Solid solution strengthening and phase transformation in high-temperature annealed Si$_{80}$Ge$_{20}$ alloy

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This investigation demonstrates the temperature-dependent mechanical properties of Si$_{80}$Ge$_{20}$ alloy films via a nanoindenter in the indentation depth of 100 nm. The roughly equal root mean square roughness ($R_{rms}$) values and repeatable load–displacement ($P$–$\delta$) curves for the samples ensure the mechanical performance mainly contributed from the influences of annealing temperatures. The hardness ($H$) values of samples increase with the temperatures of an initial annealing in the range from RT to 900°C, and, conversely, decrease for annealing temperatures over 900°C. Accordingly, both $E/H$ and $h/h_{max}$ values, exhibiting an inverse tendency in the above temperature range, hints that the solid solution strengthening effect and the softening phenomenon occur for the initial-annealing and over-annealing stages, respectively. In addition, grazing incidence X-ray diffraction (GIXRD) analysis demonstrates the lattice expansion and the broadened peak that attribute to the solid solution strengthening of samples and the segregation of Ge, respectively. Through observing the value of the (200) lattice spacing of 5.624 Å for a 900°C-annealed sample by transmission electron microscopy (TEM) analysis, it is verified that the segregation of Ge is responsible for the decreased hardness for the 1000°C-annealed sample.

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1. Introduction

Given several attractive features including tunable band gaps, high carrier densities, a complete solid solution character, and high thermal conductivity, silicon–germanium (Si–Ge) alloys are considered as potential materials for the applications for solar cells [1], photodetectors [2], light-emitting diodes [3], integrated optical [4] and photovoltaic [5] devices, heterojunctions [6], one-dimensional devices [7], standard resistors [8], and single-grain thin-film transistors [9]. Owing to the high quality of thin films, an ultrahigh-vacuum chemical deposition (UHV-CVD) is one of the popular procedures for the fabrication of Si–Ge films. Because of a thermal dissociation of precursors (e.g., silane and germane) and rapid deposition, UHV-CVD yielded metastable defects, and many researchers made efforts to overcome this problem. Kriringhøj et al. [10] relaxed the lattice strain of the Si$_{0.915}$Ge$_{0.085}$ alloy film by annealing samples at 1100°C. Parnis et al. [11] averaged magnitudes of fluctuations of X-ray diffraction spectra using a novel simulation procedure, and quantitatively characterized the degree of a structural disorder for the Si$_{0.75}$Ge$_{0.25}$ film. For the Si$_{0.5}$Ge$_{0.5}$ film, Whiteaker et al. [12] showed an increase of the averaged order parameter with increasing thickness, but then a decrease with the thickest film of 1000 Å. These features elucidate the importance of the phase- and the defect- controls for ultra-thin Si–Ge alloy films. Except for the physical properties mentioned above, the mechanical performances for Si–Ge films are also influenced from the micro- or nano-scaled imperfections. Under the annealing treatments from RT to 1000°C, this study seeks to investigate the effects of detailed structural transformations on mechanical behaviors of a Si$_{80}$Ge$_{20}$ film. Predictably, the mechanism of mechanical variations could be inferred via a grazing incidence X-ray diffraction (GIXRD) and transmission electron microscopy (TEM).

