An alternative bend-testing technique for a flexible indium tin oxide film

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Abstract

The two-dimensional refractive index distribution of a flexible indium tin oxide film deposited on a PET layer is measured before/after the bend-testing with an alternative technique based on Fresnel equations and the heterodyne interferometry. Their standard deviations are derived and they vary more obviously than the resistance variations measured in the conventional method. Hence the standard deviation of the refractive index can be used as the indicator to justify the durability of a flexible indium tin oxide film. The validity is demonstrated.

1. Introduction

Due to the high optical transmittance and the high conductivity of an indium tin oxide (ITO) film, it is widely used as the electrode for flat panel display devices, solar cells and organic light emitting diodes (OLED) [1]. In practice, the electronic patterns are printed on a thin ITO film deposited on a polyethylene terephthalate (PET) layer with laser patterning processes [2] to fabricate a flexible electronic substrate. The residual stress in part areas on the film caused by the temperature variation during the processes affects its quality and lifetime. The bending test can make the effect of the residual stress to be more obvious [3–7], so the resistance variation after definite bending cycles is always used as an indicator to justify its durability. However the resistance measurement is less sensitivity and the durability test becomes tedious due to its time-consuming bending cycles. To improve the sensitivity of this test, the two-dimensional microscopic refractive index distribution variations are observed instead of the conventional single-value resistance measurement.

Due to its photoelasticity [8], its refractive index is related with the residual stress. An alternative technique for measuring the two-dimensional refractive index distribution is presented based on Fresnel equations and the heterodyne interferometry. In this method, a collimated linearly/circularly polarized heterodyne light beam in turn enters a modified Twyman-Green interferometer, in which an ITO film is located in one arm for test. Two groups of full-field interference signals are taken by a fast CMOS camera. The sampling intensities recorded at each pixel are fitted to derive a sinusoidal signal, and its associated phase can be calculated. Then, substituting these two groups of phase distribution data into the special equations derived from Fresnel equations, its two-dimensional refractive index distribution and the standard deviation can be estimated. This film is tested before/after some different bending cycles. The standard deviation varies more obviously than the resistance variation measured with the conventional method. Hence the standard deviation of the two-dimensional refractive index distribution can be used as an indicator to justify its durability. The validity of this technique is demonstrated.

2. Principle

Fig. 1 shows a schematic diagram of this technique. For convenience, the +z-axis is chosen to be along the light propagation direction and the +y-axis is along the direction pointing out the paper plane. A light beam coming from a heterodyne light source [9] has a frequency difference \( f \) between the x- and the y-polarizations, and its Jones vector can be written as [10]

\[
\hat{E}_1 = \frac{1}{\sqrt{2}} \left( e^{i\phi} \right).
\]  

The light beam is expanded and collimated by a beam expander BE. It enters a modified Twyman-Green interferometer, which consists of a beam-splitter BS, a quarter-wave plates Q2 with the fast axis at 45° with respect to the y-axis, a reference mirror M, a test sample S, an analyzer AN with the transmission axis at 0° with...
Fig. 1. Schematic diagram of this technique. LS: laser light source; EO: electro-optic modulator; FG: function generator; VA: voltage linear amplifier; BE: beam expander; Q: quarter-wave plate; BS: beam-splitter; M: mirror; S: sample; AN: analyzer; IL: imaging lens; MO: microscopic objective; DL: doublet; C: CMOS camera.

respect to the y-axis, an imaging lens IL, and a CMOS camera C. In this interferometer, two optical paths are (1) BS → Q2 → M → Q2 → BS → AN → IL → C (the reference beam), and (2) BS → S → BS → AN → IL → C (the test beam). For convenience, we firstly assume that the S is an isotropic material. So, their amplitudes can be derived and expressed as

\[
E_{r1} = (AN(0') \cdot R_{BS} \cdot Q_{2(45')} \cdot M \cdot Q_{2(45')} \cdot E_{1}) \cdot e^{i\phi_{1}}
\]

\[
= \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} e^{-i\phi_{1}/2} & 0 \\ 0 & e^{i\phi_{1}/2} \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ i & 0 \end{pmatrix} \begin{pmatrix} -r_m & 0 \\ 0 & r_m \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ -i & 1 \end{pmatrix} \begin{pmatrix} 0 \end{pmatrix}.
\]

