A hierarchical multiple-model approach for detection and isolation of robotic actuator faults

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**A B S T R A C T**

Modern robotic systems perform elaborate tasks in complicated environments and have close interactions with humans. Therefore fault detection and isolation (FDI) schemes must be carefully designed and implemented on robotic systems in order to guarantee safe and reliable operations. In this paper, we propose a hierarchical multiple-model FDI (HMM-FDI) scheme to detect and isolate actuator faults of robot manipulators. The proposed algorithm performs FDI in stages and refines the associated model set at each stage. Consequently only a small number of models are required to detect and isolate various types of unexpected actuator faults, including abrupt faults, incipient faults, and simultaneous faults. In addition, the computational load is alleviated due to the reduced-sized model set. The relation between the fault detection stage of the HMM-FDI scheme and the likelihood ratio test is explicitly revealed and theoretical upper bounds of the false alarm and missed detection probabilities are evaluated. Then we conduct experiments to demonstrate the ability of the HMM-FDI scheme in successful and immediate detection and isolation of actuator faults.

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1. Introduction

Robotic systems are widely used to carry out various missions that require high precision, reliability and safety. Typical robotic applications are, to name a few, a manufacturing industry, demeaning, hazardous waste cleanup, and outer space exploration. In addition, recent advances in intelligent robots have inspired a large number of emerging applications such as housekeeping, medical surgeries, and the elderly home care. In order to accomplish these increasingly elaborate tasks, modern robots turn into ever complicating systems. However, the more complex the robotic systems are, the more likely they are to break down. Unfortunately, the unexpected breakdown may either incur a cost that is too high to be affordable (e.g. interruption of a space mission), or even worse, cause damage to users and their property due to close interactions with humans and environments. Therefore, faults of robotic systems must be taken care of properly in order to guarantee their safe operation. Procedures for dealing with faults include (i) detecting the occurrences of faults (fault detection), (ii) indicating faulty components (fault isolation), (iii) identifying features of faults (fault identification), and (iv) accommodating faults by dedicated control algorithms (fault tolerant control).

Fault detection and isolation (FDI) schemes have been investigated over the past three decades [1–3], and have been successfully applied to various safety-critical systems such as nuclear plants [4], flight control systems [5], vehicular drive-by-wire systems [6], automated highway systems [7,8], and robotic systems [9,10]. Commonly used techniques include state and parameter estimation [11–17], parity equations [18,19], neural networks [20,21], and multiple-model (MM) approaches [22–26]. On the other hand, fault tolerant control (FTC) can be realized with or without explicit FDI schemes [7,27–29]. In particular, applying FTC to robotic systems has drawn a lot of attention in the past [30–32].

In the aforementioned studies, faults are represented as either additive signals or multiple models. The former usually results in a complicated fault signal which is a function of the system state. Hence the fault signal cannot be treated as external disturbances, making it challenging to analyze and synthesize the FDI schemes. On the other hand, the latter represents each fault by a specific model that might be simple and structurally different from one another. Thus the multiple-model fault representation is more flexible and powerful, leading to the recent development of multiple-model FDI (MM–FDI) schemes.

For example, eight fault models were established for the air-intake system of a turbo-charged engine [22]; then structured hypothesis tests were used to detect the occurrences of faults. The multiple-model adaptive estimation (MMAE) algorithm, which runs parallel state estimators and calculates the probability of each model by Bayes’ rule, has been applied to the flight control

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system [33]. To improve the performance of multiple-model FDI (MM–FDI) schemes, the interacting multiple-model (IMM) algorithm was investigated [23] and applied to the satellite’s attitude control system [24] as well as the aircraft lateral motion control system [25].

The aforementioned MM–FDI schemes enumerate all detectable and isolatable faults in the model sets. If an unexpected fault, i.e. a fault without a corresponding model in the model set, has occurred, the results of the MM–FDI schemes become unpredictable. Therefore, a large model set is required in order to detect and isolate as many faults as possible. Unfortunately, it is difficult, if not impossible, to design an exhaustive model set that contains every possible fault. Take the partial actuator fault [26] for example. The associated fault model incorporates a fixed multiplicative “effective factor” in the actuator’s output, representing the reduction of the actuator’s gain. Since the effective factor can be any number between 0 and 1, it is impossible to include all partial fault models in the model set. In fact, we are restricted to work on a finite model set, and we will show in Section 3 that expanding the model set results in a considerable increase of the computational load. Even though the computational load is affordable, a large model set is not recommended because some models may become indistinguishable from the input–output point of view, and then the MM–FDI schemes are unable to select the fittest model from the model set with “sufficient confidence”. In short, MM–FDI schemes face a dilemma of avoiding unexpected faults by using a fine-grained model set while maintaining a tractable algorithm by limiting the size of the model set.

To tackle the model set design problem, Ru and Li [26] proposed the IMML algorithm that uses the IMM algorithm for estimating system state and the expectation-maximization (EM) algorithm for updating model parameters. Therefore the fault models are self-adaptive, relieving the need for a large model set. However only (multiple) abrupt total and partial faults were considered in [26].

In this paper, we propose a hierarchical multiple-model FDI (HMM-FDI) scheme as a solution to the model set design problem and apply it to detect and isolate actuator faults of robot manipulators. The ultimate goal of the proposed FDI scheme is to find out faulty joints in an early stage such that fault tolerant strategies can be launched in time to guarantee safe operation of the robotic system. In other words, any faulty joints must be indicated before the robotic system significantly deviates from its nominal performance, no matter what kinds of faults have taken place. To achieve this goal, the proposed HMM-FDI scheme works in stages. At each stage, the model set is refined such that only a small number of models are required. Therefore the HMM-FDI scheme avoids the need for enumerating all possible faults in the model set, while is endowed with the ability to detect and isolate various types of unexpected actuator faults, including abrupt faults, incipient faults, and simultaneous faults in a computationally efficient way. The relation between the fault detection stage of the HMM-FDI scheme and the likelihood ratio test is explicitly revealed and theoretical upper bounds of the false alarm and missed detection probabilities are evaluated. Then experiments are conducted to verify the performance and efficiency of the HMM-FDI scheme.