2. Experimental details

An ultra-high vacuum chemical vapor deposition (UHV-CVD) system was applied for depositing Si–Ge alloy films on the P-type Si(100) substrates. The substrates were pretreated using a standard Radio Corporation of American (RCA) procedure [13] and a 15-s immersion in the solution mixed with HF and H$_2$O (1:50 in volume ratio). Initially, a 120-nm Si–Ge layer was deposited at 500°C for 43 min from the mixed atmosphere of SiH$_4$ (85 sccm) and GeH$_4$ (15 sccm) maintained at 10$^{-7}$ mbar. Consequently, the...
10-nm Si buffer layer was deposited on the Si substrate at 500 °C for 100 min from pure SiH4 (5 sccm) at 10⁻⁷ mbar. The SiGe and Si buffer layers were deposited following four cycles till the total thickness of film reached 530 nm. After film fabrication, a composition of films was confirmed as Si₈₀Ge₂₀ via an electron probe microanalyzer (EPMA, JEOL JAX-8800). The temperatures of annealing treatments for Si₈₀Ge₂₀ films were RT, 800, 900, and 1000 °C for 30 min in argon atmosphere. A nanoindentation measurement system (Hysitron) equipped with atomic force microscopy (AFM, Digital Instruments Nanoscope III) was applied for recording the load–displacement (P–δ) curves of the alloy films. The test strain rate was at 0.05 s⁻¹, and each P–δ curve was repeated at least three times to ensure reproducibility. The surface morphologies of as-synthesized and indented samples were observed using the conjunct AFM. The grazing incidence X-ray diffraction (GIXRD) instrument used was a Shimadzu XRD-6000 with Cu Kα radiation operated at 30 kV and 20 mA. The scanning speed was 1°/min. After the sample preparation by a focus ion beam (FIB), the cross-sectional-transmission electron microscopy (TEM) images of a 900 °C-annealed film were recorded using a JEOL JEM-2100F operating at 200 keV.

### 3. Results and discussion

In order to exclude a measurement error resulting from the excessive surface deviation, AFM was applied to inspect the topological morphology for the samples before the indentation measurement. Fig. 1(a) displays the AFM image for the RT-annealed sample with the root mean square roughness (Rrms) value of 37.40 nm. A 3D-curved surface with no abnormal cracks represents the films well grown via the UVH-CVD system. An AFM analysis obtained from the samples is as follows. The Rrms Values of 800 °C-, 900 °C-, and 1000 °C-annealed films are 35.30, 36.45, and 33.83 nm, respectively. Notice that these Rrms values are much smaller than the maximum indentation depth (100 nm). Therefore, one can rule out the extrinsic deviations of mechanical properties which were varied with the surface condition of the sample. Next, we take the RT-annealed film, for example, to represent the closely experimental results for the samples in this study. Fig. 1(b) demonstrates the 2D AFM image for the RT-annealed sample after the indentation test. As observed in the central indentation zone, a regular triangle with no crack, shows that the pressure is uniformly applied on the sample. Fig. 1(c) reveals the load–displacement (P–δ) curves obtained from the nanoindenter. As the repeated curves are well stacked with each other, it implies a good reproducibility of our measurements. The arrows indicated, hmax, h, and hmax are the maximum indentation depth, the contact depth, and the final depth, respectively. Herein, the parameters related to the mechanical performance in this article are referred as above. To probe mechanical characteristics in advance, Table 1 lists parameters as revealed by elastic modulus (E), hardness (H), E/H, the final displacement after complete unloading (h), the maximum indentation depth (hmax), and h/hmax. One can see that the H value increases with the annealing temperature in the initial stage (from RT to 900 °C), and further decreases with that in the final stage (>900 °C). Besides the primitive H value, complex parameters including E/H and h/hmax values yield useful information to elucidate an interior mechanical character of materials. In comparison with H values, both E/H and h/hmax values appear to have an inverse tendency as a function of annealing temperature (See Fig. 2). The most important difference between E/H and bare H values is that E input to E/H truly specifies the substantial elastic recovery for a material. Owing to the insignificant influence of E, the ratio (E/H) does not vary much for different pure brittle solids [14]. In this study, the E/H values strongly depend on the annealing temperatures. This helps in providing the phase transformation insight into the hard metal matrix after a thermal treatment. Zhou et al. [15] fabricated alloys with the composition of AlCoCrFeNiTi₅ (x=0, 0.5, 1.0, 1.5), and gradually increased E values with adding a Ti element. Based on the BCC solid solution lattice, the lattice distortion