(2)

and

\[
E_{t1} = (AN(0') \cdot S \cdot R_{BS} \cdot E_{1}) \cdot e^{i\phi_{2}}
\]

\[
= \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} 0 & -r \\ 0 & r \end{pmatrix} \begin{pmatrix} e^{-i\phi_{2}/2} & 0 \\ 0 & e^{i\phi_{2}/2} \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ -i & 1 \end{pmatrix} \begin{pmatrix} 0 \end{pmatrix}.
\]

(3)

Here, \( R_{BS} \), \( M \) and \( S \) are the reflection matrix of the BS, M and S; \( r_m \) and \( r \) are the reflection coefficients of the M and the S; \( \phi_{1} \) and \( \phi_{2} \) are the phase variations due to the optical path lengths of the reference and test beam, respectively. \( \phi_{1} \) is the phase difference between the x- and y-polarizations coming from the reflection at BS. Thus, the interference signals recorded by the C can be written as

\[
I_A = |E_{r1} + E_{t1}|^2 = I_{01} + \gamma_1 \cdot \cos(2\pi ft + \phi_1)
\]

\[
= \frac{1}{2} \left[ r^2 + r_m^2 - 2rr_m \cos(2\pi ft + \phi_1 - \phi_2 + \frac{\pi}{2}) \right],
\]

(4)

where \( I_{01} \), and \( \gamma_1 \) and \( \phi_1 \) are the mean intensity, the visibility and the phase of the interference signal, respectively. From Eq. (4), we have

\[
\phi_1 = \frac{\pi}{2} - (\phi_{d1} - \phi_{d2}).
\]

(5)

Secondly, the quarter-wave plate \( Q_1 \) with the fast axis at 45° to the y-axis is inserted into the optical setup as shown in Fig. 1 and the light amplitude becomes

\[
E_2 = Q_{1(45')} \cdot E_1 = \begin{pmatrix} 1 & -i \\ i & 1 \end{pmatrix} \begin{pmatrix} e^{i\phi_{1}} \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \cos(\pi ft) - \sin(\pi ft) \\ \cos(\pi ft) + \sin(\pi ft) \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & -i \end{pmatrix} e^{i\phi_{1}} + \begin{pmatrix} 1 & -i \end{pmatrix} e^{-i\phi_{1}}.
\]

(6)

From Eq. (6), we can see that there is a frequency difference \( f \) between the right- and the left-circular polarizations, and it is a circularly polarized heterodyne light beam.

The amplitudes of the reference beam and the test beam can be derived as above and expressed as

\[
E_{r2} = (AN(0') \cdot R_{BS} \cdot Q_{2(45')} \cdot M \cdot Q_{2(45')} \cdot E_{2}) \cdot e^{i\phi_{2}}
\]

\[
= \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} e^{-i\phi_{2}/2} & 0 \\ 0 & e^{i\phi_{2}/2} \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ i & 0 \end{pmatrix} \begin{pmatrix} 0 \end{pmatrix}.
\]

(7)

and

\[
E_{t2} = (AN(0') \cdot S \cdot R_{BS} \cdot E_{2}) \cdot e^{i\phi_{2}}
\]

\[
= \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} 0 & -r \\ 0 & r \end{pmatrix} \begin{pmatrix} e^{-i\phi_{2}/2} & 0 \\ 0 & e^{i\phi_{2}/2} \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & i \\ -i & 1 \end{pmatrix} \begin{pmatrix} 0 \end{pmatrix}.
\]

(8)

Here the interference signals measured by the C can be written as

\[
I_B = |E_{r2} + E_{t2}|^2 = I_{02} + \gamma_2 \cdot \cos(2\pi ft + \phi_2)
\]

\[
= A \cdot \cos(2\pi ft) + B \cdot \sin(2\pi ft) + C,
\]

(9)
where \( I_{pq} \), \( \gamma_2 \) and \( \phi_2 \) are the mean intensity, the visibility and the phase of the interference signals, respectively. \( A \), \( B \), and \( C \) are real numbers. Here we have
\[
A = r_{rm} \sin(\phi_{d1} - \phi_{d2}) \quad \text{and} \quad B = \frac{1}{2}(r_m^2 - r^2).
\]

