A number of prior studies have developed a variety of multivariate volatility models to describe the joint distribution of spot and futures, and have applied the results to form the optimal futures hedge. In this study, the authors propose a new class of multivariate volatility models encompassing realized volatility (RV) estimates to estimate the risk-minimizing hedge ratio, and compare the hedging performance of the proposed models with those generated by return-based models. In an out-of-sample context with a daily rebalancing approach, based on an extensive set of statistical and economic performance measures, the empirical results show that improvement can be substantial when switching from daily to intraday. This essentially comes from the advantage that the intraday-based RV potentially can provide more accurate daily covariance matrix estimates than RV utilizing daily prices. Finally, this study also analyzes the effect of hedge horizon on hedge ratio and hedging effectiveness for both the in-sample and the out-of-sample data. © 2009 Wiley Periodicals, Inc. Jrl Fut Mark 30:874–896, 2010

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INTRODUCTION

A considerable amount of studies on futures hedging have focused on modeling the joint distribution of spot and futures prices and applying the results to estimate the optimal hedge ratio. Although the early studies assume that the hedge ratio is constant over time (e.g., Ederington, 1979), recent studies have documented that the joint distribution, and hence the hedge ratio, should be time dependent due to the time-varying nature of risks (e.g., Kroner & Sultan, 1993). Since then, varieties of multivariate volatility techniques have been applied. Baillie and Myers (1991), Myers (1991), Kroner and Sultan (1993), Brooks, Henry, and Persand (2002), Lien, Tse, and Tsui (2002), and Lien and Yang (2006) are examples of studies that apply generalized autoregressive conditional heteroscedasticity (GARCH) models. As a result, the central issue in the context of a dynamic hedge is to provide the conditional covariance matrix forecast that can characterize the dynamics of the distribution more realistically.

However, it has been shown that most of the latent GARCH models fail to satisfactorily describe the high kurtosis, small first-order autocorrelation of squared returns, and slow decay of the autocorrelation of squared returns toward zero that have been observed in many daily or weekly financial returns (e.g., Carnero, Peña, & Ruiz, 2004). The search for alternative volatility techniques has motivated scholars to exploit information in intraday high-frequency data (e.g., Andersen & Bollerslev, 1998; Andersen, Bollerslev, Diebold, & Labys, 2003; Barndorff-Nielsen & Shephard, 2004; Hayashi & Yoshida, 2005; Voev & Lunde, 2007). This so-called realized volatility (RV) approach provides a direct and consistent technique to estimate the latent volatility process without the need for relying on explicit models. Therefore, it has served as an ex-post benchmark for assessing the quality of any ex-ante volatility forecasts (e.g., Andersen, Bollerslev, Christoffersen, & Diebold, 2006). In forecasting future volatility, studies have shown that RV can provide more accurate forecasts than methods using daily squared returns (e.g., Blair, Poon, & Taylor, 2001). Recently, RV has been employed to explore the economic value (EV) of investment by Fleming, Kirby, and Ostdiek (2003), Bandi, Russell, and Zhu (2008),

---

1With the aim of reducing risk, this hedge ratio is equivalent to the ratio of the conditional covariance between the spot and futures over the conditional variance of the futures.
2In addition to the GARCH framework, other studies use stochastic volatility models (e.g., Lien & Wilson, 2001).
3To capture the high kurtosis of returns and low first-order autocorrelation of return squares simultaneously, GARCH models often require a high persistence and/or leptokurtic conditional distributions when they are fitted to the financial time series (Carnero et al., 2004). The restrictions on GARCH then severely restrict the allowed dynamic dependence of the volatility.
4Generally, in the absence of market microstructure and nonsynchronous trading (Epps effect), a daily measure of variance is computed as the sum of the squared intraday equidistant returns, and a daily measure of covariance is obtained by summing the products of intraday equidistant returns, for the given trading day. For a review of the RV refers to McAleer and Medeiros (2008).
and De Pooter, Martens, and van Dijk (2008). They find that the EV is substantial when switching from daily to intraday returns, even without applying bias-correction techniques in constructing realized estimates. As a result, the superiority of RV-based investment may result because it takes into account finer intraday information and thus potentially provides more accurate daily covariance matrix estimates or forecasts than methods utilizing daily prices.

This study attempts to improve the performance of a risk-minimizing futures hedge when the intraday-based RV approach is incorporated into forecasting the relevant covariance matrix. It is not clear, however, whether the accurate RV is used or not may differentiate the performance of a futures hedge. To address this issue, a new RV-based method is demonstrated in this study. The proposed method builds on the bivariate error correction model by employing the flexible constant conditional correlation (CCC) GARCH error structure of Kroner and Sultan (1993). The advantage of extending their model is that it can capture the long-run cointegration relationship and the time-varying second moments simultaneously when the dynamics of the joint distribution is specified. Moreover, when the leverage effect and/or the dynamic correlation are revealed, the asymmetric volatility and/or the dynamic conditional correlation (DCC) models can also be incorporated into this method. These desirable properties thus provide a more convenient way to lodge the realized covariance matrix in the GARCH error structures as compared with the rolling estimators of Fleming et al. (2003), Bandi et al. (2008), and De Pooter et al. (2008). The RV-based method, which uses finer volatility proxies in estimating and forecasting the conditional covariance matrix, is expected to provide better descriptions on the spot-futures dynamics and the resulting hedge ratios than methods using squared return shocks.

In the empirical analyses, the RV-based hedge ratios are calculated in an out-of-sample context spanning the period of December 19, 2003 through March 31, 2009 for the highly traded S&P 500 index futures contracts. We compare the performance of the RV-based hedge with the return-based GARCH and the ordinary least squares (OLS) hedges using an extensive set of statistical and economic measures. The comparisons are conducted for both short and long hedgers. To anticipate the results, this study finds that the RV-based hedge can substantially outperform the return-based GARCH and/or the static OLS hedges especially during the surge in volatility period. Then the RV-based method is applied to examine the effect of hedging horizon (ranges from 5 to 30 days) on the performance of the RV-based hedge.

