Spread Spectrum Multiple-Access with DPSK Modulation and Diversity for Image Transmission over Indoor Radio Multipath Fading Channels

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Abstract—As demand for networked multimedia applications is increasing rapidly, it is important to provide the ubiquitous accessibility for these services in wireless communication environment. Such access allows users to share novel multimedia applications without any geographical restrictions. In this paper, we investigate the application of the well-known antimultipath spread spectrum code-division multiple access (SS-CDMA) techniques to image transmission related to the development of next-generation multimedia wireless local area networks within a building. SS-CDMA is particularly well suited to a subband coding scheme that divides the image information into multiple parallel data streams using an analysis filter bank, each of which is multiplied by its unique spreading code. All the product signals are then transmitted at the same time in the same radio channel, even though the total bandwidth of all the signals may exceed the channel bandwidth. Each received signal is independently recovered at the decoder by multiplying its spreading code and all the recovered subbands are then reassembled by a synthesis filter bank into a close reproduction to the original image. A forward error correction (FEC) scheme based on convolutional codes with interleaving is proposed to minimize the effect of bursty channel errors on the picture quality degradation. Better image quality can be achieved by using the predetection diversity combining in order to combat the indoor multipath distortion. In this paper, the image quality of subband image transmission via SS-CDMA indoor radio channels with differential phase shift keying (DPSK) modulation is evaluated and examined. Simulation results show that the image peak signal-to-noise (PSNR) ratio is inversely related to a logarithmic function of bit error rate when each subband employs equal protection channel coding.

I. INTRODUCTION

The future generation of wireless local area networks (WLAN) [1]–[4] will provide multimedia transport capabilities qualitatively similar to those offered by ISDN wireline networks within homes, offices, and intelligent buildings. The concept of wireless indoor communication networks suggests itself as a replacement for wired multimedia communication networks in order to avoid expensive installation and relocation cost and to provide portability to various pieces of equipment. Furthermore, the use of radio for indoor multimedia communication in home and office automation systems is an attractive proposition. It would free the users from the cords or optical fibers tying them to particular locations within the buildings, thus offering true mobility which is convenient and sometimes even necessary. The deployment of multimedia terminals will support the ever-growing demand for mixed data, voice, and image applications and will be used to connect the portable pen pad and lap-top devices to backbone information resources and computational facilities. The possibility of multimedia service will allow services such as dial-up personal videoconference to any location, image-on-demand services, and portable FC-based applications incorporating with image/voice/data transfer. Image transmission is one of the future potential multimedia services which should be supported with a high wireless transmission bit-rate within a wider allowable bandwidth. Due to limited radio spectrum, however, only a finite number of radio communication channels can be shared by mobile users. As a result, image data should be compressed before transmission in order to efficiently use each radio channel. CCITT recommends the international standard H.261 for video transmission at $p \times 64$ kbps ($p = 1, 2, \ldots, 30$), where the intended applications are videophone and videoconference. Recently, transmission of compressed video signal coded by H.261 over a digital cordless telephone system has been experimented with by N. MacDonald [6]. More recently, transmissions of differential pulse code modulation- (DPCM)-cooded and layered images via radio multipath fading channels with TDMA QAM or quaternary differential phase shift keying (QDPSK) modulation have been investigated by several researchers [1], [2], [7]–[10]. However, to the authors' best knowledge, little work has been done for image transmission by employing the well-known antimultipath spread spectrum techniques except for that reported in [35].

In the existing systems, the spread spectrum is used for packet radio to improve the performance in multipath, to make possible coexistence with other systems, and to provide resistance to intentional interference [3], [4]. In an in-building environment, the use of spread spectrum can reduce the effects of multipath caused by reflections from the walls and, consequently, can increase the mobility of the multimedia terminals within the office or home environment. To further attain the maximum image quality and spectrum efficiency, coded division multiple access (CDMA) techniques incorporating the spread spectrum [15], [16], [27] are used, where a splitting process is required to divide the image information into a large number of independent data streams, each of which is...
transmitted using one of signature (spreading) codes in the
CDMA system, and is then spread to full channel bandwidth.
In other words, higher data rates are achieved by allocating
more than one code to a single image. Moreover, CDMA
allows more than one image to be transmitted and be accessed
simultaneously and dynamically with no waiting time at the
same limited channel bandwidth. This scheme is termed as
a multiple code transmission. Wyrwas et al. [11] proposed
an alternative approach called the multirate CDMA system to
increase the transmission data rates. Meanwhile, in this paper,
we are only interested in the multiple code CDMA systems.

Another advantage of the image transmission via CDMA
indoor fading channels is that the CDMA systems can be in
combination with the well-known asynchronous transfer mode
(ATM) networks for multimedia services [14]. Each CDMA
signature code represents an ATM virtual connection for each
image data stream over the air interface.

The image splitting process adopted here is based on sub-
band coding [15]-[18], which is one of the less complex
coding algorithms. The principle of subband coding is based on
the decomposition of the input image into a number of
narrow bands using an analysis filter bank where each band
is then decimated, coded, and assigned to its unique signature
code separately. In addition to achieving the highest possible
image quality within the narrow radio channel bandwidth and
maximum spectrum utilization, the input image should be
decomposed into a sufficient number of subbands where each
band is spread to full channel bandwidth. After transmission,
each signal sample is then independently recovered at the
receiver by multiplying its code, each with a fixed spreading
factor. These recovered subbands are reassembled by the
synthesis filter bank into a close approximation to the input
image. For dividing the image into subbands, the symmetric
short kernel filters [16]-[18] (SSKF's) are used for filtering.
These filters require a very small number of coefficients and
are necessary to keep the implementation complexity at a
low level. Moreover, since the synchronous carrier recovery
of conventional SS-CDMA system with coherent phase-shift
keying (CPSK) modulation is a difficult task in a multipath
fading environment, it is natural to consider noncoherent
differential PSK (DPSK) as a modulation scheme in the SS-
CDMA systems [24], [25]. In addition, predetection diversity
is employed to combat the multipath fading.