From Eq. (10), the phase can be calculated as
\[
\phi_2 = \tan^{-1}\left( \frac{B}{A} \right) = \cot^{-1}\left[ \frac{2r_{rm} \sin(\phi_{d1} - \phi_{d2})}{(r_m^2 - r^2)} \right].
\]

According to Fresnel equations [10], \( r \) can be derived by substituting Eq. (5) into Eq. (11) and expressed as
\[
r = -\frac{\cos \phi_1 + \sqrt{\cos^2 \phi_1 + \cot^2 \phi_2}}{\cot \phi_2} r_m = \frac{n - 1}{n + 1},
\]
where \( n \) is the refractive index of \( S \). Eq. (12) can be rewritten as
\[
n = \frac{\cot \phi_2 - r_m \cos \phi_1 + r_m \sqrt{\cos^2 \phi_1 + \cot^2 \phi_2}}{\cot \phi_2 + r_m \cos \phi_1 - r_m \sqrt{\cos^2 \phi_1 + \cot^2 \phi_2}}.
\]

The camera \( C \) with the frame frequency \( f_c \) is used to record \( m \) frames at time \( t_1, t_2, \ldots, t_m \). Each pixel records a series of interference intensities \( I_{1p}, I_{2p}, \ldots, I_{mp} \), which are the sampled intensities of a sinusoidal signal. The data of \( \phi_1 \) and \( \phi_2 \) can be derived by using the absolute phase determination method [11] and the least-square sinusoidal fitting algorithm [12]. If these processes are applied to all other pixels, then the associated data \( \phi_1(x,y) \) and \( \phi_2(x,y) \) can be obtained similarly. Substitute them into Eq. (13), the refractive index distribution \( n(x,y) \) can be calculated.

In reality, the \( S \) is a photoelastic material, its Jones matrix \( S \) in Eq. (3) and Eq. (8) should be modified and represented as
\[
S = \begin{pmatrix}
  r_{pp} & r_{pa} \\
  r_{ap} & r_{ss}
\end{pmatrix}.
\]

Consequently, \( \phi_1 \) and \( \phi_2 \) can be derived again with two simultaneous equations Eqs. (3) and (4) and Eqs. (8) and (9), and they can be written as
\[
\phi_1 = \tan^{-1}\left[ \frac{r_{rm} \sin(\phi_{d1} - \phi_{d2}) + r_{mp} \sin \phi_1}{r_{mp} \sin(\phi_{d1} - \phi_{d2}) - r_{rm} \cos \phi_1} \right],
\]
\[
\phi_2 = \cot^{-1}\left[ \frac{2r_{pp} \sin(\phi_{d1} - \phi_{d2}) - r_{pp} \cos \phi_1}{r_m^2 - r_{pp}^2 + r_{pp}^2 - 2r_{pp} \sin(\phi_{d1} - \phi_{d2})} \right],
\]
where \( r_{pp} = \frac{(n_a - n_0) \cos 2\phi_y + n_0 - 1}{(n_a + 1)(n_a - 1)} \), \( r_{mp} = \frac{(n_a - n_0) \sin 2\phi_y + n_0 - 1}{(n_a + 1)(n_a - 1)} \), \( n_a \) is the ordinary refractive index, \( n_0 \) is the extraordinary refractive index and \( \alpha \) is the angle between the principal axis of the stress and the \( y \)-axis. Substitute Eq. (15) and Eq. (16) into Eq. (13), the relationship between \( n \) and the refractive index variation \( \Delta n \) caused by the residual stress can be obtained, where \( \Delta n = n_e - n_o \) is also known as the birefringence. Because a two-dimensional photoelastic model exerted by the forces in its own plane will behave as a general retarder [8], the retardation induced by \( \Delta n \) is proportional to the associated stress variation. Under the experimental conditions \( r_m = 99\% \), \( \phi_{d1} = 10^\circ \), \( \phi_{d2} = 10^\circ \) and \( n_o = 1.8 \), the relationship between \( n \) and \( \Delta n \) can be calculated and depicted in Fig. 2 at \( \alpha = 0^\circ \), 30°, 60° or 90° by substituting Eqs. (15) and (16) into Eq. (13). From this figure, we can see that the measured data of \( n \) is quasi-linear to the stress if \( \alpha \neq 90^\circ \). Although the principal axis of the stress at each pixel is different from others, the standard deviation can be measured to show the effect of the residual stress as the resistance measurement in the conventional method.