The remainder of this paper is organized as follows: Section 2 introduces the dynamic and kinematic models of the robot manipulator. Section 3 illustrates the notions of the MM–FDI methods and the related techniques. The HMM-FDI scheme is proposed in Section 4 while experimental results are presented in Section 5. Section 6 concludes this paper.

2. Dynamic and kinematic models of the manipulator

The dynamic equation of an \( n \)-joint manipulator is given as follows [34]:

\[
\mathbf{M}(\mathbf{q}(t))\ddot{\mathbf{q}}(t) + \mathbf{C}(\mathbf{q}(t), \dot{\mathbf{q}}(t))\dot{\mathbf{q}}(t) + \mathbf{G}(\mathbf{q}(t)) + \mathbf{F}(\mathbf{q}(t)) = \tau(t)
\]

(1)

where \( \mathbf{q}(t), \dot{\mathbf{q}}(t), \ddot{\mathbf{q}}(t) \in \mathbb{R}^n \) are vectors of joint positions, velocities, and accelerations at time \( t \), respectively. \( \mathbf{M}(\mathbf{q}(t)), \mathbf{C}(\mathbf{q}(t), \dot{\mathbf{q}}(t)), \mathbf{G}(\mathbf{q}(t)) \in \mathbb{R}^{n \times n} \) are the inertia matrix, and Coriolis and centrifugal matrix respectively. \( \mathbf{F}(\mathbf{q}(t)), \tau(t) \in \mathbb{R}^n \) denote the gravitational torque vector, friction vector, and control torque vector, respectively. For clarity, we will drop the notational dependence of all variables on \( t \) as long as it leads to no confusion.

Define the state vector of the manipulator as \( \mathbf{x} = [\mathbf{q}^T, \dot{\mathbf{q}}^T]^T \).

Because the proposed HMM-FDI scheme will be derived in the discrete-time domain, we apply the Euler’s method to convert (1) to its discrete-time counterpart and obtain the following state space representation:

\[
\mathbf{x}_{k+1} = \mathbf{x}_k + h \left[ \mathbf{f}(\mathbf{x}_k, \tau_k) \right] + \mathbf{w}_k
\]

(2)

where \( \mathbf{f}(\mathbf{x}_k, \tau_k) = \mathbf{M}^{-1}(\mathbf{q}_k) \tau_k - \mathbf{C}(\mathbf{q}_k, \dot{\mathbf{q}}_k) \dot{\mathbf{q}}_k - \mathbf{G}(\mathbf{q}_k) - \mathbf{F}(\mathbf{q}_k) \) is the sampling time, and the subscript \( k \) denotes the \( k \)-th sample.

\( \mathbf{w}_k \) is the process noise representing the model uncertainties and the approximation error due to the Euler’s method.

We assume that only the joint positions are measurable. Thus the output equation of the manipulator is:

\[
\mathbf{y}_k = \mathbf{C} \mathbf{x}_k + \mathbf{v}_k
\]

(3)

where \( \mathbf{C} = [1, 0, \ldots, 0] \) and \( \mathbf{v}_k \) is the measurement noise which is assumed to be Gaussian distributed white noise with zero mean and covariance matrix \( \mathbf{R} \).

In the context of the HMM-FDI scheme, the dynamic model consists of (2) and (3) along with the assumption that \( \mathbf{w}_k \) is Gaussian distributed noise with zero mean and covariance matrix \( \mathbf{Q}^w \). In addition, we assume that components of \( \mathbf{w}_k \) are mutually uncorrelated, i.e. \( \mathbf{Q}^w \) is a diagonal matrix. Note that we allow the covariance matrix to be time-varying.

Remark 1. It should be noted that the actual distribution of \( \mathbf{w}_k \) may not be Gaussian; nevertheless the dynamic model assumes that \( \mathbf{w}_k \) is Gaussian distributed and mutually uncorrelated, and treats the covariance matrix \( \mathbf{Q}^w \) as a tunable parameter of the model, not a physical quantity of the robot. By tuning \( \mathbf{Q}^w \) we change the “accuracy” of the dynamic model. If \( \mathbf{Q}^w \) is set to an inappropriate value, then the dynamic model behaves poorly in predicting the motion of the manipulator; however, it is our intention to reduce the “relative accuracy” of one model w.r.t. the others for the purpose of fault detection and isolation. See Section 4 for more details.

On the other hand, we can predict the motion of the manipulator through the kinematic relations of joints. By kinematic relation we mean that the joint velocity is the first derivative of the joint position. Approximating the kinematic relation by the Euler’s method yields

\[
\dot{\mathbf{q}}_{k+1} = \mathbf{q}_{k+1} + \mathbf{h} \dot{\mathbf{q}}_k + \dot{\mathbf{x}}^\epsilon_k
\]

(4)

where \( \dot{\mathbf{x}}^\epsilon_k \) is the approximation error due to the Euler’s method. On the other hand, if the differentiation relation is approximated by the backward difference equation, then we have

\[
\dot{\mathbf{q}}_{k+1} = \mathbf{q}_{k+1} - \mathbf{q}_k + \mathbf{h} \dot{\mathbf{x}}^\epsilon_k
\]

(5)

where \( \dot{\mathbf{x}}^\epsilon_k \) is the approximation error due to the backward difference equation. Combining (4) and (5) yields the following equation:

\[
\mathbf{x}_{k+1} = \mathbf{A}^\epsilon \mathbf{x}_k + \mathbf{C}^\epsilon \dot{\mathbf{x}}^\epsilon_k
\]

(6)
where $A^K = \begin{bmatrix} 1 & 0 \\ 0 & I \end{bmatrix}$, $G^K = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$, and $\xi_k = e_k$. In the context of the HMM-FDI scheme, the *kinematic model* consists of (6) and (3) along with the assumption that $\xi_k$ is Gaussian distributed with zero mean and covariance matrix $Q^K$. We also assume that the components of $\xi_k$ are mutually uncorrelated, i.e., $Q_i^K$ is a diagonal matrix. Here $Q_i^K$ is also regarded as a tunable parameter of the kinematic model (c.f. Remark 1). In addition, we assume that $v_\tau, w_\tau$, and $\xi_k$ are independent.