### Table 1

<table>
<thead>
<tr>
<th>Sample condition</th>
<th>E (GPa)</th>
<th>H (GPa)</th>
<th>E/H</th>
<th>h (nm)</th>
<th>hmax (nm)</th>
<th>h/hmax</th>
</tr>
</thead>
<tbody>
<tr>
<td>RT annealing</td>
<td>182.5 ± 0.8</td>
<td>12.3 ± 0.2</td>
<td>14.83</td>
<td>13.8</td>
<td>50.8</td>
<td>0.261</td>
</tr>
<tr>
<td>800 °C annealing</td>
<td>188.3 ± 0.4</td>
<td>12.9 ± 0.1</td>
<td>14.59</td>
<td>13.3</td>
<td>50.8</td>
<td>0.261</td>
</tr>
<tr>
<td>900 °C annealing</td>
<td>190.1 ± 0.7</td>
<td>13.1 ± 0.1</td>
<td>14.51</td>
<td>13.0</td>
<td>50.6</td>
<td>0.256</td>
</tr>
<tr>
<td>1000 °C annealing</td>
<td>186.1 ± 0.5</td>
<td>12.5 ± 0.2</td>
<td>14.88</td>
<td>13.5</td>
<td>50.9</td>
<td>0.256</td>
</tr>
</tbody>
</table>

**Fig. 1.** (a) 3-d AFM image of RT-annealed Si₈₀Ge₂₀ alloy films before the indentation, (b) 2-d AFM image of RT-annealed film after the indentation, and (c) the P–δ curves repeated for three times for RT-annealed sample in the depth of 100 nm, where h, h, and hmax are the contact depth, the final depth, and the maximum indentation depth, respectively.

**Fig. 2.** The temperature-dependent plots of H, E/H, and h/hmax values for the samples, where H, E, h, and hmax are the hardness, the elastic modulus, the final displacement after complete unloading, and the maximum indentation depth, respectively.
energy will increase significantly and the solid solution strengthening will be enhanced because a Ti atom, with a larger atomic radius, occupies the lattice sites. Hence, $E$ undoubtedly increases with $x$ in AlCoCrFeNiTi$_x$. Inferred from the Si–Ge phase diagram [16], the incensement of $E/H$ ratio with elevating the annealing temperature from RT to 900 °C can be explained via the same mechanism since $Si_{80}Ge_{20}$ is basically a diamond-like solid solution. However, the mechanism of the descending hardness while temperature surpassing 900 °C needs detailed verification. The $h/f_{\text{max}}$ acquired from the unloading $P-\delta$ curve can be used to clarify the sample in the nanoindentation experiment; the natural limits for the $h/f_{\text{max}}$ parameter are $0 \leq h/f_{\text{max}} \leq 1$, where the lower limit and the upper one correspond to the full elastic deformation and a rigid-plastic behavior [17]. On the basis of $h/f_{\text{max}} < 0.7$, dominated by the sink-in effect [18], the decreasing of $h/f_{\text{max}}$ values from RT to 900 °C could be suspected for the solid solution strengthening which is considered as a weak type of hardening. Fig. 3 shows the XRD patterns for the $Si_{80}Ge_{20}$ alloy films after RT-, 800 °C-, 900 °C-, and 1000 °C-annealing treatments, respectively. Three main groups of peaks are locating around 66.6°, 67.0, 67.8, and 69.2°, corresponding to pure Ge, Si–Ge alloy, and Si substrate, respectively. As the red-dashed line indicated, the peaks are attributed to the Si–Ge(400) plane-shift leftward with the temperatures ranging from RT to 900 °C, and correspondingly show a right shift for temperatures higher than 900 °C. The lattice parameters of RT-, 800 °C-, 900 °C-, and 1000 °C-annealed samples are 5.519, 5.521, 5.524, and 5.515 Å, respectively. It implies that the lattice parameters of the investigated Si–Ge films increase with the temperatures from RT to 900 °C but then reduce with temperatures greater than 900 °C. The expansion of the lattice parameters strongly supports the solid solution strengthening mechanism to cause the hardness increasing that varies with the annealing conditions. The processing of Si–Ge films involves thermal dissociations of SiH$_4$ and GeH$_4$ gases. Unavoidably, a small amount of pure elemental Ge or Si exists in the as-synthesized film. The annealing treatment promotes entire mixing of alloying elements, and accompanies the solid solution strengthening effect. Notice that the lattice parameters of Si and Ge are 5.43 Å [19] and 5.65 Å [20], respectively. The peak shifting leftward signifies increasing of the lattice parameter which warrants dissolving the elemental Ge atoms into the Si-based matrix in the annealing process. Thus rather instead of a pure Si lattice, an enlarged lattice parameter occurs. On the other hand, the over-annealing treatment (> 900 °C) denotes the hardness effect. As the experimental segregation enthalpy of Si–Ge alloy is only $5.3 \pm 0.5$ kJ mol$^{-1}$ [21], the precipitation of elemental Ge causes the decayed hardness, after Ge atoms get enough thermal energies to overcome the activation barrier. As displayed in Fig. 3, the broadened Ge peak at 900 °C points to the presence of amorphous Ge, while the raised Ge peak at 1000 °C displays the nanoscaled Ge. The precipitation of Ge not only weakens the solid solution strengthening but also creates the right shift of the peak. Fig. 4(a) shows the bright-field (BF) TEM micrograph including the Si substrate, the Si–Ge alloy films, and the ultra-thin silicon buffer layers for the samples after the 900 °C annealing. Fig. 4(b) exhibits the high resolution (HR) lattice image obtained from the blue rectangle marked in Fig. 4(a). As shown in the upper-inset figure, the lattice spacing with the value of 2.812 Å roughly satisfies the spacing of the (200) plane for the Si–Ge alloy. Fig. 4(d) demonstrates the selected area diffraction patterns (SADP) obtained from the region shown in Fig. 4(b). As can be seen, the [1–1], [200], [11–1] spots from the [110] zone axis confirms existence of the diamond cubic structure. The lattice spacing calculated from the (200), the experimental lattice parameter in Fig. 4(b) is 5.624 Å, evidencing segregation of Ge (Notice..