In Section IV, we will discuss the transmission error effects
in the subband image via SS-CDMA indoor fading channels.
Bit errors in an individual subband will generate error con-
tributions at the receiver output within that frequency band.
Since the channel error contributions in different subbands are
expected to be uncorrelated, the total channel error variance
in the recovered image equals the sum of these errors. Moreover,
we will show that the total channel error variance is in
proportion to the bit error rate when the bit error rate is
sufficiently small. This would lead to the image signal-to-noise
ratio (SNR) being inversely related to a logarithmic function of
the bit error rate. Section V shows computer simulations used
to evaluate the image SNR performance of subband image
transmission by CDMA systems with perfect power control
and without power control.

II. TRANSMISSION OF SUBBAND-CODED IMAGES
OVER IN-BUILDING WIRELESS CDMA LAN’S

Indoor wireless LAN’s are drawing a lot of attention be-
cause of their lower cost layout and indoor mobility. A wireless
LAN that is compatible to ethernet has been achieved [1]-[3].
More broad-band and multimedia wireless LAN’s that are
compatible to ATM-based fiber-optic LAN’s will be developed
[11], [34]. In the near future, high mobility portable terminals
in the wireless LAN’s will be integrated and connected to the
broad-band wireline fiber-optic networks. Fig. 1 shows this
concept.

One current trend is to build the main links to the home
automation system of an intelligent building by using the
optical fiber-based ISDN network as a high-speed backbone
LAN at 155.5 MB/s × n (n: integer). Branch lines are created
using the wireless LAN. From Fig. 1, the portable terminals
communicate with the base station via an indoor radio channel.
Associated with each base station is a cell or a coverage area,
which is the region in the building in which a portable terminal
can maintain a dependable link with that base station. In the multiple-access system for image transmission of interest, the system is assumed to multiplex a set of video signals by applying the CDMA techniques to both wireless and wireline networks. For the wireline backbone fiber optic network, optical CDMA allows more than one image from the base stations of their associated buildings, which technically collide with one another, to transmit and be accessed simultaneously and dynamically with no waiting time at the same wavelength [12], [13]. This fiber optic CDMA image multiple access network can provide system throughput exceeding well over 1 Gb/s, which is much greater than that of a traditional spread spectrum CDMA system via a limited and narrow radio channel. Thus, the total performance of a combination of both wireline and wireless CDMA systems will severely deteriorate as their throughput difference increases.

To overcome this difficulty, a multi-code CDMA technique is applied to the image transmission in order to increase its transmission bit rate via the limited radio channels and then reduce the throughput difference. In other words, higher transmission bit rates are achieved by allocating more than one spreading code to each image in order to create more than one virtual transmission channel for that image.

In Fig. 2, there are two possible transmission modes over the indoor radio channel, e.g., forward- and reverse-link transmissions. The forward-link connection represents the base-to-mobile transmission used to support the video-on-demand (VOD) service, and the reverse-link connection is used to provide the call-in or interactive video program and video dial tone (VDT) from each portable terminal to the base station. As shown in Figs. 2 and 3, each field in a video sequence is decomposed into several components (four in Figs. 2 and 3) using a bank of filters (i.e., $H_{ll}(z_1, z_2)$, $H_{hl}(z_1, z_2)$, $H_{hh}(z_1, z_2)$) called the analysis filter bank. The lowest frequency component is a lower resolution version of the original scene, and the high frequency components mostly carry information about the contours, edges, and other finer details. These filtered signals are then downsampled to yield the subband signals. The downsampling following the analysis filter bank reduces the sampling rate of each of the $M$ subband signals to $\frac{1}{\sqrt{2}}$ times the input signal sampling rate. As a result, these filters decompose the signal into $M$ equally spaced subbands at the same time. For the transmission of these subbands at the same time in the same channel, the SS-CDMA multiplexing scheme is particularly well suited to subband coding that divides the image information into multiple parallel data streams, each of which has assigned to it a spreading code in the SS-CDMA system.

Each active subband in the system depicted in Fig. 2 has a unique spreading code which is used for communication to the base station. The base station contains a bank of spread-spectrum transceivers, one for each active subband. For wireless networks, it is possible to use the multi-code CDMA scheme to support higher bit rate video services by increasing the number of spreading codes and their associated decomposed subbands. With a sufficient number of decomposed subbands or streams, a large spreading factor can be used and yet the total signal can fit within the narrow wireless

![Diagram](image-url)
channel bandwidth and also provide the high transmission rate for the fiber optic CDMA network. In other words, an image of rate $M r_0$ is disassembled (de-multiplexed) into $M$ subsequences each of rate $r_0$. Each subsequence is transmitted using one of $M$ spreading codes with a fixed relatively large spreading factor. Thus, the $M$ subsequences can be transmitted at the same time in the same channel, without crosstalk. Each subsequence is independently recovered at the receiver by multiplying by its unique spreading code and integrating over the sequence length. At the receiver, the $M$ received subsequences are then decoded, upsampled, and reassembled (multiplexed) by the synthesis filter bank into a close approximation to the input scene.

In this paper, the focus is on intra-field subband coding, and the exploitation of temporal correlation can be carried out by a 3-D subband system [20], which consists of temporal, horizontal, and vertical filterings. Undoubtedly, the SS-CDMA system can be applied to the 3-D subband system directly. However, the use of intra-field coding is motivated by the goal to keep the decoder cost low. The implementation is relatively simple since frame stores and motion detection/estimation hardware is not required. Each field in the video sequence is represented by using 2-D subband coding [15].