Furthermore, we can describe the motion of the $i$th joint by either (7) (dynamical equation) or (8) (kinematic equation) below and obtain a set of models with arbitrary combinations of (7) and (8) for the $n$ joints.

$$
\begin{align*}
q_i(k+1) &= q_i(k) + h \left[ \dot{q}_i(k) \right] + w_{i,1}^p + e_{i,1}^p, \\
q_i(k+1) &= q_i(k) + h \left[ \dot{q}_i(k) \right] + q_i(k) + 0 + \frac{\xi_i^p}{h} + e_i^p + e_i^v
\end{align*}
$$

(7) (8)

where the symbol $i$ in the first part of the subscript denotes the $i$th element of a vector.

To facilitate the presentation, we introduce the notation $K_1, K_2, \ldots$ to denote a model that includes (8) for those joints inside the parentheses, and (7) for all the other joints. For example, if $n = 3$, then $K_1, K_2, K_3$ denotes the following model:

$$
\begin{align*}
q_1(k+1) &= q_1(k) + h \left[ \dot{q}_1(k) \right] + w_{1,1}^p + e_{1,1}^p, \\
q_2(k+1) &= q_2(k) + h \left[ \dot{q}_2(k) \right] + q_2(k) + 0 + \frac{\xi_2^p}{h} + e_2^p + e_2^v, \\
q_3(k+1) &= q_3(k) + h \left[ \dot{q}_3(k) \right] + q_3(k) + 0 + \frac{\xi_3^p}{h} + e_3^p + e_3^v.
\end{align*}
$$

(9)

In particular, (6) and (2) are denoted by $K(1, 2, \ldots, n)$ and $K(0)$ respectively.

3. Multiple-model FDI schemes

MM–FDI schemes use one model for one particular fault. Then all fault models as well as the normal model (2), i.e. the model describing the normal operation of the robot, are contained in a model set. Whenever a fault has taken place, the model that best fits the current behavior of the robot switches from the normal model to the associated fault model. If we can detect the switch of models and identify the associated fault model, the FDI problem is solved.

We say that the robotic system is currently in mode $i$ if the $i$th model is the fittest one. Suppose that we have defined an *exclusive and exhaustive* model set which consists of $J$ models. Namely, the robotic system is in one and exactly one of the $J$ modes at any time. Then we can estimate the current mode of the robotic system by evaluating the probabilities of the modes.

Let $P(M_i)$ be the probability of the event $M_i$, which denotes that the robotic system is in mode $i$ at step $k$ for $i = 1, 2, \ldots, J$ and all $k$. We assume that $M_i$ forms a Markov chain, i.e.

$$
P(M_i^{k+1} | M_i^{-k-1}, M_i^{k-j}, \ldots, M_i^{0}) = P(M_i^{k+1} | M_i^{k-j}) = \pi_i^{k-j},
$$

(10)

where $i_j$ is the mode transition probability satisfying $\sum_{j=1}^{J} \pi_i^{k-j} = 1$ for all $i$. The posterior mode probability conditioning on all measurements up to step $k$ is

$$
s_k^i = P(M_i | y_1, y_2, \ldots, y_k), \quad i = 1, 2, \ldots, J \text{ and } k.
$$

If $s_k^i = \max \{s_k^1, \ldots, s_k^J\}$, then we conclude that the robotic system is in mode $j$ at step $k$. Furthermore, if mode $j$ is associated with a particular fault, then we infer that the corresponding fault has taken place. Therefore the FDI problem is equivalent to evaluating the posterior mode probabilities.

Evaluation of the posterior mode probabilities requires state estimation in the multiple-model setting. Related techniques adopted in this paper are introduced in the following subsections.

3.1. Nonlinear state estimation

Without loss of generality, we can assume that the $i$th model in the model set has the following state space representation:

$$
\begin{align*}
\dot{x}_{i,k+1} &= \phi_i(x_{i,k}, \tau_k) + w_{i,k} \\
y_k &= C_i x_k + v_k
\end{align*}
$$

where $\phi_i$ is a nonlinear function of the state $x_{i,k}$ and the control torque $\tau_k$, $w_{i,k}$ and $v_k$ are process noise and measurement noise respectively which are assumed to be Gaussian distributed with zero means and covariance matrices $Q_i$ and $R$.

In this paper, we use unscented Kalman filter (UKF) for nonlinear state estimation because in general, UKF achieves a better performance than the well-known extended Kalman filter (EKF) with similar computational complexity [36]. For completeness, the UKF algorithm is presented in Algorithm 1, where the following notations are used:

$$
\begin{align*}
\hat{x}_{i,k} &= E [x_{i,k} | y_1, \ldots, y_k], \\
P_{i,k} &= \text{var} [x_{i,k} | y_1, y_2, \ldots, y_k], \\
L_k &= p (y_k | y_1, y_2, \ldots, y_{k-1})
\end{align*}
$$

Algorithm 1: UKF algorithm

$$
\begin{align*}
&(x_{i,k+1}^{j} | x_{i,k+1}^{j-1}) = \\
&\text{UKF} (\hat{x}_{i,k}, P_{i,k}^{j} | y_{k+1:k+1}, \tau_k, \phi_i, \phi_j, \phi_{i,j, C_i, Q_i, R}).
\end{align*}
$$

$$
\begin{align*}
&\dot{x}_i = \frac{x_{i,k} \pm \sqrt{N}}{2} + \epsilon_{k,i} \phi_i \left( x_i, \tau_k \right), \\
&w_i = \frac{1}{2(N + \epsilon_{i,k})}, \\
&L_k = \text{var} [x_{i,k} | y_1, y_2, \ldots, y_{k-1}]
\end{align*}
$$

(continued on next page)
Comprehensive discussions about UKF can be found in [37].