3. Experiments and results

To demonstrate the validity of this technique, an ITO film sample coated on PET layer (CPFilms/OC100) was tested. The isolation lines with about 0.85 mm pitch were printed on the ITO film with laser patterning processes. It was originally a plane plate as shown in Fig. 3a, where the gray, the white and the black parts represent the ITO film, the PET layer and the isolation lines, respectively. Under the bending test, it was bent with a constant bending force \( F \) applied on its two sides simultaneously as shown in Fig. 3b. Then, the bending force was removed and it became a plane plate again. In our tests, it was bent with a bending machine (ITRI-CMS/FCIS/08) under the conditions of 20 mm bending radius, 20°/s bending angular speed, and 8 cycles/min bending frequency. Although it has a 60 mm × 60 mm dimension, only a 260 μm × 260 μm area near its center with higher stress caused by the bending test was measured, as shown in Fig. 3a. An He–Ne laser with 632.8 nm wavelength, an electro-optic modulator (New Focus/Model 4002), a CMOS camera (Basler/A504 K) with 8-bit gray levels and 350 × 350 pixels, a reference mirror with \( r_m = 99\% \) and a 10× imaging lens IL were used. To measure the full-field absolute phase, the saw-tooth voltage signal with the amplitude \( V \) being lower than its half-wave voltage \( V_h \) was applied to drive the EO, the phase at the break-point position of the periodical sinusoidal segment was used to be the reference phase [11]. Under the conditions \( f = 20 \text{ Hz}, V_x = 144 \text{ V}, V = 120 \text{ V} \) and \( f_c = 300 \text{ frames/s} \), 300 frames were taken in 1 s each time. For easier reading, the measured results of the two-dimensional refractive index distribution are displayed in color. Fig. 4 shows the results before bending, and Fig. 5a and b show the results after bending 1000 cycles and 4000 cycles, respectively. The mean values of the measured area can be calculated and they are 1.855, 1.849 and 1.811, respectively; that is, they have 0.32% and 2.37% variations. Their associated standard deviations can also be derived and they are 0.006, 0.008, and 0.033, respectively. So, they have 33% and 450% variations.

4. Discussion

For comparison, the resistances of this sample were also measured before/after bend-testing by a digital multimeter (Model 2700, Keithley Instrument Inc.). The nodes are located as shown in Fig. 3a. The measured resistances of the above three situations are 2.613 kΩ, 2.623 kΩ and 2.674 kΩ, respectively. They have 0.38% and 2.33% variations. For easy understanding, the variations
of two methods and the standard deviation measured with this method are depicted in Fig. 6. Either the resistance or the mean value of the refractive index acts as an average effect inside the conduct area, so they have consistent variations as shown in Fig. 6. From this figure, we can infer that the standard deviation of the refractive index may be used as an indicator to justify the durability of the ITO film. It varies more sensitively than the resistance does.

To collect the reflected parallel beam from the ITO surface and magnify the object simultaneously, it is better to use the imaging lens IL composed of a microscopic objective (MO) and a doublet (DL). Because the IL is an afocal optical system, the ITO surface needs to be located in the front focal plane of the MO and the image plane of the CMOS camera should be correspondingly located in the rear focal plane of the DL. The transverse magnification of the IL in our experiments is $10$.

All the lower left circles in Figs. 4, 5a and b have larger refractive index variations, so it has more residual stress. Comparing the data in these three circles, we can see that the residual stress increases with more bending cycles [3–5]. This tendency can be also found in two other circles in Fig. 5a and b.

5. Conclusion

The two-dimensional refractive index distribution of an ITO film deposited on a PET layer has been measured before/after bend-testing with an alternative method based on Fresnel equations and the heterodyne interferometry. The variation of the standard deviation is larger than the resistance variation measured in the
conventional method, so it may be used as the indicator to justify its durability. The validity has been demonstrated.

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References