A. Spread Spectrum CDMA Model with DPSK Modulation

The spread spectrum CDMA technique is able to achieve the high transmission bit-rate services of more than one image via the same limited radio band within a building simultaneously. However, the synchronous carrier recovery of the SS-CDMA with BPSK modulation is a difficult task in a multipath fading channel. To resolve the phase ambiguity in the recovery, a differentially encoded PSK (DPSK) is used to encode the binary digit not by the absolute phase of the carrier but by the phase change between successive bits. For $N$ images transmitted at $N$ different positions, each of them is divided into $M$ subband images which have their own spreading $PN$ codes. The transmitting DPSK signal $s_{kj}(t)$ of the $j$th subband of the $k$th image is expressed as

$$s_{kj}(t) = \sqrt{2P} a_k^{(j)}(t)b_k^{(j)}(t)\cos(\omega_c t + \theta_{kj})$$

where $a_k^{(j)}(t)$ and $b_k^{(j)}(t)$ denote a spreading code and a differentially encoded data signal for the $j$th subband of the $k$th image, respectively, $P$ is the signal power, $\theta_{kj}$ is a random phase, uniformly distributed between $0$ and $2\pi$, and $1 \leq j \leq M$, $1 \leq k \leq N$.

$$b_k^{(j)}(t) = \sum_{t=-\infty}^{\infty} b_k^{(j)}(t-\Pi_T(t-iT))$$

$$a_k^{(j)}(t) = \sum_{t=-\infty}^{\infty} a_k^{(j)}(t-\Pi_T(t-iT_c))$$

where $b_k^{(j)} \in \{+1, -1\}$ denotes the differentially encoded bit of subband $j$ of image $k$ in the $i$th time interval, $a_k^{(j)}(t)$ is an infinite random signature code sequence assigned to the $j$th subband of image $k$ with each chip $a_k^{(j)}$ independent and equiprobably distributed on $\{+1, -1\}$, and $\Pi_T(\cdot)$ is the unit pulse function of duration $T$, defined by

$$\Pi_T(t) = \begin{cases} 1, & t \in [0, T) \\ 0, & \text{else.} \end{cases}$$

The duration of each data bit is $T_c$, while the duration of each chip in the spreading code signal is $T_c$. As a result, the number of chips per bit is $N_c = \frac{T}{T_c}$, where $N_c$ is an integer and usually called the length of the spreading sequence. In mathematical sense, the DPSK encoding scheme selects the current encoded bit $b_k^{(j)}$ based on the information bit $d_k^{(j)}$ and the previous encoded bit $b_k^{(j)}_{i-1}$ according to the logic function

$$b_k^{(j)}_{i} = d_k^{(j)} \oplus b_k^{(j)}_{i-1}$$

where $\oplus$ represents the exclusive OR operation.
B. Statistical Channel Impulse Response Models for Indoor Radio Channels

The multipath fading indoor channels are assumed to be discrete and time-invariant with channel impulse response for the jth subband of the kth image given by [3], [5], [19], [24]

\[ h_{kj}(t) = \sum_{\tau_{kj}} \beta_{kj}(t - \tau_{kj}) e^{j\phi_{kj}} \]  

where \( \beta_{kj} \) is the lth Rayleigh distributed random path gain, \( \phi_{kj} \) is the lth random path phase, uniformly distributed between zero and \( 2\pi \), and \( \tau_{kj} \) is the lth uniformly distributed random delay ranging from zero to one data bit period, \( T \).

The multipath fading indoor channels are assumed to be virtually time-invariant random variables which do not vary significantly over two consecutive bit intervals. In addition, it should be mentioned that these channel parameters vary with the transmitter-receiver distance. For example, the mean amplitude of each path gain is generated from a log-normal distribution which depends on the distance. Therefore, it could be concluded that \( \beta_{kj} = \beta_{k1} = \beta_{k}, \tau_{kj} = \tau_{k1} = \tau_{k}, \phi_{kj} = \phi_{k1} = \phi_{k} \).

In a typical indoor radio channel, utilizing the FEC allocated 25 MHz bandwidth \( (T_c = 40 \text{ ns}) \), the number of paths for different multipath delay spreads are \( L_{km} = 1 \) for \( T_m = 25 \text{ ns} \), \( L_{km} = 4 \) for \( T_m = 150 \text{ ns} \). Generally, the number of paths, \( L_k \) is a random variable which varies uniformly between unity and the maximum value given in (7). Recently, a ray cluster model of the indoor radio channel, which fits measurements well, has been suggested [19]. In this model, the received signals arrive in cluster.

C. DPSK Demodulation with Predetection Diversity

The effect of transmitting \( M \times N \) subbands is as if there were \( MN \) users to be transmitted. A receiver consisting of \( M \) DPSK SS-CDMA demodulators may be used to recover a desired image where each demodulator is trying to match its corresponding subband belonging to that image. The \( M \) recovered subbands are then upsampled and reassembled by synthesis filters into a close approximation to the desired image. However, to combat the multipath fading distortion and achieve better performance, a receiver with diversity combining is needed [24], [25], [29].

The commonly-used diversity combining techniques are selection diversity and predetection diversity. In this paper, we consider the predetection diversity. Predetection diversity for coherent PSK reception is called the maximal ratio combining (MRC). However, it should have perfect knowledge of the path gains and phases in the indoor radio channels. Unlike coherent PSK with MRC, DPSK with predetection combining can be implemented without estimation of the path gains and delays; it is required only that the phases of the Rayleigh-fading components do not change over the duration of two adjacent bits (slow fading). The predetection diversity for DPSK is also called equal gain combining (EGC). The predetection diversity is obtained either by using multiple antennas, or by resolving multipath, or both. Diversity obtained from resolving multipath is called spread-spectrum diversity or inherent diversity, while that obtained from multiple antennas is called antenna or external diversity. Fig. 4 for predetection combining shows only spread-spectrum diversity since this is the simplest to implement. The receiver contains a filter matched to the spreading code waveform of the reference user, followed by a DPSK demodulator and an integrator acting as an EGC diversity circuit. The demodulated signal is integrated prior to detection over a time interval whose length depends on the delay spread.