3.2. Multiple-model state estimation

Given that the robotic system is in mode $j$, we can apply Algorithm 1 to estimate the state. Unfortunately, the mode of the robotic system is unknown; therefore, the generalized pseudo-Bayesian method of order 2 (GBP-2) [38] is applied to estimate the state and the posterior mode probabilities in the multiple-model setting. Suppose that there are $J$ models in the model set and define

$$\hat{x}_{k+1|i}^j = E\left[x_k|M_{k-1}^i, M_k^j, y_1, \ldots, y_k\right],$$

$$P_{k+1|i}^j = \text{var}\left(x_k|M_{k-1}^i, M_k^j, y_1, \ldots, y_k\right),$$

$$L_{k+1}^j = \frac{1}{(2\pi)^{2N/2}} \text{det} S_{k+1}^j,$$

$$\exp\left\{-\frac{1}{2} (y_{k+1} - \mu_{k+1}^j)^T \left(S_{k+1}^{-1} J^i \mu_{k+1}^j\right) \right\}$$

$E[\cdot]$ and var(.) denote the expected value and variance respectively. $P(\cdot)$ is the probability density function (PDF).

At each time step, the GBP-2 algorithm runs UKF $J^2$ times and generates $J^2$ state estimates $\hat{x}_{k+1|i}^j, i, j = 1, 2, \ldots, J$. $\hat{x}_{k+1|i}^j$ denotes the estimated state under the condition that the robotic system switches from mode $i$ to mode $j$ at step $k$. In the meanwhile, the GBP-2 algorithm also evaluates the posterior mode probabilities (10). Then these $J^2$ state estimates are merged together according to the posterior mode probabilities, leaving $J$ estimated states at the end of each step. The GBP-2 algorithm is presented in Algorithm 2.

4. HMM-FDI scheme

As we have mentioned in Section 1, model set design is the most challenging part of the MM–FDI approaches. To solve this problem, we propose to perform FDI in stages with mixture models of dynamic equations (7) and kinematic equations (8), resulting in a hierarchical multiple-model FDI (HMM–FDI) scheme. Unlike conventional MM–FDI approaches which detect and isolate faults in one step with a large model set, the proposed HMM–FDI scheme detects (multiple) faults as the first step, and then isolates the faulty joints as the next step. If the joints fail successively, the HMM–FDI scheme keeps refining its model set in the isolation stage until all faults have been isolated, or the robot is forced to give up its task. The flowchart of the HMM–FDI scheme is shown in Fig. 1.

4.1. Fault detection

In the fault detection stage, the model set consists of only two models: the dynamic model (2) and the kinematic model (6). Roughly speaking, we tune the model parameters $Q_k^j$ and $K_k^j$ such that the dynamic model is more accurate than the kinematic model under normal operation. In other words, we increase $Q_k^j$ or decrease $Q_k^j$ such that the covariance of the estimated state associated with the kinematic model becomes larger than that of the dynamic model. Thus the GBP-2 algorithm favors the dynamic model and assigns a higher posterior mode probability to it, indicating that the robotic system is normal.

In the event of actuator faults, the faulty joints no longer satisfy the dynamic model; however the kinematic model remains a good approximation to the motion of all joints because it has nothing to do with actuators’ torques. Thus the posterior mode probability of the kinematic model increases. If it exceeds a predefined threshold
To, we assert the occurrence of faults. Note that 0 < To < 1; hence To represents the least confidence level we must have when we claim that the robotic system is faulty.

4.2. Fault isolation

In the fault isolation stage, we focus on finding out the faulty joints instead of recognizing the types of faults, i.e., whether the joint is locked or suffers from partial loss of the output gain does not matter as long as we know that it has failed. For easy illustration, we temporarily assume that multiple faults take place successively, not simultaneously. Under this assumption, the proposed model set for fault isolation is \( \{K(1), K(2), \ldots, K(n)\} \) (see Section 2 for an explanation of the notations). Suppose that the jth joint has failed. Because all models but \( K(j) \) incorporate the dynamic equation \( (7) \) for the jth joint, \( K(j) \) is least susceptible to the fault of the jth joint. Therefore \( K(j) \) will be assigned the highest posterior mode probability. If the posterior mode probability of \( K(j) \) exceeds a predefined threshold \( T_j \), we assert that the jth joint has failed. Since \( 0 < T_j < 1 \), \( T_j \) represents the least confidence level we must have to isolate the faulty joint.

Once the faulty joint has been isolated, the robotic system may continue its operation, reconfigure its mission, or make an emergency stop. The decision is made by the control system, which is beyond the scope of this paper. However, the FDI scheme must be ready for detecting and isolating succeeding faults as long as the robotic system remains operational. To do this, the HMM-FDI scheme refines its model set as \( \{K(1), K(1, j), K(2, j), \ldots, K(n, j)\} \) after the fault of the jth joint has been isolated. The new model set contains \( n \) models and all of them have the kinematic equation \( (8) \) for the jth joint. \( n-1 \) models include one more kinematic equation for one of the remaining \( n-1 \) joints. Note that \( K(j) \) is the model with the highest posterior mode probability in the previous stage. If no more faults take place, \( K(j) \) will be selected. On the other hand, if the mth joint has failed, \( m \neq j \), then by the same arguments we infer that \( K(j, m) \) will be assigned the highest posterior mode probability. If the posterior mode probability exceeds the threshold \( T_j \), the mth joint is isolated. The process continues until the robotic system stops or all joints have been isolated.

Now we relax the assumption of no simultaneous faults. If any two joints may fail at the same time, the proposed model set is \( \{K(i), K(i, j)|i, j = 1, \ldots, n\} \), i.e. the model set contains \( C^2 \) models that include kinematic equations for any one or any two joints. If the robot motion controller robustly alleviates the dynamic couplings of the joints [39], then the fault of one joint has minor effects on the other joints. Therefore \( K(j) \) gets the highest posterior mode probability when a single fault occurs on the jth joint. This is because \( K(j) \) includes the kinematic equation for the faulty joint and the more accurate dynamic equations for the other normal joints. Similarly, \( K(i, j) \) gets the highest posterior mode probability when faults occur on the jth and jth joints simultaneously. Consequently, both single faults and simultaneous faults can be isolated. Then the model set is refined again. The refining procedure is similar: using the kinematic equations for all faulty joints, and one or two of the remaining normal joints.