5For example, Fleming et al. (2003) show how a risk-averse investor would be willing to pay 50–200 basis points per year to capture the multivariate volatility forecasts based on intraday returns instead of daily returns in the context of investment decisions on three actively traded futures contracts (S&P 500 index, Treasury bonds, and gold). It is assumed that the investor follows a volatility-timing strategy, which rebalances his portfolio only when the estimated conditional covariance matrix of the daily returns changes. This case treats the expected daily returns as time-invariant.
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one week to three month) on hedge ratio and hedging effectiveness. The results show that hedge ratio tends to increase and to approach unity (i.e., naïve hedge ratio) with the length of hedging horizon; and, hedging effectiveness tends to increase as the length of hedging horizon increases. The rest of the study is organized as follows. First, we present the conventional hedging method and demonstrate the RV-based method used in this study. Next, we present the data and their properties with the empirical results. Finally, the last section concludes the study.

THE CONVENTIONAL HEDGING MODELS

Kroner and Sultan (1993) have proposed a bivariate GARCH error correction model for modeling the joint distribution of spot and futures. As such, the most prominent application of this model is to estimate time-varying hedge ratios. Let \( r_{st} \) and \( r_{ft} \) denote, respectively, the changes in the logarithmic spot price, \( S_t \), and the logarithmic futures price, \( F_t \), between time \( t - 1 \) and \( t \). The econometric model for the daily returns conditioning on the set of all relevant information \( \Phi_{t-1} \) at time \( t - 1 \) can be described as

\[
\begin{align*}
    r_{st} &= \alpha_{0s} + \alpha_{1s}(S_{t-1} - \delta F_{t-1}) + e_{st} \\
    r_{ft} &= \alpha_{0f} + \alpha_{1f}(S_{t-1} - \delta F_{t-1}) + e_{ft} \\
    \begin{pmatrix} e_{st} \\ e_{ft} \end{pmatrix} &\sim N(0, H_t)
\end{align*}
\]

(1)

where \( (S_{t-1} - \delta F_{t-1}) \) is the error correction term (ECT). The incorporation of ECT in the conditional mean equations is essential, especially in currency and equity markets (see Brooks et al., 2002; Choudhry, 2003; Park & Switzer, 1995). The residual vector \( (e_{st}, e_{ft})' \) is postulated as a bivariate normal distribution with a \( 2 \times 1 \) zero mean vector and a \( 2 \times 2 \) time-varying covariance matrix

\[
H_t = \begin{bmatrix} h_{s,t} & h_{sf,t} \\ h_{sf,t} & h_{f,t} \end{bmatrix} = \begin{bmatrix} h_{s,t}^{1/2} & 0 \\ 0 & h_{f,t}^{1/2} \end{bmatrix} \begin{bmatrix} 1 & \rho \\ \rho & 1 \end{bmatrix} \begin{bmatrix} h_{s,t}^{1/2} & 0 \\ 0 & h_{f,t}^{1/2} \end{bmatrix} = D_t R D_t
\]

(3)

where \( h_{sf,t} \) is a conditional covariance, and \( h_{s,t} \) and \( h_{f,t} \) are conditional variances for the spot and futures returns, respectively, and \( \rho \) is the time-invariant correlation coefficient between them. That is, the model applies the CCC estimator of Bollerslev (1990) to model and forecast the bivariate conditional covariance matrix.

The expressions of the conditional variances \( h_{s,t} \) and \( h_{f,t} \) in Equation (3) are typically thought of as univariate GARCH-type models. For example, the
GARCH(1,1) structure introduced by Bollerslev (1986) for the returns can be specified as

\[ h_{s,t} = \beta_{0s} + \beta_{1s} h_{s,t-1} + \beta_{2s} \epsilon_{s,t-1}^2 \]  
\[ h_{f,t} = \beta_{0f} + \beta_{1f} h_{f,t-1} + \beta_{2f} \epsilon_{f,t-1}^2 \]  

(4)

When the leverage effect is revealed, asymmetric volatility models are commonly formulized, such as the GJR (Glosten–Jagannathan–Runkle) model of Glosten, Jagannathan, and Runkle (1993). This simply modifies the standard GARCH(1,1) model with an additional ARCH (autoregressive conditional heteroscedasticity) term conditional on the sign of the past innovation. The conditional volatilities of Equation (4) are then reformulated as

\[ h_{s,t} = \beta_{0s} + \beta_{1s} h_{s,t-1} + \beta_{2s} \epsilon_{s,t-1}^2 + \beta_{3s} \epsilon_{s,t-1}^2 I(\epsilon_{s,t-1} < 0) \]  
\[ h_{f,t} = \beta_{0f} + \beta_{1f} h_{f,t-1} + \beta_{2f} \epsilon_{f,t-1}^2 + \beta_{3f} \epsilon_{f,t-1}^2 I(\epsilon_{f,t-1} < 0) \]  

(5)

where \( I(\cdot) \) denotes an indicator function. For estimating the constant correlation coefficient, the ever-popular rolling estimator uses equal weight to all past \( T \) return innovations:

\[ \hat{\rho} = \frac{\sum_{t=1}^{T} \epsilon_{s,t} \epsilon_{f,t}}{\sqrt{\left( \sum_{t=1}^{T} \epsilon_{s,t}^2 \right) \left( \sum_{t=1}^{T} \epsilon_{f,t}^2 \right)}} \in [-1, 1] \]  

(6)

To fit in with reality, however, the conditional correlation coefficient can be relaxed to vary with time (Engle, 2002; Tse & Tsui, 2002). That is, the conditional covariance matrix of Equation (3) is generalized to the DCC formulation:

\[ H_t = \begin{bmatrix} h_{s,t} & h_{sf,t} \\ h_{sf,t} & h_{f,t} \end{bmatrix} = \begin{bmatrix} h_{s,t}^{1/2} & 0 \\ 0 & h_{f,t}^{1/2} \end{bmatrix} \begin{bmatrix} 1 & \rho_t \\ \rho_t & 1 \end{bmatrix} \begin{bmatrix} h_{s,t}^{1/2} & 0 \\ 0 & h_{f,t}^{1/2} \end{bmatrix} = \bar{D} \rho_t \bar{D} \]  

(7)