Fig. 3. The GIXRD patterns for the samples annealed at different temperatures.

Fig. 4. The cross-sectional TEM morphology of 900 °C annealed film. (a) The bright filed image of the region including the Si substrate, Si–Ge alloy films, and ultra-thin silicon buffer layers. (b) The HR lattice image obtained from the blue rectangle marked in (a). (c) The HR lattice image enlarged from the red rectangle marked in (a). (d) The selected area diffraction patterns (SADP) of (b). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
that the lattice parameter of pure Ge is 5.650 Å [20]]. This result validates our conjecture that the decreasing hardness is contributed by the Ge cluster once again. In addition, Fig. 4(c) shows the HR lattice image (The upper-inset figure displays in enlarged scale) for the area marked with the red rectangle in Fig. 4(a). Corresponding to the quartz (151) plane, the referred lattice spacing (2.913 Å, JCPDS: 2-471) and the experimental one (2.905 Å) are close to each other. It expresses the presence of SiO2 on the top layer of the alloy film, even though the sample was annealed in the Ar atmosphere.

4. Conclusion

This study investigates the mechanical performances of Si80Ge20 alloy films annealed at RT, 800 °C, 900 °C, and 1000 °C, respectively. The samples were indented in the depth of 100 nm to probe the intrinsic mechanical properties in avoidance of the extrinsic disturbances including the abnormal crack and the excess deviation of roughness. Recorded from the load–displacement curves, the hardness value increases with the annealing temperature ascended from RT to 900 °C, and further deceases with that elevated higher than 900 °C. Accordingly, both $E/H$ and $h_{\text{max}}$ values appearing an inverse tendency in the above temperature range hints the occurrence of the solid solution strengthening, and implies a soft phase segregating at a temperature higher than 900 °C. Meanwhile, XRD analysis demonstrates that the lattice expansion and the broadened peak attribute to the solid solution strengthening of Si80Ge20 and the segregation of Ge, respectively. Expected as a symptom of the abruptly descended hardness for 1000 °C-annealed sample. TEM analysis evidences the segregation of Ge for the 900 °C-annealed one in the presence of the (200) lattice spacing of 5.624 Å.

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