The received signal at the input to the matched-filter in the receiver is given by

\[ r(t) = Re \left\{ \sum_{k=1}^{N} \sum_{j=1}^{M} \int_{-\infty}^{\infty} h_{kj}(\tau) \delta_{kj}(t - \tau) e^{j\omega_c t} d\tau \right\} + n(t) \]
\[
N_M L_{kj} = \text{real component of number, and } n(t) \text{ is a white Gaussian noise with two-sided power spectral density } N_0/2.
\]

For simplified analysis, the first subband of the first image is chosen as the reference user for calculating the probability of error of its data symbol \( b_{kj}^{(1)} \). The receiver is able to coherently recover the carrier phase \( \phi_{k1} \) and \( \tau_{k1} \) locking to the ith path as a reference path between the transmitter of reference subband and its corresponding receiver [24]. All other paths constitute interference. That is, we assume without loss of generality that \( \phi_{k1} = 0 \) and \( \tau_{k1} = 0 \). According to the concept of Kavehed and Ramamurthi [24], the complex envelope of the matched-filter output at the sampling instant \( t = T \) is denoted by \( z_0 \) and can be expressed as a form in terms of \( b_{k-1}^{(j)} \) and \( b_{k,0}^{(j)} \):

\[
z_0 = F(b_{k-1}^{(j)}, b_{k,0}^{(j)}; 1 \leq j \leq M, 1 \leq k \leq N) + (\eta_0 + j\nu_0)
\]

\[
\beta_{11} \sqrt{\frac{P_T}{2}} \sum_{l=1}^{L_{11}} + \sqrt{\frac{P}{2}} \sum_{l=1}^{L_{11}} \sum_{j=2}^{M} \sum_{l=1}^{L_{1j}} \left\{ \right. \\
\times \beta_{11} \cos(\psi_{11}) \\
\times b_{k-1}^{(j)} R_{k,11}^{(j)}(\tau_{11}) + b_{k,0}^{(j)} R_{k,11}^{(j)}(\tau_{11}) \\
+ j\beta_{11} \sin(\psi_{11}) \\
\times b_{k-1}^{(j)} R_{k,11}^{(j)}(\tau_{11}) + b_{k,0}^{(j)} R_{k,11}^{(j)}(\tau_{11}) \\
+ \left. \right\} \\
+ \sqrt{\frac{P}{2}} \sum_{k=2}^{M} \sum_{j=1}^{L_{1j}} \sum_{l=1}^{L_{11}} \left\{ \right. \\
\times \beta_{1j} \cos(\psi_{1j}) \\
\times b_{k-1}^{(j)} R_{k,1j}^{(j)}(\tau_{1j}) + b_{k,0}^{(j)} R_{k,1j}^{(j)}(\tau_{1j}) \\
+ j\beta_{1j} \sin(\psi_{1j}) \\
\times b_{k-1}^{(j)} R_{k,1j}^{(j)}(\tau_{1j}) + b_{k,0}^{(j)} R_{k,1j}^{(j)}(\tau_{1j}) \\
+ \left. \right\} \\
+ \sqrt{\frac{P}{2}} \sum_{k=1}^{M} \sum_{j=1}^{L_{11}} \sum_{l=1}^{L_{1j}} \left\{ \right. \\
\times \beta_{kj} \cos(\psi_{kj}) \\
\times b_{k-1}^{(j)} R_{k,j}^{(j)}(\tau_{kj}) + b_{k,0}^{(j)} R_{k,j}^{(j)}(\tau_{kj}) \\
+ j\beta_{kj} \sin(\psi_{kj}) \\
\times b_{k-1}^{(j)} R_{k,j}^{(j)}(\tau_{kj}) + b_{k,0}^{(j)} R_{k,j}^{(j)}(\tau_{kj}) \\
+ \left. \right\} \\
+ (\eta_0 + j\nu_0)
\]

where \( b_{k-1}^{(j)} \) and \( b_{k,0}^{(j)} \) are the previous and current data bit for the jth subband of the kth image, respectively, and \( F(\cdot) \) denotes the first four terms of (9) and is a function of a set of data bits, \( b_{k-1}^{(j)} \) and \( b_{k,0}^{(j)}; 1 \leq j \leq M, 1 \leq k \leq N \).

In (9), \( R_{k,j1}^{(1)}(\tau) \) and \( R_{k,j1}^{(1)}(\tau) \) are the well known continuous time partial cross-correlation functions of the regenerated code, \( a_{1,j}^{(1)}(t) \), and a delayed version of the interfering codes, \( a_{k,j}^{(1)}(t - \tau) \). They are defined as

\[
R_{k,j1}^{(1)}(\tau) = \int_{0}^{T} a_{k,j}^{(1)}(t) a_{1,j}^{(1)}(t - \tau) dt
\]

The noise samples \( \eta_0 \) and \( \nu_0 \) are independent, zero-mean Gaussian random variables with identical variances \( \sigma^2 (= N_0 T) \) and given as

\[
\eta_0 = \int_{0}^{T} a_{1,j}^{(1)}(s) n_k(s) ds
\]

\[
\nu_0 = \int_{0}^{T} a_{1,j}^{(1)}(s) n_q(s) ds
\]

where \( n_k(t) \) and \( n_q(t) \) are the in-phase and the quadrature components of \( n(t) \), respectively. Since the fading of indoor radio channel is slow compared to the data rate, the corresponding complex envelope at the previous sampling instant, denoted by \( z_{-1} \), differs from \( z_0 \) only in the data bits, and in the additive Gaussian noise samples. Hence, \( z_{-1} \) has the same expression as that of \( z_0 \) but involves a set of data bits and Gaussian noise samples at the previous sampling point and is given by

\[
z_{-1} = F(b_{k-1}^{(j)}, b_{k,0}^{(j)}; 1 \leq j \leq M, 1 \leq k \leq N) + (\eta_{-1} + j\nu_{-1}).
\]