The evolution of \( \rho_t \) in this study is analogous with the univariate GARCH equation:

\[ \rho_t = (1 - \theta_1 - \theta_2) \bar{\rho} + \theta_1 \rho_{t-1} + \theta_2 \frac{\sum_{h=1}^{M} \eta_{s,t-h} \eta_{f,t-h}}{\sqrt{\left( \sum_{h=1}^{M} \eta_{s,t-h}^2 \right) \left( \sum_{h=1}^{M} \eta_{f,t-h}^2 \right)}} \]  

(8)

where \( \theta_1 \) and \( \theta_2 \) are nonnegative with \( \theta_1 + \theta_2 \leq 1 \); the sample size \( M = 2 \) for estimating the sample correlation coefficient with \( \eta_{i,t-h} = \epsilon_{i,t-h} / h_{i,t-h}^{1/2} \) (\( i = s, f \)) follows Tse and Tsui (2002); \( \bar{\rho} \) is the unconditional correlation between spot and futures.
Given the null hypothesis that the set of all relevant information $\Phi_{t-1}$ is observed with correctly specified models, these CCC or DCC models with the ECT describe the dynamic nature of spot-futures distributions. In particular, this GARCH class of volatility (correlation) models provides simple ways to forecast the bivariate volatility by using actual return innovations and the estimated hedge ratio by minimizing the risk of the hedged portfolio return at time $t$ is given by

$$\hat{\beta}^*_t = \hat{h}_{sf,t+1}/\hat{h}_{f,t+1}$$  \hspace{1cm} (9)

where $\hat{h}_{sf,t+1}$ and $\hat{h}_{f,t+1}$ are the covariance and variance forecasts using Equations (3) or (7). In brief, Equations (1) through (9) then construct the conventional hedge ratio models, namely, the ECT-GARCH-CCC model (Equations (1)–(4), (6), and (9)), the ECT-GARCH-DCC model (Equations (1)–(2), (4), and (7)–(9)), the ECT-GJR-CCC model (Equations (1)–(3), (5)–(6), and (9)), and the ECT-GJR-DCC model (Equations (1)–(2), (5), and (7)–(9)).

**ALTERNATIVE MODELS USING RV**

To explore the incremental value of a RV-based hedge, the realized variance and/or correlation are encompassed within the conventional CCC and DCC models with the ECT specification. Following the previous specifications, the RV-based GARCH(1,1) volatility can be expressed as

$$h_{s,t} = \beta_0 + \beta_1 h_{s,t-1} + \beta_2 s \text{RV}_{s,t-1}$$
$$h_{f,t} = \beta_0 + \beta_1 h_{f,t-1} + \beta_2 f \text{RV}_{f,t-1}$$  \hspace{1cm} (10)

where each $\text{RV}_{i,t-1}$ ($i = s, f$) is defined by summing up $\Delta$-minute squared returns at time $t - 1$. Analogously, the RV-based GJR(1,1) model can be reformulated as

$$h_{s,t} = \beta_0 + \beta_1 h_{s,t-1} + \beta_2 s \text{RV}_{s,t-1} + \beta_3 s \text{RV}_{s,t-1} I(e_{s,t-1} < 0)$$
$$h_{f,t} = \beta_0 + \beta_1 h_{f,t-1} + \beta_2 f \text{RV}_{f,t-1} + \beta_3 f \text{RV}_{f,t-1} I(e_{f,t-1} < 0)$$  \hspace{1cm} (11)

That is, the right-hand side squared residuals in the conventional GARCH or GJR models are replaced by realized variances. To encompass the realized correlation $\text{RCorr}_{t-1} = \text{RCov}_{t-1}/(\text{RV}_{s,t-1} \text{RV}_{f,t-1})^{1/2}$ within the conditional correlation dynamics, Equation (8) can be modified as

$$\rho_t = (1 - \theta_1 - \theta_2)\bar{\rho} + \theta_1 \rho_{t-1} + \theta_2 \text{RCorr}_{t-1}$$  \hspace{1cm} (12)

where the realized covariance $\text{RCov}_{t-1}$ is defined by cumulating the cross-products of intraday spot and futures returns at time $t - 1$. For estimating the
constant correlation in the RV-based CCC model, however, the sample mean of
the realized correlations should be a biased estimate due to nonsynchronous
trading (Epps effect) and/or market microstructure noise (see, e.g., Hayashi &
Yoshida, 2005; Voev & Lunde, 2007). To simplify the estimation process, the
rolling estimator of Equation (6) is still adopted. Then, these modifications con-
struct a new class of RV-based hedge ratio models, namely, the ECT-RV-GARCH-
CCC model (Equations (1)–(3), (6), (9), and (10)), the ECT-RV-GARCH-DCC
model (Equations (1)–(2), (7), (9), (10), and (12)), the ECT-RV-GJR-CCC model
(Equations (1)–(3), (6), (9), and (11)), and the ECT-RV-GJR-DCC model
(Equations (1)–(2), (7), (9), and (11)–(12)).

To estimate the parameters in the RV-based or the conventional CCC or
DCC models, we follow the two-step estimation procedure of Bollerslev (1990)
and Engle (2002). As this class of multivariate volatility models has separate
parameters, it can be estimated easily and consistently in two steps.6 With the
normality assumption of Equation (2), we can maximize each volatility term
with the conditional mean in the first step:

$$\hat{\theta}_i = \arg \max \{L_{V_i}(\hat{\theta}_i)\}$$

where $\theta_i = (\alpha_i, \beta_i, \delta)$ and $L_{V_i}$ denote the Gaussian quasi-likelihood function for
asset $i$, and then maximize the correlation term:

$$\hat{\theta} = \arg \max \{L_C(\hat{\theta})\}$$

in the second step, $L_C$ represents the Gaussian quasi-likelihood function of the
correlation part, and $\theta = \rho$ for the CCC and $\theta = (\theta_1, \theta_2)$ for the DCC. Without
the normality assumption, these estimators still have the quasi-maximum like-
lihood interpretation.

**EMPIRICAL ANALYSES**

**Data Descriptions**

The performance of the RV-based hedging method is examined empirically on
the S&P 500 index futures contracts traded on Chicago Mercantile Exchange
(CME). The sample period is from January 1, 1998 to March 31, 2009, which
covers the period of subprime mortgage crisis. We obtain the daily closing (set-
ttlement) prices for the spot (futures) from the Datastream and the intraday

---

6Engle and Granger (1987) indicate that a cointegration system could consistently be estimated via a two-
step estimator, where both steps require only single equation least squares, so that we can estimate the DCC-
type models with the ECT by using the two-step procedure of Bollerslev (1990) and Engle (2002).
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transaction prices for them from Tick Data Inc. Note that this study rolls the nearest month contract to the next month when the daily volume of the current contract is exceeded. Specifically, daily and intraday prices of all days corresponding to U.S. public holidays are removed. Hence, there are 2828 trading days for the period examined.