Therefore we have established the procedure for FDI. Only two models are used for fault detection and a small number of models (depending on how many simultaneous faults are considered) are required for fault isolation. The refinement of the model set depends on the previously isolated faulty joints, and thus the evolution of the model set forms a hierarchical structure. Besides, no particular fault information (e.g. locked joints or partial loss of output gains) is assumed. Hence the HMM-FDI scheme is able to detect and isolate various types of unexpected actuator faults. Furthermore, the implementation of the HMM-FDI scheme can be computationally efficient in comparison with conventional MM-FDI approaches due to the reduced-sized model set. Experiments in Section 5 will verify the ability of the HMM-FDI scheme in immediate detection and isolation of a variety of actuator faults.

4.3. HMM-FDI scheme vs. likelihood ratio test

To analyze the performance of the HMM-FDI scheme, we relate its fault detection stage to the well-known likelihood ratio test and evaluate the probabilities of false alarms and missed detections. Recall that the likelihood function \( L_s^{ij} \) defined in (11) is the PDF of \( y_i \) conditioning on \( y_1, \ldots, y_{k-1} \) as well as the mode transition from i to j at step k. Since only two models are involved in the fault detection stage, we use the superscript D and K to denote that the variable is evaluated based on the dynamic model and the kinematic model respectively.

According to Algorithms 1 and 2, \( L_s^{ij} \) is a Gaussian function with mean \( \mu_s^{ij} \) and covariance matrix \( S_s^{ij} \). \( i, j = D, K \). However, the true likelihood function, i.e. the PDF of \( y_i \) conditioning on \( y_1, \ldots, y_{k-1} \), is unknown and susceptible to faults. In the fault detection stage, let \( L_s^{ij} \) and \( L_s^{ij} \) denote the true likelihood functions under normal and faulty operations, respectively, i.e.

\[
L_s^{ij} = p(y_i|y_1, \ldots, y_{k-1}, \text{ the system is normal at step } k)
\]

\[
L_s^{ij} = p(y_i|y_1, \ldots, y_{k-1}, \text{ the system is faulty at step } k)
\]

\( L_s^{ij} \) and \( L_s^{ij} \) are unknown and may not be Gaussian. Their means and covariance matrices are denoted by \( \mu_s^N \) and \( S_s^N \), respectively and are unknown either. We explicitly distinguish \( L_s^{ij} \) and \( L_s^{ij} \) to emphasize the difference between models and the physical system, especially when the accuracy of the models are reduced purposely.

If we choose

\[
Q_k = \begin{bmatrix} Q_{11,k} & 0 \\ 0 & Q_{22,k} \end{bmatrix}, \quad i = D, K, \quad \text{and all } k
\]

(12)

where \( Q_{11,k}, Q_{22,k} \in \mathbb{R}^{n \times n} \) are diagonal matrices, then direct computation based on the UKF algorithm yields \( \mu_s^{i,k} = \mu_s^{i,k} \leq \mu_s^{i,k} \) and \( S_s^{i,k} = S_s^{i,k} \leq S_s^{i,k} \) for \( i = D, K \), and all \( y_i \). Furthermore, if we choose the mode transition probabilities defined in (9) to be \( \pi_0 = \pi^K = \pi^D \), then the GBP-2 algorithm leads to the following fault detection criterion:

The fault is detected at step \( k \) if \( s_k \geq T_0 \) if \( k \) if \( u_k \geq r \) where \( u_k = \rho_k - l_k \), \( l_k = \log l_k \), \( r = \log \frac{\pi^K}{\pi^D} \).
where $1_S$ is the indicator function of the set $S$, i.e., $1_S(y_k) = 1$ if $y_k \in S$ and $1_S(y_k) = 0$ if $y_k \notin S$. $E[\cdot]$ and $\text{var}(\cdot)$ denote the mean and variance w.r.t. $L_k^i$. To further simplify the notations, we use $E_i^k$ and $\psi_i^k$ for $E[i^k]$ and $\text{var}(l_i^k)$, $i = N, F$, respectively. Then the following theorem gives theoretical upper bounds of the false alarm and missed detection probabilities.

**Theorem 1.** If (12) holds, and $\pi^0 > T_D > 0.5$, then

$$p_{FA}^k \leq \frac{\tilde{P}_{FA}^k}{\lambda_i^k} E_i^N < r - \rho_{k-1}, 1, \quad E_i^N \geq r - \rho_{k-1},$$

$$p_{MD}^k \leq \frac{1}{\lambda_i^k} E_i^F > r - \rho_{k-1}, 1, \quad E_i^F \leq r - \rho_{k-1},$$

where

$$\tilde{P}_{FA}^k = 1 - \frac{1}{2r^2} \left( (\rho_{k-1} + E_i^N - r)^2 + V_i^N + r^2 \right) - \sqrt{\left[ (\rho_{k-1} + E_i^N - r)^2 + V_i^N + r^2 \right]} \right] < 1 \quad (13)$$

$$\tilde{P}_{MD}^k = 1 - \frac{1}{2r^2} \left( (\rho_{k-1} + E_i^F - r)^2 + V_i^F + r^2 \right) - \sqrt{\left[ (\rho_{k-1} + E_i^F - r)^2 + V_i^F + r^2 \right]} \right] < 1. \quad (14)$$

**Proof.** We derive (13) in detail and (14) can be established by the same procedure.

Define $m_k = \{y_k \in R^{|l_k|} | v_k(y_k) < 0\}$. Since $\pi^0 > T_D > 0.5$, $r$ is positive. Therefore $m_k \subseteq \{y_k \in \Omega_k | \int_{\Omega_k} v_k L_k^i dy_k = E_i^N [1_{m_k} v_k] < 0, \text{ and } \int_{\Omega_k \setminus m_k} v_k L_k^i dy_k \geq 0\}$. Besides, $E_i^N [1_{m_k}] = E_i^N [1_{\Omega_k}]$. Then

$$E_i^N [v_k] = \int_{\Omega_k} v_k L_k^i dy_k + \int_{\Omega_k \setminus m_k} v_k L_k^i dy_k + \int_{m_k} v_k L_k^i dy_k \geq E_i^N [1_{m_k}] + r (1 - E_i^N [1_{\Omega_k}]). \quad (15)$$