Therefore, the output of the DPSK demodulator at the sampling instant is written as

\[
\xi = \text{Re}\{z_0 z_{-1}^*\}
\]

where * denotes complex conjugate. When there is no diversity, \( \xi \) is the decision variable. The estimate \( \hat{b}_{1,0}^{(1)} \) of the data bit \( b_{1,0}^{(1)} \) is determined based on the hard decision value

\[
\hat{b}_{1,0}^{(1)} = \begin{cases} 1, & \xi \geq 0 \\ -1, & \xi < 0 \end{cases}
\]

A bit error occurs if \( \hat{b}_{1,0}^{(1)} \neq b_{1,0}^{(1)} \).

In (9), the first term represents the desired subband to be detected and it has average power, \( (\beta_{kj}^2 P)^2/2 \), for a fixed \( \beta_{kj} \). The second term is called the interpath interference or self-interference induced by the desired subband on itself because of multipath and the sidelobes of the autocorrelation function of the spreading code of reference subband. The interuser interference for the desired subband can be divided into two parts. The third term in (9) is the first part, called the intra-image interference, which is generated from the \( L_{12} + L_{13} + \ldots + L_{1M} \) inter-subbands in the same image corresponding to the desired subband. The fourth term in (9) is the second part, called the inter-image interference, which is generated from the \( \{L_{21} + \ldots + L_{2M} + L_{31} + \ldots + L_{3M} + \ldots + L_{NM}\} \) subbands in the \( (N - 1) \) inter-images. Finally, \( \eta_0 + j\nu_0 \) is an additive complexed-valued Gaussian noise with...
zero mean and variance $\frac{N_0 T}{4}$. Note that all the interference terms can also come from the preceding bit, $b_{k-1}$, in addition to the current bit, $b_{k}^{(j)}$.

From the above discussion, it is clear that each additional path adds extra interference to the reference user. If there are $(K - 1)$ interfering users, each of whose signals arrive via $L$ paths, the effect is as if there were $(K - 1)L$ interfering users. However, the total number of interference terms should be $N_I = (K - 1)L + L - 1$ when the reference user is also transmitted via $L$ paths to create $(L - 1)$ self-interference terms. For the subband coded images, the total number of interference terms to a reference subband is $N_I = MNL - 1$ when $L_kj = L$ for $1 \leq k \leq N$ and $1 \leq j \leq M$.

With predetection combining diversity of order $M_d$, the new decision variable is the weighted sum of $M_d$ DPSK demodulator outputs resulted from the $M_d$ diversity channels or combined paths. We refer to the $M_d$ paths involved in the combining as the combined paths. The weights are taken equal to the corresponding complex-valued channel gain $\beta_{kj}\exp(-jk\pi_k)$. The effect of this multiplication is to compensate for the phase shift in the channel and to weigh the signal by a factor that is proportional to the signal strength. A reason for using DPSK is that the time variations in the channel parameters are sufficiently slow so that the channel phase shifts ($\gamma_{hk}$) do not change appreciably over two consecutive signaling intervals (DPSK detection). Hence, the channel parameters $\{\beta_{kj}\exp(-jk\pi_k)\}$ are assumed to remain constant over two successive signaling intervals. Under that condition, the DPSK with predetection combining can be implemented without estimation of the channel parameters. This predetection combining scheme is also called the equal gain combining (EGC). In practice, its decision variable, $\xi_{\text{EGC}}$, is obtained by sampling the DPSK demodulated signal at the appropriate instants within a specific time interval and adding the samples. The EGC decision variable, $\xi_{\text{EGC}}$, is thus written as

$$
\xi_{\text{EGC}} = \sum_{m=1}^{M_d} \xi_m = \sum_{m=1}^{M_d} \text{Re}\{z_{m,0}z_{m,1}^*\}
= \text{Re}\left\{ \sum_{m=1}^{M_d} \left[ \sqrt{\frac{PT^2}{2}} \beta_{m1}b_{m1}^{(1)} + I_{0,m} + (\gamma_{0,m} + j\nu_{0,m}) \right] \cdot \left[ \sqrt{\frac{PT^2}{2}} \beta_{m1}b_{m1}^{(1)} + I_{-1,m} + (\gamma_{-1,m} + j\nu_{-1,m}) \right]^* \right\}
$$

(15)

where $\xi_m$ is the DPSK demodulated signal at the $m$th sampling instant corresponding to the $m$th diversity channel or combined path. $I_{0,m}$ and $I_{-1,m}$ denote the total interferences to the desired data bits $b_{k,j}^{(0)}$ and $b_{k,j}^{(1)}$ at the $m$th sampling point respectively, and $(\gamma_{0,m} + j\nu_{0,m})$ are the complex-valued additive white Gaussian noise (AWGN) noises at the $m$th sampling point for $b_{k,j}^{(j)}$, $i = -1, 0$. The above diversity scheme is termed as an EGC time diversity where each time slot represents a diversity channel. The structure of an equal-gain combining DPSK receiver is shown in Fig. 5, where the number of branches (or the number of combined paths), $M_d$, is a parameter less than or equal to $(L_1/2)$.