Table I reports the diagnostic checks on the distribution properties of the daily spot (futures) returns, which are calculated as differenced natural logarithmic daily closing (settlement) prices. The results of unit root and cointegration tests are shown in Panel A, and summary statistics on the returns are reported in Panel B. The augmented Dickey–Fuller tests show that the spot and futures log-prices have a unit root, but their first-differenced series are stationary. The Johansen trace statistic indicates that the spot and futures prices are cointegrated with the cointegrating parameter $\hat{\delta} \approx 1$. The unconditional distributions of the univariate returns reveal nonnormality, as evidenced by the nonzero skewness, high kurtosis, and significant Jarque–Bera statistics. Panel C

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**TABLE I**

Data Description: Daily Price Returns

<table>
<thead>
<tr>
<th>Indices</th>
<th>ADF (price)</th>
<th>ADF (return)</th>
<th>Trace</th>
<th>$\hat{\delta}$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Panel A: Unit root and cointegration tests</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Spot</td>
<td>-1.36</td>
<td>-42.15*</td>
<td>84.97*</td>
<td>0.9841</td>
</tr>
<tr>
<td>Futures</td>
<td>-1.36</td>
<td>-42.40*</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Mean Std. Dev. Skewness Kurtosis Correlation JB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spot 0.0001 0.0138 -0.1280 10.5955 0.9760 6798.74*</td>
</tr>
<tr>
<td>Futures 0.0001 0.0141 0.0369 12.4322 10480.13*</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>ACF(1) ACF(2) ACF(3) ACF(4) ACF(5) Q$^2$(10)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spot 0.3661* 0.1785* 0.2935* 0.3307* 0.2982* 2230.80*</td>
</tr>
<tr>
<td>Futures 0.4093* 0.1692* 0.2526* 0.3000* 0.2516* 2032.04*</td>
</tr>
<tr>
<td>Spot-Futures 0.1970* 0.4310* 0.1727* 0.3139* 0.3488* 1279.50*</td>
</tr>
</tbody>
</table>

Notes. The daily spot (futures) returns are calculated as differenced natural logarithmic closing (settlement) prices where public holidays are removed. The sample period for the prices runs from January 1, 1998 to March 31, 2009 and the sample size for each is 2,828. The values in rows ADF, Trace, JB, ACF($k$), and $Q^2$(10) are statistics of the augmented Dickey–Fuller unit root test, the Johansen cointegration test, the Jarque–Bera normality test, the order $k$ autocorrelation of squared returns, and the Ljung–Box test for the serial correlations in the squared returns. $\hat{\delta}$ is the estimated cointegrating parameter. * indicate significance at the 5% level.

7The intraday transaction observations consist of open, high, low, and close prices at the one-minute sampling frequency.
provides the autocorrelation functions (ACF) as well as the Ljung–Box statistics of the squared (cross-product) daily returns. The first-order ACF ranges from 0.1970 to 0.4093 but decays slowly toward zero. Based on the empirical evidences and the findings of Carnero et al. (2004), the conventional GARCH models may be inadequate to describe the spot-futures volatility dynamics, hence, it is not clear whether the inadequacy may damage the performance of a futures hedge.

To construct the realized (co-)variance for the alternative method, the intraday futures prices after 3:00 p.m. Chicago time for each day are dropped as the futures market closes 15-minutes later than the spot market.8 We divide the contemporaneous time section across the markets, which runs from 8:30 a.m. until 3:00 p.m. (390-minutes), into m (nonoverlapping) intervals of equal lengths $\Delta = 390/m$ such that the times $t_j = t_{j-1} + \Delta$ for $j = 1, \ldots, m$ with $t_0 = 8:30$ a.m. Chicago time. The log close price at time $t_j$ is denoted as $p(t_j)$, then the equidistant intraday returns on day $t$, $r_{ij} = p(t_j) - p(t_{j-1})$, for $j = 2, \ldots, m$; and, the first period ($j = 1$) intraday returns are defined as the difference between the log close and open prices during that time interval. With these mathematical definitions, the realized variance is then defined as $RV_{it}^{(m)} = \sum_{i=1}^{m} r_{i,t_j}^2$ for $i = s, f$, and the realized covariance is defined as $RCov_{it}^{(m)} = \sum_{j=1}^{m} r_{s,j} r_{f,t_j}$ for each day $t$.

This study uses 15-minute intraday prices ($m = 26$) to construct the realized (co-)variance estimates, and summarizes their descriptive statistics in Table II. As only observations during the floor trading section are sampled, the average realized variances are smaller than the corresponding unconditional variances obtained from daily returns. For example, the average value of the

---

**TABLE II**

Data Description: Realized Variance, Covariance, and Correlation

<table>
<thead>
<tr>
<th>Realized Estimates</th>
<th>Summary Statistics</th>
<th>Autocorrelation Functions</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>Median</td>
</tr>
<tr>
<td>$RV_{st}$</td>
<td>1.11e-4</td>
<td>5.40e-5</td>
</tr>
<tr>
<td>$RV_{ft}$</td>
<td>1.20e-4</td>
<td>5.90e-5</td>
</tr>
<tr>
<td>$RCov_t$</td>
<td>1.11e-4</td>
<td>5.40e-5</td>
</tr>
<tr>
<td>$RCorr_t$</td>
<td>0.9506</td>
<td>0.9595</td>
</tr>
</tbody>
</table>

**Notes.** The sample period for these (daily) realized estimates, which are constructed from fifteen-minute equidistant intraday returns, spans the period of January 1, 1998–March 31, 2009, and the sample size is 2,828. It is noted that the futures returns after 3:00 p.m. Chicago time for each day are dropped as the futures markets close fifteen minutes later than the spot markets. The ACF($k$) indicates the sample autocorrelation function of the realized estimates corresponding to lags $k = 1, 2, \ldots, 5$. The upper and lower confidence bounds of the ACF with the 5% confidence level are 0.0375 and $-0.0375$, respectively.