Apply Cauchy–Schwarz inequality to $E_i^N [1_{m_k} v_k]$ and rearrange (15): then we obtain

$$\psi \left( \sqrt{E_i^N [1_{m_k}]} \right) \leq r E_i^N [1_{m_k}] + \sqrt{E_i^N [v_k^2]} E_i^N [1_{m_k}] + (E_i^N [v_k] - r) \geq 0.$$

Note that $\psi$ is a convex parabolic function of $\sqrt{E_i^N [1_{m_k}]}$. It is easy to show that $\psi$ has two real roots and at least one of them is negative. Therefore if $E_i^N [1_{\Omega_k}] \geq r$, both roots are negative, implying that $\psi \geq 0$ for all $0 \leq E_i^N [1_{m_k}] \leq 1$. On the other hand, if $E_i^N [1_{\Omega_k}] < r$, then we can show that $\psi$ has one positive root which is always less than 1. Under these circumstances, $\psi \geq 0$ implies

$$0 \leq \frac{1}{2r} \left( -\sqrt{E_i^N [v_k^2]} + \sqrt{E_i^N [v_k^2] - 4r (E_i^N [v_k] - r)} \right) \leq \sqrt{E_i^N [1_{m_k}]} \leq 1. \quad (16)$$

Since $P_{FA}^k = 1 - E_i^N [1_{m_k}]$, $E_i^N [v_k] \geq r$ implies $P_{FA}^k \leq 1$. In this case, we say that the upper bound is trivial because it provides little information about the false alarm probability. On the other hand, if $E_i^N [v_k] < r$, then (16) holds, implying $P_{FA}^k \leq \frac{1}{\lambda_i^k} < 1$. \hspace{1cm} □

Note that $\tilde{P}_{FA}^k$ is a function of $E_i^N$ and $V_i^N$. It is straightforward to show that the partial derivatives of $\tilde{P}_{FA}^k$ w.r.t. both $E_i^N$ and $V_i^N$ are always nonnegative, i.e., $\tilde{P}_{FA}^k$ is a non-decreasing function of $E_i^N$ and $V_i^N$. Hence if $E_i^N < \tilde{E}_i^N$ and $V_i^N < \tilde{V}_i^N$, then $\tilde{P}_{FA}^k (E_i^N, V_i^N) \leq \tilde{P}_{FA}^k (\tilde{E}_i^N, \tilde{V}_i^N)$. An upper bound of $E_i^k$ can be evaluated directly from its definition as follows:

$$E_i^k \leq \frac{1}{2} \left( n \log \frac{\lambda_{i,k}^D}{\lambda_{i,k}^L} + \frac{\text{tr} S_i^k + \| \Delta \mu_k^D \|^2}{\lambda_{i,k}^L} - \frac{\text{tr} S_i^k + \| \Delta \mu_k^L \|^2}{\lambda_{i,k}^L} \right),$$

$$i = N, F. \quad (17)$$

where $\lambda_{i,k}^L$ and $\lambda_{i,k}^D$ are the minimum and maximum eigenvalues of $S_i^k$ respectively; $\Delta \mu_i^D = \nu_i^D - \mu_i^L$ for $i = D, K$ and $j = N, F$. $\| \cdot \|$ is the Euclidean norm and $\text{tr} \cdot$ is the trace of a matrix. Furthermore, if $\mu_i^D$ and $\mu_i^L$ are Gaussian functions, then an upper bound of $V_i^k$ can be found as follows [40]:

$$V_i^k \leq \left( \text{tr} S_i^k \right) \left( \frac{1}{\lambda_{i,k}^D} + \frac{1}{\lambda_{i,k}^L} \right)^2 + \text{tr} S_i^k \left( \frac{\| \Delta \mu_k^D \|^2}{\lambda_{i,k}^L} + \frac{\| \Delta \mu_k^L \|^2}{\lambda_{i,k}^D} \right)^2, \quad i = N, F. \quad (18)$$

Substitute (17) and (18) into (13) and (14), and we can find the theoretical upper bounds of the false alarm and missed detection probabilities in terms of parameters of the models, i.e., $\lambda_{i,k}^L$, $\lambda_{i,k}^D$ and $\mu_i^L$, $\mu_i^D$, $i = D, K$, and parameters of the physical system, i.e., $\text{tr} S_i^k$, $\| \cdot \|$, $j = N, F$.

**Remark 2.** (18) holds under the assumption that $l_i^k$ is a Gaussian function, $i = N, F$. However it is also possible to find an upper bound of $V_i^k$ w.r.t. any other distributions [40]. We made the Gaussian assumption because it facilitates the derivation of the upper bound in terms of $\lambda_{i,k}^L$ and $\lambda_{i,k}^D$, $i = D, K$.

5. Experiments

5.1. Experimental setting

A two-joint manipulator was set up for experimental verifications. The schema and the photograph of the manipulator are shown in the left and right sides of Fig. 2 respectively. Each link is driven by a DC motor with an optical encoder mounted on the shaft. A motion controller and the HMM-FDI scheme are implemented on a 32-bit floating point DSP chip (TMS320F28335). The sampling time is 0.01 s. The dynamics of the DC motors and the manipulator can be lumped together as follows [34].

$$\begin{bmatrix} 1_1 + \theta_1 + 2\theta_1 \cos q_2 & \theta_2 + \theta_1 \cos q_2 \\ \theta_1 + \theta_0 \cos q_2 & \theta_1 \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} + \begin{bmatrix} -\theta_1 \dot{q}_2 \sin q_2 & -\theta_3 (\dot{q}_1 + \dot{q}_2) \sin q_3 \\ \theta_3 \dot{q}_1 \sin q_2 & 0 \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} + \begin{bmatrix} \theta_0 \cos q_1 + \frac{g}{l_1} \theta_1 \cos (q_1 + q_2) \\ \frac{g}{l_1} \theta_0 \cos (q_1 + q_2) \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix} + \begin{bmatrix} \theta_0 \dot{q}_1 + \theta_0 \sin q_1 \\ \theta_0 \dot{q}_1 + \theta_1 \sin q_1 \end{bmatrix} = \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \end{bmatrix}$$

where the control inputs $v_1$ and $v_2$ are armature voltages of the DC motors within the range of ±24 V. $\dot{q}_i$, $i = 1, 2, \ldots, 11$, are model
A closed-loop system consists of both a controller and a manipulator. The controller is implemented as a computed torque plus PID motion controller. The parameters of the manipulator are shown in Table 1. The model parameters and their nominal values are given in Table 2.