Eng and Milstein [25] showed that the branch spacing of diversity is $2T_c$ (instead of $T_c$ as for the coherent PSK receiver) because the matched filter response to adjacent paths is correlated and are uncorrelated for nonadjacent paths. Therefore, to maximize the benefits of diversity for a given number of branches, only every other path is combined. In (15), $\xi_m$ corresponds to the $m$th branch of the receiver. The sampling times of the receiver are $(i + 1)T + 2(M_d - 1)T_c$, where $i$ represents the time index of data bits. For example, to detect the zeroth data bit $b_{k,j}^{(0)}$, the sampling time would be $T + 2(M_d - 1)T_c$; the "$T$" term is the usually matched filter sampling time and the "$(2(M_d - 1)T_c$) term is from the combining of $(M_d - 1)$ additional combined paths. By using multiple antennas, the highest possible order of diversity can be increased to $(M_d)_{\text{MAX}} = L_{\text{ant}} \cdot (L_1/2)$ where $L_{\text{ant}}$ is the number of antennas. Moreover, in a practical implementation, the decision variable $\xi_{\text{EGC}}$ is approximated by integrating the DPSK demodulator output over an interval with a duration of $(2(M_d - 1)T_c)$, thereby replacing a sum of samples by a continuous-time integration. This approximation avoids the need for the time-synchronization to each of the different path signals of the reference subband (user). A hard decision is made on $\xi_{\text{EGC}}$ in order to detect $b_k^{(j)}$.

D. Average Bit Error Probability

For the simplified derivation of the bit error probability, the Gaussian assumption is to take all the self-interference, intra-image interference, and inter-image interference terms as Gaussian noise. To calculate the total power of the interference terms, one should evaluate a term like

$$
\kappa^2 = \frac{\sum_{k=1}^{M_d} \sum_{j=1}^{L_1} \left| b_{k,j-1}^{(j)}R_{k,j-1}(\gamma_{k,j}) + b_{k,j}^{(0)}\hat{R}_{k,j-1}(\gamma_{k,j}) \right|^2}{T^2}
$$

(16)

where $b_{k,j-1}^{(j)}$ and $b_{k,j}^{(0)}$ are independent bipolar random variables. Pursley [26] showed that $\kappa^2$ is a constant which has the value $2/3N_c$. Since the interference terms in (9) are all mutually independent, the total interference power becomes

$$
P_{\text{int}} = \text{interference power} = \text{Re}\{I'I\}
= \frac{PT^2}{4}\kappa^2 \left\{ \sum_{j=2}^{M_d} \sum_{i=1}^{L_1} \beta_{k,j}^{(i)} \right\}
+ \sum_{j=2}^{M_d} \sum_{i=1}^{L_1} \sum_{k=2}^{M_d} \sum_{j=1}^{L_1} \sum_{i=1}^{L_1} \beta_{k,j}^{(i)}^* \beta_{k,j}^{(i)}
$$

(17)

where $I$ is the total interference to the desired bit $b_k^{(j)}$ and contains the second, third, and fourth terms of (9). It is shown in II-B that $b_{k,j}^{(j)} = \beta_{k,j} = \beta_k$ and $L_{k,j} = L_{k,1} = L_k$ for $1 \leq j \leq M$ and $1 \leq k \leq N$. Furthermore, assume that the path gains for all the subbands in the same image are independently identically distributed (i.i.d.) random variables.
Fig. 5. Equal-gain combining DPSK receiver.

Thus, $E(\beta_{E_b}) = E(\beta_{E_b}^2) = E(\beta_{E_b}^2) = \beta_{E_b}^2$. Then, (17) becomes

$$P_{\text{int}} = \frac{Tr^2}{4} \left\{ (M\bar{L}_1 - 1)E_b + M \left( \sum_{k=2}^{N} \bar{L}_k E_{b,k} \right) \right\}$$

(18)

where $\bar{L}_k$ denotes the average number of paths for each subband in the $k$th image, $E_b = PT$ represents the signal energy per bit, $E_{b,k} = \beta_{E_b}^2 E_b$ and $E_{b,k} = \beta_{E_b}^2 E_b$ for $2 \leq k \leq N$.

Similarly, the received signal power is found to be $\frac{TE_b^2}{2}$ when $\beta_1$ is a random variable. Thus, the average value of half the signal-to-noise plus interference power ratio becomes

$$\gamma_b = \frac{E_b}{\kappa^2 \left( (M\bar{L}_1 - 1)E_b + M \left( \sum_{k=2}^{N} \bar{L}_k E_{b,k} \right) \right) + N_0}$$

(19)

At a reference receiver, the received power from the nearer transmitter can be much bigger than that of the farther transmitter. This is called the near-far problem. Ideally, the received signals are intended to be received with equal power but actually have different power when received. A number of power control mechanisms [27], [28] are trying to compensate for the difference and then keep the received average powers almost equal. This is equivalent to placing all the images on an equidistance contour around the reference receiver. Thus, all the path gains $\beta_n$'s become i.i.d. random variables. Therefore, after applying a perfect power control to the SS-CDMA system, each image would contribute the identical received power per bit, i.e., $E_{b,k} = E_b$ for $1 \leq k \leq N$. Moreover, $E_{b,k}$, $1 \leq k \leq N$ are assumed to be identical and equal to $L$. Thus, for a large $MN/L$, $\gamma_b$ would become

$$\gamma_b = \frac{E_b}{MN \bar{L}^2 E_b + N_0} = \frac{E_b}{(2MN \bar{L}E_b/3N_c) + N_0}$$

(20)

Moreover, for the application of video telephone, the interference term can be reduced by a factor of $8/3$ because the video activity factor of video telephone would be often equal to its associated voice activity factor ($= 3/8$) [27] during the video telephone conversations. Thus with video and voice activity monitoring, $\gamma_b$ is increased relative to (20), and becomes

$$\gamma_b = \frac{E_b}{(3/8) \cdot (MNL\bar{L}^2 E_b) + N_0} = \frac{E_b}{(MNL E_b/4N_c) + N_0}$$