---

8The (floor) trading section for the S&P 500 index futures on the CME runs from 8:30 a.m. Chicago time until 3:15 p.m. Chicago time.
realized variance estimates for the S&P 500 cash index is $1.11 \times 10^{-4}$, which is about 58% of the unconditional variance $1.90 \times 10^{-4}$ calculated from Table I. To measure the realized variance (covariance) for the whole day, the squared (cross-product) overnight returns can further be incorporated into the realized estimators (De Pooter et al., 2008; Fleming et al., 2003, Hansen & Lunde, 2005; Martens, 2002). For the realized correlations, the average level for the S&P 500 (about 0.95) shows slight bias toward zero as compared with the corresponding unconditional correlation estimates (about 0.98) using Equation (6). According to Hayashi and Yoshida (2005) and Voev and Lunde (2007), the biasness may come from the nonsynchronous trading and/or the market microstructure noise, but it can be corrected using some bias-correction techniques. The ACF of these realized estimates are also reported in Table II. It shows that these realized second moments reveal considerable persistency. However, the ACF of the realized variance (covariance) is higher than the corresponding ACF of squared (cross-product) returns in Table I. For example, in the spot market, the ACF(1) of the realized variance is about 0.66, which is higher than the ACF(1) of the squared returns in Table I by about 0.37. We expect that the behavior difference between the realized variance (covariance) and squared (cross-product) returns should produce different volatility (covariance) estimates and forecasts based on the alternative and the conventional methods.

**Estimation Results**

Table III presents the estimation results of the return-based and the RV-based GARCH models. Panel A shows the conditional mean and variance estimates, and Panel B shows the conditional correlation estimates. Given the evidence of the cointegration relationship between the spot and futures (in Table I), the restricted ECT $(S_{t-1} - F_{t-1})$, is parameterized in the conditional mean equations to avoid the loss of long-run information; though, all $\alpha_{1t}$ are insignificant different from zero (Brooks et al., 2002; Park & Switzer, 1995). The insignificance of $\alpha_{yi}$ and $\alpha_{1f}$ coefficients show the expected returns of futures should be zero, meaning the minimum variance hedge is generally the expected utility maximization hedge (Baillie & Myers, 1991; Kroner & Sultan, 1993).

Although the estimates of the conditional mean equations are similar, the results in the conditional variance and/or correlation equations are quite different. Concerning the result of the conventional models, the insignificance of the $\beta_{2i}$ shows the symmetric GARCH specification seems more suitable for the

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9We do not adjust for the biases in the empirical analyses because the bias-correction procedures do not guarantee a positive definite realized covariance matrix estimates; see De Pooter et al. (2008) for discussions.
data. The persistence of the GARCH for the spot and futures are about 0.9947 and 0.9933, respectively, which suggests the conditional volatilities reveal high persistence. For the correlation equations, the inferences conclude that the DCC is held. Hence, the empirical evidence using daily information indicates the ECT-GARCH-DCC model fits reasonably well to the S&P 500 market.
Then turn to the estimation results of the RV-based models. The significance of $\beta_{3i}$ suggests that the asymmetry in volatility are revealed. A positive $\beta_{3i}$ shows that the impact of a positive return shock on the current volatility is smaller than that of a negative return shock of the same magnitude. Particularly, the persistence of volatility implied by the RV-based models is about 0.9999, which is higher than the persistence implied by the return-based models. Besides the persistence, the weight on the persistence parameters between the two methods also differs. Taking the spot volatility as an example, the return-based GARCH estimates of $\beta_{1i} (\beta_{2i})$ is about 0.91 (0.08), whereas the RV-based GARCH estimates of $\beta_{1i} (\beta_{2i})$ is about 0.77 (0.23). The higher weight on the $\beta_{2i}$ using RV-based GARCH indicates that past RV may provide more information in predicting the current volatility than those using lagged daily return squares. For the conditional correlation equations, the significance of $u_{1}$ and $u_{2}$ for the S&P 500 indicates the null of mean-reverting DCC hypothesis is held. In addition, the higher persistence of the RV-based correlation than the return-based one is also observed from the empirical evidence. It shows that the persistence of correlation implied by the RV-based models is about 0.99, which is much higher than the persistence (ranges from 0.19 to 0.29) implied by the return-based models. Thus, the empirical evidence using RV indicates the ECT-RV-GJR-DCC model seems suitable to the S&P 500 data. Figure 1 compares the conditional volatility and correlation estimates using the two methods. We report the best-fitted models among them to save space. It is evident that the RV-based second moment estimates are not equal to those of the return-based models. Essentially, the difference should come from the dynamics difference between the RV and the return squares.

**RV-based Hedge Ratios and their Hedging Performances**

We now turn to analyze the performance of a futures hedge using the RV approach. As the hedging decision has to be made ex-ante, the evaluation is conducted in an out-of-sample context using a rollover method.\(^\text{10}\) To do so, this study splits the full sample period into two: the in-sample period (from January 1, 1998 to December 18, 2003; 1500 observations), and the out-of-sample period (from December 19, 2003 to March 31, 2009; 1328 observations). Each model is estimated with the use of the in-sample data and then re-estimated with a daily rollover in the out-of-sample period, keeping the estimation sample size of 1500 (fixed). This rollover method is continued for all the 1328 out-of-samples. The estimated hedge ratios as indicated in Equation (9) for each model are

\(^\text{10}\)This rollover method is also used in Lien et al. (2002) and Lien and Yang (2006).
subsequently constructed, and the corresponding realized portfolio returns for both the short \((r_{p,t+1} = r_{s,t+1} - \beta_t r_{f,t+1})\) and the long \((r_{p,t+1} = -r_{s,t+1} + \beta_t r_{f,t+1})\) hedges are calculated. In addition to the dynamic models specified in the previous sections, we also evaluate the performance of the static OLS method based on this rollover method. Particularly, to see whether the RV-based models can provide a superior hedging performance during the crisis, the results before (Period I: December 19, 2003 through September 28, 2007, 950 observations) and during (Period II: October 1, 2007 through March 31, 2009, 378 observations) that period are separately reported.