The following values are used in the experiments:
\[ K_P = \text{diag}(800, 500), \quad K_v = \text{diag}(30, 15), \quad K_i = \text{diag}(1.411, 0.3). \]

In the experiments, the desired trajectory in the joint space is
\[ q_{1d}(t) = -\frac{\pi}{8} + \frac{\pi}{4}(1 - e^{-2t^3}) + \frac{\pi}{9}(1 - e^{-2t})\sin(4t) \]
\[ q_{2d}(t) = \frac{\pi}{3}(1 - e^{-2t^3}) + \frac{\pi}{6}(1 - e^{-2t^3})\sin(3t). \]

Remark 3. If a closed-loop system consists of both a controller and an FDI scheme, the FDI scheme is inevitably affected by the controller. A robust controller reduces the fluctuation of the system state caused by model uncertainties, external disturbances, and faults as well, making the closed-loop system less sensitive to faults. Moreover, some "soft faults", i.e., faults that are not detrimental to the system stability and performance, may turn out to be invisible from the input–output data due to the robustness of the controller. However, integrated design of the controller and the FDI scheme remains an open question and is beyond the scope of this paper. To carry out experiments, we implement the motion controller first and then manually tune the parameters of the HMM-FDI scheme. Despite the non-optimal combination of the controller and the FDI scheme, experimental results demonstrate that tracking performance of the control system just deteriorates slightly before the fault is detected and isolated. Hence we consider the performance of the HMM-FDI scheme satisfactory as far as the manipulator’s safe operation is concerned.

In the fault detection stage, the model set consists of the dynamic model (2) and the kinematic model (6). In the fault isolation stage, the model set is chosen to be \( \{K(1), K(2), K(1, 2)\} \) such that simultaneous faults can be isolated. Since all combinations of faulty joints are included in the last model set, there is no need to refine it during the isolation stage. The following parameters of the HMM-FDI scheme are chosen: \[ R = 0.001^2I, \quad Q_{1, k} = 0.0026^2I, \quad Q_{2, k} = 0.0023^2I, \quad Q_{22, k} = 0.003^2I \] for all \( k, \pi^{B, D} = \pi^{X, K} = 0.999, \) and \( \tau_D = 0.7, \) and \( \tau_I = 0.75. \) Five types of faults in Table 3 are considered. Note that Type 5 fault is an incipient fault indicating a gradual
### Table 3

<table>
<thead>
<tr>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type 1</td>
<td>The 1st joint is locked.</td>
</tr>
<tr>
<td>Type 2</td>
<td>Both joints are locked simultaneously.</td>
</tr>
<tr>
<td>Type 3</td>
<td>The 1st joint is locked first; then the 2nd joint is locked.</td>
</tr>
<tr>
<td>Type 4</td>
<td>The 1st joint loses 60% of its output torque.</td>
</tr>
<tr>
<td>Type 5</td>
<td>The output torque of the 2nd joint gradually decays to zero with time constant 0.15 s.</td>
</tr>
</tbody>
</table>

![Fig. 3](image1.png)

**Fig. 3.** The 1st joint is locked at \( t = 10 \) s. (a),(d) Joint positions: desired trajectory (solid line); real trajectory (dotted line). (b),(e) Joint velocities: desired velocities (solid line); estimated velocities (dotted line). (c),(f) Armature voltages of both joints.

![Fig. 4](image2.png)

**Fig. 4.** (a) The fault occurs suddenly at \( t = 10 \) s. (b) Posterior mode probabilities of the dynamic model (solid line) and the kinematic model (dotted line). The fault is detected at \( t = 10.04 \) s. (c) Posterior mode probabilities of \( K(1) \) (solid line), \( K(2) \) (dashed line) and \( K(1,2) \) (dash–dot line). The faulty joint is isolated at \( t = 10.08 \) s.

loss of the actuator’s torque. All the others are abrupt faults. Type 2 is simultaneous faults, Type 3 represents successive multiple faults, and all the others are single faults.

Note that it is difficult for the conventional MM–FDI methods to model Type 4 and Type 5 faults since both the percentage of loss and the time constant of the decay are unknown and may vary substantially. However, the HMM-FDI scheme can handle these faults easily. Even if the models for these five types of faults are established, the computational load is very demanding. Because the model set contains at least six models (five fault models and one normal model), the conventional MM–FDI methods have to run at least 30 UKFs at each sampling time. On the other hand, the
HMM-FDI scheme uses at most three models in the model set and runs at most 9 UKFs at each sampling time. Therefore the HMM-FDI scheme not only extends the applicability of the conventional MM–FDI methods, but also significantly improves the computational efficiency. Besides, the HMM-FDI scheme does not incorporate any particular fault information in the models. Hence these five types of faults are all unexpected to the HMM-FDI scheme. However, the HMM-FDI scheme is not restricted to detecting and isolating only these five types of faults. More unexpected faults can be detected and isolated with the HMM-FDI scheme unaltered.

5.2. Experimental results

- The 1st joint is locked (Type 1)

Suppose that at \( t = 10 \) s, the first joint is suddenly locked. The results are shown in Figs. 3 and 4. Fig. 3 illustrates the positions, velocities, and armature voltages of both joints. It can be seen that the 1st joint is locked at \( t = 10 \) s while the 2nd joint operates normally. Since the dynamics of both joints are coupled, the 2nd joint is affected by the fault of the 1st joint. However, due to the robustness of the controller, the tracking performance of the 2nd joint just degrades slightly in the event of the locked 1st joint. It can also be seen from Fig. 3(b), (e) that the estimated velocities are close to the desired velocities, implying that the state estimators included in the HMM-FDI scheme work well.