(21)

Proakis [29] showed that the average bit error rate (BER) for the binary DPSK can be expressed as a form in terms of $\gamma_b$ and is given by

$$p_e = p(\gamma_b) = \frac{1}{2 \gamma_b + 1}$$

(22)

When predetection diversity of order $M_d$ is used, it can be shown [29] that the bit error rate for the DPSK with EGC combining is written as

$$p_e = \frac{1}{2^{2M_d-1}((M_d - 1)!)(1 + \gamma_c)M_d} \times \sum_{i=0}^{M_d-1} b_i (M_d - 1 + i) \left( \frac{\gamma_c}{1 + \gamma_c} \right)^i$$

(23)

where

$$b_i = \frac{1}{i!} \sum_{n=0}^{M_d-1-i} \left( \frac{2M_d - 1}{n} \right)$$

(24)

In (23), the quantity $\gamma_c$ is the average signal-to-noise ratio per combined path, with the sum of interference and Gaussian noise. It can be shown that the value of $\gamma_c$ may be identical to either (20) or (21) and is given by

$$\gamma_c = \left\{ \begin{array}{ll} \frac{E_b}{(2\alpha MNL E_b/3N_c) + N_0} & \text{for general video applications} \\ \frac{E_b}{(MNL E_b/4N_c) + N_0} & \text{for video telephone} \end{array} \right.$$  

(25)

where $\alpha$ is a video activity factor of a specific video application. For $\gamma_c \gg 1$, the bit error probability in (23) can be approximated by the expression

$$p_e \cong \left( \frac{1}{2\gamma_c} \right)^{M_d} \left( \frac{2M_d - 1}{M_d} \right)$$

(26)
III. LOW-COMPLEXITY SUBBAND CODING USING 
SEPARABLE EXACT RECONSTRUCTION FILTER BANKS 

The most computationally efficient approach to splitting and 
merging subband images results from using separable filters. 
The separable subband decomposition is performed in two 
stages using 1-D filters that process the data along the rows 
and columns of the image data array. The input signal \( x \) is 
first applied to horizontal filters \( H_X(z_1) \) (lowpass) and \( H_H(z_1) \) 
(highpass), and horizontally downsampled to get the signals \( x_1 \) 
and \( x_h \), respectively. In the second stage of the decomposition, 
each of the signals \( x_1 \) and \( x_h \) is applied to the two vertical 
filters \( H_Y(z_2) \) (lowpass) and \( H_H(z_2) \) (highpass), and vertically 
downsampled to get the subband signals \( x_1h, x_1h, x_hh, \) and \( x_hh \). 

For the purpose of reconstruction, the signals are merged by 
upsampling and filtering using the synthesis filters. The vertical 
synthesis filters are denoted by \( G_Y(z_2) \) (lowpass) and \( G_H(z_2) \) 
(highpass), and the horizontal synthesis filters are denoted by 
\( G_Y(z_1) \) (lowpass) and \( G_H(z_1) \) (highpass).

According to the separability characteristics of \( H_{xy}(z_1, z_2) \) 
and \( G_{xy}(z_1, z_2) \), the 2-D filtering can be implemented as a 
product of 1-D filtering operations \[15\]

\[
\begin{align*}
H_{xy}(z_1, z_2) &= H_X(z_1) H_Y(z_2) \\
G_{xy}(z_1, z_2) &= G_Y(z_2) G_Y(z_2)
\end{align*}
\]

where \( x \) and \( y \) denote \( i \) (lowpass) or \( h \) (highpass).

Moreover, it is shown that the 2-D exact reconstruction 
filters for \( H_{xy}(z_1, z_2) \) and \( G_{xy}(z_1, z_2) \) can be developed in terms 
of 1-D exact reconstruction filters. In designing 1-D 
exact reconstruction filters, we should focus on an analysis into 
a two-channel system. The analysis filter bank splits the input 
signal into two-channel signals by processing it with a lowpass 
filter \( H_L(z) \) in one path and with a highpass filter \( H_H(z) \) in 
the other. The filtered signals \( u_2 \) and \( u_1 \) are downsampled 
by a factor of two to obtain the subband signals \( x_1 \) and \( x_h \). 

In a back-to-back connection, these signals are upsampled and 
processed by the synthesis filters with transfer functions \( G_Y(z) \) 
and \( G_H(z) \). In other words, every second sample has been 
discarded by the downsampling and has been reinserted as a 
zero-valued sample by the upsampling. The aliasing distortion 
in the reconstruction can be removed if the synthesis filters 
are defined as 

\[
\left\{ 
\begin{align*}
G_Y(z) &= H_H(-z) \\
G_H(z) &= -H_L(-z)
\end{align*}
\right.
\]

Quadrature mirror filters \[21\] (QMF's) have been proposed 
and widely used as analysis and synthesis filters in subband 
coding of images. However, \[18\] showed that QMF’s do not 
permit reconstruction to be exact, although the reconstruction 
error can be made very small by using long tap filters. For 
video and digital image applications, use of such long tap 
filters, while not providing any significant coding gain, may 
increase the hardware complexity. Since the processing of 
video signals in wireless channels involves high sampling 
rates, it is very desirable to keep the filter bank complexity 
low. SSKF’s have been considered as the low-complexity 
subband decomposition and reconstruction filter pairs because 
of the simplicity in implementation \[17\]. The SSKF’s are

the symmetric short filters which are obtained by factoring 
a product filter, \( F(z) = H_H(z) H_L(-z) \) into linear phase 
components. Le Gall et al. \[17\] showed an example of the 
lowpass and highpass analysis filters given by

\[
\left\{ 
\begin{align*}
H_L(z) &= \frac{1}{2}(-1 + 3z^{-1} + 3z^{-2} - z^{-3}) \\
H_H(z) &= \frac{1}{2}(1 - 3z^{-1} + 3z^{-2} - z^{-3})
\end{align*}
\right.
\]

The four-tap filters of \(30\) are implementable using a small 
number of shift and add operations. The use of general multi-
multipliers is avoided. This leads to a simple and computationally 
efficient subband coding implementation. These filters are able 
to decompose the signal into two equally spaced subbands at a 
time, and produce visually pleasant and smooth outputs. Note 
that the decomposition of the input image can be extended to 
more than four bands by repeating the separability process to 
each subband image in a tree-structured manner. An alternative 
method of dividing a signal into a number of equally spaced 
subbands is the generalized quadrature mirror filters (GQMF's) \[5\].