Table IV exhibits some diagnostic statistics of the hedge ratios; and, Figure 2 plots the dynamic hedge ratios.\(^{11}\) On average, the RV-based hedge ratios are larger (smaller) than the conventional return-based hedge ratios in Period I (II); however, they have smaller variation in both the periods. The ADF tests on the hedge ratios illustrate the unit-root hypothesis is rejected at the 5% level except

\(^{11}\)As the CCC-based hedge ratios are similar to the DCC-based ones, we do not plot them to save space.
for the results based on the OLS (in both periods) and the ECT-GARCH-CCC (in period II) models. The study also reports the ACF values of these out-of-sample hedge ratios up to lag five. It is apparent that, the ACF of the RV-based hedge ratios is smaller but decays more quickly than the ACF of the return-based hedge ratios.

Table V presents several statistics on the realizations of the hedged portfolio returns. Considering the hedging performance using standard deviation (Std. Dev.), the results show that the RV-based method yields an average sample volatility of 0.1730% (0.4284%) for the Period I (II), which is smaller than the 0.1745% (0.4404%) of the conventional method. That is, the improvement of the RV-based method over the return-based method is about 0.90 and 2.74% for the Periods I and II, respectively. Particularly, the RV-based method even can

### Table IV
Summary Statistics of Out-of-Sample Hedge Ratios

<table>
<thead>
<tr>
<th>Statistics</th>
<th>ECT-GARCH</th>
<th>ECT-RV-GARCH</th>
<th>ECT-GJR</th>
<th>ECT-RV-GJR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>CCC</td>
<td>DCC</td>
<td>CCC</td>
<td>DCC</td>
</tr>
<tr>
<td>Mean</td>
<td>0.9820</td>
<td>0.9761</td>
<td>0.9908</td>
<td>0.9864</td>
</tr>
<tr>
<td>Std. Dev.</td>
<td>0.0415</td>
<td>0.0427</td>
<td>0.0246</td>
<td>0.0242</td>
</tr>
<tr>
<td>Min</td>
<td>0.8314</td>
<td>0.8037</td>
<td>0.8795</td>
<td>0.8749</td>
</tr>
<tr>
<td>Max</td>
<td>1.0859</td>
<td>1.0778</td>
<td>1.0771</td>
<td>1.0707</td>
</tr>
<tr>
<td>ACF(1)</td>
<td>0.9036</td>
<td>0.8353</td>
<td>0.6509</td>
<td>0.6453</td>
</tr>
<tr>
<td>ACF(2)</td>
<td>0.8272</td>
<td>0.7486</td>
<td>0.4817</td>
<td>0.4735</td>
</tr>
<tr>
<td>ACF(3)</td>
<td>0.7585</td>
<td>0.6850</td>
<td>0.3343</td>
<td>0.3264</td>
</tr>
<tr>
<td>ACF(4)</td>
<td>0.6996</td>
<td>0.6335</td>
<td>0.2570</td>
<td>0.2487</td>
</tr>
<tr>
<td>ACF(5)</td>
<td>0.6500</td>
<td>0.5886</td>
<td>0.2206</td>
<td>0.2104</td>
</tr>
</tbody>
</table>

#### Panel A: Period I (December 19, 2003~September 28, 2007, 950 observations)

#### Panel B: Period II (October 1, 2007~March 31, 2009, 378 observations)

Notes. The ADF indicates the augmented Dickey-Fuller unit root test based on trend stationary AR model, where the 5% critical values for Period I and II are −3.4150 and −3.4234, respectively. The ACF(k) indicates the sample autocorrelation function of the hedge ratios corresponding to lags k. Their 95% confidence bounds for Periods I and II are [−0.0649, 0.0649] and [−0.1029, 0.1029], respectively.

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12This agrees with the finding of Lien et al. (2002), who report that the out-of-sample GARCH hedge ratios are stationary.
surpass the simple OLS method during the crisis, whereas the return-based GARCH method does not.\textsuperscript{13} Besides the Std. Dev., two alternatives, namely the value-at-risk (VaR) and the expected shortfall (ES), are also included in the comparisons as the evaluation results may change if performance criteria other than traditional measures are applied (Cotter & Hanly, 2006).\textsuperscript{14} The result shows that using the RV-based method generally can provide a better performance in managing portfolio VaR and ES especially during the crisis period. In addition,

\textsuperscript{13}Lien et al. (2002) indicate that the out-of-sample CCC-GARCH hedge does not outperform the OLS hedge in the S&P 500 market, where their data were extracted for the period of January 1988 through June 1998. However, Cotter and Hanly (2006) show that the CCC-GARCH hedge can beat the OLS hedge in the S&P 500 market in terms of variance reduction, where their data were extracted for the period of January 1998 through December 2003.

\textsuperscript{14}The VaR is defined by the negative of the $\alpha$th empirical percentile of the realizations on hedged portfolio returns, i.e., \( \text{VaR}(\alpha) = -\bar{F}_{\alpha}(\tilde{r}_{pt+1}; \alpha) \), where \( \bar{F}_n \) denotes the empirical distribution of the hedged portfolio returns using the $n$ realized observations. A major shortcoming with the VaR is that it is not a coherent risk measure (Artzner, Delbaen, Eber, & Heath, 1999). Hence, the ES measure has received some attention recently. The ES summarizes the negative of the average returns on the portfolio given that the hedged portfolio return has exceeded its $\alpha$th empirical percentile, or \( \text{ES}(\alpha) = -\bar{E}_n(\tilde{r}_{pt+1} \mid \tilde{r}_{pt+1} \leq -\text{VaR}(\tilde{r}_{pt+1}; \alpha)) \), where \( \bar{E}_n \) represents the sample average operator. This gives the hedger additional information about both the probability of losses and possible magnitude of losses beyond the $\alpha$th percentile.
### TABLE V
Out-of-Sample Comparisons of Hedging Performance: Statistical Evaluations