The posterior mode probabilities for fault detection and fault isolation are shown in Fig. 4. During normal operation, the posterior mode probability of the dynamic model is significantly higher than that of the kinematic model. Therefore false alarms caused by model uncertainties and external disturbances are avoided. After the fault occurs, the posterior mode probability of the kinematic model dominates. It takes 0.04 s to detect the fault.
Once the fault has been detected, the model set changes and the fault isolation process starts. The posterior mode probability of $K(1)$ becomes highest. The time between the occurrence of the fault and the time of the fault being isolated is 0.08 s.

- **Both joints are locked simultaneously (Type 2)**

Suppose that both joints are suddenly locked at $t = 7.2$ s. The positions, velocities, and armature voltages of both joints are shown in Fig. 5. Fig. 6 illustrates the posterior mode probabilities for fault detection and fault isolation. The HMM-FDI scheme detects and isolates the fault within 0.03 s and 0.08 s respectively. At this moment, the model $K(1)$ has the highest probability since the 1st joint is locked. Then the 2nd joint is locked at $t = 13.5$ s and the model with highest probability switches to $K(1, 2)$ at $t = 13.61$ s, indicating that both joints have failed.

- **Both joints are locked successively (Type 3)**

In this case, the 1st joint is locked at $t = 7$ s; then the 2nd joint is locked at $t = 13.5$ s. Fig. 7 illustrates the positions, velocities, and armature voltages of both joints. The posterior mode probabilities for fault detection and fault isolation are shown in Fig. 8. The fault of the 1st joint is detected and isolated within 0.03 s and 0.08 s respectively. At this moment, the model $K(1)$ has the highest probability since the 1st joint is locked. Then the 2nd joint is locked at $t = 13.5$ s and the model with highest probability switches to $K(1, 2)$ at $t = 13.61$ s, indicating that both joints have failed.

- **The 1st joint loses 60% of its output torque (Type 4)**

Suppose that the 1st joint suddenly loses 60% of its output torque at $t = 8$ s. The experimental results are shown in Figs. 9 and 10. We can see from Fig. 9 that this type of fault has minor effects on the tracking performance because the controller has compensated for the fault by increasing the armature voltage of the 1st joint after the fault has taken place.
The fault is detected and isolated within 0.07 s and 0.37 s respectively. Note that in the fault detection stage, the posterior mode probability of the kinematic model is just above the threshold $T_\text{D}$ when Type 4 fault has taken place. Some readers may argue that if the loss of the output torque is less than 60%, the fault may be undetected and the sensitivity to faults of the HMM-FDI scheme is questionable. However the reason for not detecting the slight loss of the output torque is that the controller has already made compensation for it. In such a case, a slight loss of the output torque is usually regarded as model uncertainties due to underestimation of actuator gains, and should be taken care of by a robust controller. Instead, alarms triggered by small variations of actuator gains may be considered as false alarms.

- **The output torque of the 2nd joint gradually decays (Type 5)**

Suppose that the output torque of the 2nd joint gradually decays after $t = 7$ s. More precisely, let $\tau_2$ be the output torque delivered by the controller to the 2nd joint, and $\tau_{2a}$ be the actual torque experienced by the 2nd link. For Type 5 fault, we assume that $\tau_{2a}(t) = e^{-0.15(t-7)}\tau_2(t)$ for $t \geq 7$. Experimental results are shown in Figs. 11 and 12.

Because the output torque of the 2nd joint gradually decays, the controller gradually increases the armature voltage of the 2nd joint to compensate for the loss of the control torque. The tracking performance degenerates slightly before the fault is detected (see Fig. 11). Consequently the HMM-FDI scheme takes a longer time to detect and isolate the fault (3.21 s and 3.51 s, respectively). However we consider the detection and isolation
Fig. 11. The output torque of the 2nd joint gradually decays, starting at $t = 7$ s. (a),(d) Joint positions: desired trajectory (solid line); real trajectory (dotted line). (b),(e) Joint velocities: desired velocities (solid line); estimated velocities (dotted line). (c),(f) Armature voltages of both joints.

Fig. 12. (a) The “effective factor” of the 2nd joint. (b) Posterior mode probabilities of the dynamic model (solid line) and the kinematic model (dashed line). The fault is detected at $t = 10.21$ s. (c) Posterior mode probabilities of $K(1)$ (solid line), $K(2)$ (dashed line) and $K(1, 2)$ (dash–dot line). The faulty joint is isolated at $t = 10.51$ s.

Table 4
Summary of the experimental results.

<table>
<thead>
<tr>
<th>Faults</th>
<th>Detection delay (s)</th>
<th>Isolation delay (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type 1</td>
<td>0.04</td>
<td>0.08</td>
</tr>
<tr>
<td>Type 2</td>
<td>0.03</td>
<td>0.08</td>
</tr>
<tr>
<td>Type 3</td>
<td>0.08 (for the 1st fault)</td>
<td>0.11 (for the 2nd fault)</td>
</tr>
<tr>
<td>Type 4</td>
<td>0.07</td>
<td>0.37</td>
</tr>
<tr>
<td>Type 5</td>
<td>3.21</td>
<td>3.51</td>
</tr>
</tbody>
</table>

The experimental results are summarized in Table 4. The detection delay and isolation delay refer to the time between the occurrence of the fault and the time at which the fault is detected and isolated, respectively. For the incipient fault (Type 5), the occurrence time of the fault refers to the time when the output torque starts decaying. It can be seen that all abrupt faults (Type 1–4) were detected and isolated successfully and immediately after their occurrences. Although the detection delay and the isolation delay for the incipient fault (Type 5) are longer, the tracking performance just deteriorates slightly when the fault is isolated. Therefore, safe operation of the robot manipulator is still preserved.

6. Conclusion

In this paper, we proposed the HMM-FDI scheme as a solution to the model set design problem, which is the most challenging part of the conventional MM-FDI approaches. The HMM-FDI
scheme incorporated only a small number of models which are mixtures of the dynamic and kinematic equations of the robot manipulator. Therefore it is much more computationally efficient than conventional MM–FDI methods. In addition, the HMM-FDI scheme is applicable to various types of unexpected actuator faults, including abrupt faults, incipient faults, and simultaneous faults. Experiments were conducted on a two-joint robot manipulator. The experimental results verified the good performance of the HMM-FDI scheme.

References

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