new environment.
the circular obstacle Ob1. The plan was modified around this area, and the robot slowed down at the 26th sampling instant because it was close to a newly planned subgoal. At the 31st sampling instant, Mo5 was predicted to be in the robot’s path, and the robot turned right to avoid it. However, unlike when it met Mo4, before it could move fast, Mo5 suddenly intruded and then passed its course. At the 36th sampling instant, it turned slightly left to avoid Mo5. After the 38th sampling instant, the robot moved toward the goal smoothly. Figure 7e depicts the updated map, in which Ob1’s position had been corrected and Ob2 had been eliminated, as expected. The tracks of moving obstacles can be seen on the grid map, but they are invisible on the binary map (Fig. 7f).

In this simulation, the robot controlled its moving direction and speed so well that it was close to a human’s behavior. It accelerated to pass slow obstacle Mo1, took slight turns to keep safe distances from Mo2 and Mo3, took a sharp turn to avoid oncoming obstacle Mo4 and static Ob1, then replanned its path, and finally decelerated to wait for quick Mo5 pass. The whole path was so smooth and nearly every turn or speed change was necessary. Humans with the same sensing capability could hardly do better.

6. EXPERIMENTAL RESULTS

Figure 8 shows the experimental mobile robot developed in the authors’ laboratory. Its diameter is 60 cm and it is about 110 cm high. It has two independent drive wheels and two casters for balance. Its maximum speed is 40 cm/s. A ring of 16 ultrasonic sensors is installed around it at alternating heights of 30 cm and 75 cm with equal angle spans. The effective range of each sensor is 43 to 300 cm. A cycle of all 16 ultrasonic sensor measurements takes about 140 ms. The sampling time for a navigation command is 560 ms. Two encoders attached to the drive wheels and a gyroscope are used for self-localization. The control and computation tasks are distributed among two HCTL-1100s (for servo motor control), an Intel 8751 (for ultrasonic sensor measurements), and an Intel 80486-33 (for other tasks).

The experiments were conducted in corridor of the authors’ laboratory. Only part of the floor (33 × 12 m) was utilized in the experiments, and its original map is as shown in Figure 9a. This is a simplified map in which the details of doors and objects are not illustrated. Figure 9a also shows a path planned in corridors for a given task. Note that there was a long wall in the goal direction at the beginning. The robot could hardly attain its goal without the plan because the goal attraction would be canceled by the virtual forces from the wall. Three previously unrecorded static obstacles (cartons) and two moving obstacles (persons) were present in the experimental environment. Ob3 just blocked the preplanned path. A static obstacle recorded in the previous map had been taken away. Figure 9b illustrates the trajectories of the robot and moving obstacles. Because the speeds of the robot and moving obstacles were relatively low, depicting their positions every sampling instant would be too dense to read. The authors depicted every 4th sampling instant and with dark shading every 20th sampling instant, to make them easier to read.

In the beginning, the robot moved toward its first subgoal. A slight directional change occurred at the 4th sampling instant due to a door frame (prominent in a plane wall) at its left front. From the 44th
to 92nd sampling instants, the robot smoothly passed a slowly moving person. From the 108th to 144th sampling instants, it moved along a straight line at a constant speed in the corridor, a difficult task for general potential field methods. The virtual force system is able to do this because each force is associated with a behavior, and therefore it is easier to design appropriate force. It is also worth noting that the trajectory of the robot during this stage was farther away from the wall than the preplanned path.

Figure 9. Experiment showing that the mobile robot can deal with unexpected obstacles and update its world model in real-time operation. (a) Initial world model and planned path. (b) Trajectory of motion showing the robot avoiding unexpected moving and static obstacles smoothly (speed of Mo1 was 14 cm/s and of Mo2 was 36 cm/s). (c) Updated grid map, in which previously unknown obstacles are reported.
path, resulting in safe navigation. The robot turned right at the 144th sampling instant because of a closed door at its left front. It then traveled around Ob2 and Ob3 through the middle of the free area. At the 196th sampling instant, the robot began turning right because of Mo2. However, Mo2 moved fast, and the robot had no chance to move toward the goal in front of Mo2. Consequently, it began to turn left again at the 208th sampling instant and then moved toward the goal after Mo2 no longer blocked its path. The updated map is depicted in Figure 9c. Figure 10a shows the binary map converted from Figure 9c. It was observed that three previously unknown static obstacles were recorded, and an old static obstacle had been removed from the map because it was not present in the environment. The closed doors were also perceived. Part of Mo1’s track was recorded in the map because it moved slowly. However, this was only temporary.

Continuing the experiment, this time the robot traveled back to the previous starting point. The planned path (Fig. 10a) was not blocked by any position-changed static obstacles. With this correct plan resulting from map-learning, the robot moved faster than its previous journey, especially when traveling around Ob3 (Fig. 10b). At the 84th sampling instant, the robot predicted Mo1 would be close and turned left to avoid it. Mo2 came along later, and the robot turned right to avoid it at the 104th sampling instant. Because the robot had been very close to Mo1 and Mo2, the spring force from Mo1 and Mo2 pushed it away at the 92nd and 112th sampling instants, respectively. After the robot passed Mo2, it traveled smoothly to the goal. Note that, without the reactive part, the robot would have collided with the moving obstacles. The updated map is shown in Figure 10c and 10d. Note that the track of Mo1 in the last experiment has

![Figure 10](image-url)
disappeared. This experiment reveals that the robot can navigate safely and smoothly in a dynamic environment. The proactive and reactive navigation algorithms are integrated to give satisfactory results. Because of the accumulated errors, the positioning errors at the final positions in this round-trip experiment were 15 and 17 cm, respectively. A landmark approach can be employed to compensate for this accumulated error. Compared to the traveling distance over 30 m, these small errors implied that the robot can run a long distance without losing its position if only a few landmarks are available.

7. CONCLUSIONS

This paper presents an integrated navigation system for an intelligent autonomous mobile robot in dynamic environments. A new method is proposed for integrating local reactive navigation with a proactive plan. This method is based on the virtual-force concept, which assumes that each navigational resource exerts virtual force on the robot to produce desired motion changes. This approach has the advantage of integrating various resources with different degrees of abstraction in a uniform manner. To deal with moving obstacles, a real-time sensory predictor is used so that the robot can react to environmental changes more efficiently. A grid map is maintained for path planning by using a first-order digital filter, a simple, effective way to update the map on-line. Consequently, the robot always has an up-to-date world knowledge whenever it plans a global reference path. Bidirectional DT has been developed for fast path planning based on a recorded grid map. This method has the advantage of employing previously planned information to find new global paths when the robot needs to replan because of considerable environmental changes.
Simulation and experimental results reveal that the integrated navigation system can cope with complex, changing environments. However, more reliable navigation performance still depends on the resources employed. Problems involving the robot's perception capabilities still need to be overcome. Currently, studies are being conducted to add a vision system to compensate for the ultrasonic sensors employed for navigation. With a vision system, self-localization of the robot can also be made more accurate, which will help overcome the accumulated error problems. All these extensions can be realized using the proposed architecture.

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