<table>
<thead>
<tr>
<th>Models</th>
<th>Short Hedge</th>
<th>Long Hedge</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Std. Dev.</td>
<td>VaR(95)</td>
</tr>
<tr>
<td></td>
<td>(×10⁻²)</td>
<td>(×10⁻²)</td>
</tr>
<tr>
<td>ECT-GARCH-CCC</td>
<td>0.1753</td>
<td>0.2917</td>
</tr>
<tr>
<td></td>
<td>(0.0024)</td>
<td>(0.0085)</td>
</tr>
<tr>
<td>ECT-RV-GARCH-CCC</td>
<td>0.1750</td>
<td>0.2888</td>
</tr>
<tr>
<td></td>
<td>(0.0169)</td>
<td>(0.0074)</td>
</tr>
<tr>
<td>ECT-GARCH-DCC</td>
<td>0.1730</td>
<td>0.2699</td>
</tr>
<tr>
<td></td>
<td>(0.0008)</td>
<td>(0.0164)</td>
</tr>
<tr>
<td>ECT-RV-GJR-DCC</td>
<td>0.1738</td>
<td>0.2600</td>
</tr>
<tr>
<td></td>
<td>(0.0106)</td>
<td>(0.0134)</td>
</tr>
<tr>
<td>OLS</td>
<td>0.1719</td>
<td>0.2719</td>
</tr>
</tbody>
</table>


**Panel B: Period II (October 1, 2007 ~ March 31, 2009, 378 observations)**

The values in columns Std. Dev., VaR, and ES are standard deviation, value-at-risk, and expected shortfall of the realized hedged portfolio returns. The entries in the parentheses are the relative values of the improvement of the alternative over the conventional hedge ratio models. The bold values are the best hedging model based on each risk measure.
in Period II, the improvement of RV-based method over the conventional method tends to enlarge when the percentile has moved toward 99%. For example, on average, the improvement of long hedges in VaR(0.95), ES(0.95), VaR(0.99), and ES(0.99) is about 2.53, 8.33, 20.82, and 11.43% (the percentage change in VaR and ES reduction), respectively; and they all can surpass the simple OLS method whereas the return-based models cannot. For the performance in Period I, it seems that the RV-based method is inferior to the conventional method. In this period, it is observed that the OLS hedge has the best performance in most of the cases. Hence, the empirical evidences conclude that the RV-based hedges are more useful than the return-based hedges in managing portfolio risk especially during the surge of volatility period.

In addition to statistical evaluations, hedgers may wish to understand the economic gains of a futures hedge using the intraday-based RV approach. As a result, the EV, \( E_n U (\gamma) = \hat{E}_n U (\gamma) \), gives an amount that the hedger would be willing to sacrifice each day to switch from the benchmark strategy to the alternative strategy, where \( \hat{E}_n \) represents the sample average operator (Lence, 1995). Note that the mean–variance utility function \( EU(\gamma) = E (r_{p,t+1} - \gamma) - \gamma \sigma (r_{p,t+1}) \) is specified with the degree of risk aversion \( \gamma > 0 \).15 The advantage of using EV is that it further accounts for the hedger’s risk preference. This study considers four different levels of risk aversion \( \gamma = 1, 3, 7, 10 \) to assess the performance gains across hedgers.16 The results for each model and each period examined are summarized in Table VI.17

Table VI illustrates that the RV-based hedges can substantially outperform the static OLS and/or the return-based dynamic GARCH hedges in terms of EV gains. For short hedges in Period I, the RV-based method generates positive EV gains over the conventional and the OLS methods, whereas the EV of the return-based GARCH method over the OLS is negative. Taking \( \gamma = 1 \) as an example, the average EV of the RV-based hedges surpasses the return-based GARCH (OLS) hedges by about 0.17 (0.07) basis points per day, whereas the average EV gain of the return-based GARCH method over the OLS is about −0.10 basis points per day. For long hedges, however, it is observed that the RV-based method not only underperforms the return-based GARCH method but also loses the static OLS method in Period I. As the expected hedged portfolio returns \( E (r_{p,t+1}) \) for short and long hedges have the same magnitude but with opposite sign, the benefits for short hedging using RV should be harmful

15The utility function is also considered in Kroner and Sultan (1993) and Lien and Yang (2006).
16This specification on risk aversion follows Patton (2004), who considers \( \gamma = 1, 3, 7, 10, 20 \) for asset allocating. In addition, Lien and Yang (2006) assume that the risk aversion to be 4 in measuring the expected utility of a futures hedge.
17Given risk aversion \( \gamma \), the EV of the alternative over the benchmark model is obtained by solving the nonlinear equation: \( E (r_{p,t+1} - \gamma) - \gamma \sigma (r_{p,t+1}) = E (r_{p,t+1} - EV) - \gamma \sigma (r_{p,t+1} - EV) \) with the use of the out-of-sample hedged portfolio returns.
## TABLE VI
Out-of-Sample Comparisons of Hedging Performance: EV Gains

<table>
<thead>
<tr>
<th>Benchmark</th>
<th>Alternative</th>
<th>Short Hedge</th>
<th>Long Hedge</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\gamma = 1$</td>
<td>$\gamma = 3$</td>
<td>$\gamma = 7$</td>
</tr>
<tr>
<td>ECT-GARCH-CCC</td>
<td>ECT-RV-GARCH-CCC</td>
<td>0.1556</td>
<td>0.1572</td>
</tr>
<tr>
<td>ECT-GARCH-DCC</td>
<td>ECT-RV-GARCH-DCC</td>
<td>0.1250</td>
<td>0.1267</td>
</tr>
<tr>
<td>ECT-GJR-CCC</td>
<td>ECT-RV-GJR-CCC</td>
<td>0.2061</td>
<td>0.2067</td>
</tr>
<tr>
<td>ECT-GJR-DCC</td>
<td>ECT-RV-GJR-DCC</td>
<td>0.1754</td>
<td>0.1758</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-RV-GARCH-CCC</td>
<td>0.0230</td>
<td>0.0223</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-RV-GARCH-DCC</td>
<td>0.0371</td>
<td>0.0366</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-RV-GJR-CCC</td>
<td>0.1009</td>
<td>0.1001</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-RV-GJR-DCC</td>
<td>0.1156</td>
<td>0.1148</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-GARCH-CCC</td>
<td>-0.1326</td>
<td>-0.1349</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-GARCH-DCC</td>
<td>-0.0879</td>
<td>-0.0901</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-GJR-CCC</td>
<td>-0.1052</td>
<td>-0.1066</td>
</tr>
<tr>
<td>OLS</td>
<td>ECT-GJR-DCC</td>
<td>-0.0598</td>
<td>-0.0610</td>
</tr>
</tbody>
</table>

### Panel A: Period I (December 19, 2003~September 28, 2007, 950 observations)

### Panel B: Period II (October 1, 2007~March 31, 2009, 378 observations)

Notes. The table shows the basis point fees per day that an hedger with the quadratic utility and the constant relative risk aversion of $\gamma$ would willing to pay to switch the benchmark to the alternative strategies. Note that the effect of transaction costs on the hedging performance is excluded.
to the long hedge when the hedgers have the quadratic utility form. Then examining the performance in Period II, the average EV gain over the conventional method by the RV-based method for long (short) hedges is about 1.35 (−1.24) basis points per day. As compared with the OLS method, it is observed that the ECT-RV-GARCH-based (ECT-RV-GJR-based) models for long (short) hedges can generate positive EV gains in the period. Clearly, a short (long) hedger with the mean–variance utility would prefer using the RV-based method for his/her hedging activity in Period I (II). Moreover, it is evident that the EV gains of the RV-based models differentiate across hedgers with different risk aversions. The EV of the alternative method surpasses the conventional method because it increases as the risk aversion of the hedger increases. That is, a hedger with a higher risk aversion in the S&P 500 market can benefit more when he/she uses the RV-based models in hedging.

Hedge Horizon, Hedge Ratio, and Hedging Effectiveness

As we have discussed the results based on a daily hedging horizon, as individuals and institutions may not have the same hedging horizon for their specific purposes, the RV-based method is further applied to study the effect of hedging horizon on hedge ratio and hedging effectiveness. A few studies have found that hedge ratio depends on the hedging horizon and approaches unity (i.e., naïve hedge ratio) for a longer horizon; and, hedging effectiveness tends to increase as the length of hedging horizon increases (see, for example, Chen, Lee, & Shrestha, 2004; Ederington, 1979; Geppert, 1995; Lien and Shrestha, 2007). It is noted that, however, this result has never been examined empirically using the RV-based and the return-based GARCH methods. Thus, this study analyzes the relationships of the dynamic methods for six hedging horizons: 1-week (1W), 2-week (2W), 3-week (3W), 1-month (1M), 2-month (2M), and 3-month (3M), and the in-sample and out-of-sample results are plotted in Panel (a)–(b) and (c)–(d) of Figure 3, respectively. Panel (a) and (c) show the hedge ratio tends to increase and to approach unity with increase of the length

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18For example, the findings are supported by Ederington (1979), Geppert (1995), and Lien and Shrestha (2007). These studies use the OLS technique, the cointegration method, and the wavelet analysis, respectively, to study the effect of hedging horizon length on the minimum-variance hedge ratio and the hedging effectiveness of Ederington (1979).

19Lien and Shrestha (2007) indicate that there are two ways to incorporate hedging horizon in estimating hedge ratio. One way is to derive an optimal hedge ratio that explicitly depends on hedging horizon based on some models, such as the model of Geppert (1995). The other way is to estimate the hedge ratio by matching the data frequency with the hedging horizon, such as the approach used by Chen et al. (2004). In this study, we use the nonoverlapping approach of Chen et al. (2004) that matches the data frequency to estimate the hedge ratio and the resulting hedging effectiveness. The figures plot the average values of the empirical results based on the conventional and the alternative models mentioned in the previous sections.
of hedging horizon. For the in-sample case, the conventional hedge ratio is likely to exceed the alternative hedge ratio except the 3W and the 1M horizons. For the out-of-sample study, however, the alternative generally has higher hedge ratio estimates but not for the 3W and the 3M cases. In terms of hedging performance, Panel (b) and (d) plot the effect of hedging horizon on the hedging effectiveness as shown by Ederington (1979), which is estimated by calculating the percentage reduction in the variance of the naked spot portfolio. It is apparent that the hedging effectiveness increases with the length of hedging horizon, but the degree of hedging effectiveness does not approach one. For the out-of-sample analysis, the RV-based method generally outperforms the conventional method in terms of the hedging effectiveness for shorter horizons (within 2 weeks), but fail to outperform the conventional method for longer horizons.\textsuperscript{20} As a result, to achieve a better hedging performance, it is suggested

\textsuperscript{20}It should be noted that, however, the sample size used to estimate hedge ratio and hedging effectiveness decreases quickly with hedging horizon length (e.g., there are only 20 out-of-sample estimates for 3M hedging horizon). Hence, the results for longer horizons, such as 2M and 3M, may not be reliable because a lower frequency results in a substantial reduction in the sample size (see, e.g., Lien & Shrestha, 2007).
that hedgers should use more futures contracts for hedging when their hedging horizon is no longer than two weeks.

CONCLUSIONS

This study has proposed a new class of RV-based GARCH models to estimate risk-minimizing hedge ratios and has examined their benefits relative to the return-based GARCH and OLS models. The RV approach, which utilizes finer information in intraday high-frequency data, provides a direct and consistent technique for estimating the latent volatility so that the spot-futures distribution is quite realistic. Hence, it offers us a reliable method for estimating the risk-minimizing hedge ratio. In addition, the RV-based method is also applied to study the effect of hedge horizon on hedge ratio and hedging effectiveness, which has important implications for hedgers with different hedging horizons.

The empirical results show that the conditional variances and correlations estimates (forecasts) and the resulting hedge ratios using this RV approach are different from those generated by conventional models. Obviously, the difference essentially comes from the information sets used in describing the volatility dynamics. As the imperfect volatility proxies in the conventional GARCH models are replaced by the accurate RV estimates, the out-of-sample comparisons indicate that the hedging performance based on the RV-based models can be substantially improved in terms of risk reductions and EV gains as compared with competing return-based models. The results are summarized from the out-of-sample comparisons of both short and long hedgers with different levels of risk aversion using a rollover method, which spans the periods from December 19, 2003 to March 31, 2009. For longer hedging horizons, however, the effectiveness of the RV-based hedge is generally inferior to the return-based GARCH hedge. Finally, it is important to point out that the results exhibited in this study are based on 15-minute intraday prices. The hedging performance should change as the sampling frequency for calculating the RV changes. Finding the optimal sampling frequency for the RV-based hedging method is an interesting area for a further research.

BIBLIOGRAPHY