A. PCM/DPCM Coding of Subband Signals 

To achieve maximum compression with high image fidelity, 
the subbands have to be encoded on a perceptual basis by 
following proper coding strategy. The subband signal carrying 
the lowest frequency information usually has a high degree 
of spatial correlation that is suitable for coding using either 
predictive techniques such as DPCM or transform coding 
using discrete cosine transform \[16\], \[22\]. Since the baseband 
contains the most information, this band is quantized as 
accurately as possible. The high frequency subbands contain 
edge and contour information. These subband signals can 
be directly quantized by coarse quantizers since the noise 
produced by quantizing higher bands with a few levels can 
easily be tolerated by the human eye and then PCM encoded 
in the spatial domain. A large fraction of the quantized data in 
the high frequency band signals consists of zero samples and 
these signals are therefore well suited for runlength encoding.

The baseband has a histogram that is similar to the original 
image with high pixel-to-pixel correlation. Due to this high 
correlation, the DPCM encoder is chosen to code the subband. 
The pixel configuration for the 2-D prediction is shown in 
Fig. 6. The predicted value is given by

\[
\hat{x}_A = b x_B + c x_C + d x_D
\]

where \( x_B, x_C, \) and \( x_D \) are previously reconstructed pixels, 
and \( x_A \) is the prediction of the present pixel. The weighting 
factors, \( b, c, \) and \( d \) are chosen to be 0.3, 0.25, and 0.25, 
respectively. The prediction error signal is quantized by a 
symmetric nonuniform quantizer.

An optimal approach in the minimum mean square sense is to 
design a quantizer which matches the probability density 
function of the input signals (close to generalized Gaussian or 
Laplacian probability density function). This optimal quantizer 
is known as Lloyd–Max quantizer. However, Gharavi and 
Tabatabai \[16\] showed that such a quantizer is not suitable for 
encoding the higher frequency band signals. This is mainly 
due to the existence of picture noise which manifests itself as a
low level signal within these bands, and would result in a fine quantization of the noise. To circumvent this problem, they proposed a highly efficient nonuniform symmetric quantizers with a center dead zone, \( d \), to quantize the high bands. The dead zone is used to eliminate the picture noise. The input values in the active region are then uniformly quantized to \( L \) levels. Moreover, it contains a saturation value, \( Y \), for signals whose magnitude are above a given threshold, \( t \). Meanwhile, the quantized high bands are observed to have a large number of connected areas of zeros. Therefore, run-length coding techniques are implemented as 1-D codes for this purpose. In order to achieve a higher compression ratio, Le Gall et al. [17] extended the above method by using arithmetic coding in combination with DPCM coding of lower band and PCM coding of higher band signals.

When aiming for a constant bit rate for each subband via the SS-CDMA system, it is convenient to assume that each subband is encoded into a constant number of bits and its output rate is monitored on a line-by-line basis. The instantaneous bit rate of the specific line being encoded is compared against its targeted rate, and its dead zone is appropriately increased, decreased, or maintained. In addition, a buffer is used to smooth out the variations in the rate. Then the bit rate is kept constant for each subband. More details about the bit rate control can be found in [22].

B. Error Protection Strategies

Among various forward error correction (FEC) schemes, the convolutional code with interleaving is one of the useful codes for correcting both bursty and random errors in the SS-CDMA multipath fading channels. Decoding algorithms play an essential role in the performance of a convolutional code. The well-known Viterbi algorithm is an effective maximum likelihood decoding algorithm for convolutional codes. We consider a SS-CDMA system in which a convolutional encoder with a code rate \( R_c \) is used in conjunction with hard decision Viterbi decoding. Although it is possible to obtain better performance with soft-decisions, hard-decision decoding is commonly used in wireless communications because it is simpler to implement. Moreover, Lin and Costello [23] addressed the problem of constructing good codes for use with the Viterbi algorithm. Once the desired code rate has been selected, the bit error probability is minimized when the free distance of the code, \( d_{\text{free}} \), is chosen as large as possible. One of the good codes is a binary (2, 1, 6) code which has \( R_c = \frac{1}{2} \), \( d_{\text{free}} = 10 \) and asymptotic coding gain of 3.98 dB. In this paper, we used the convolutional codes to improve the BER performance shown in (23). Reference [29] indicated that there is no exact closed form for the BER of the DPSK receiver with convolutional codes and equal-gain combining diversity for Rayleigh fading channels. However, its BER is upperbounded by the expression

\[
p_e \leq \Phi(\gamma_{\text{code}}, d_{\text{free}}) \tag{32}
\]

where \( \gamma_{\text{code}} = R_c \gamma_c \). Note that the expression of \( \Phi(\cdot) \) depends on the types of diversity combining decoding, i.e., hard-decision or soft-decision decoding.

IV. IMAGE QUALITY EVALUATION FOR CDMA SUBBAND IMAGE TRANSMISSION VIA INDOOR FADING CHANNELS

As discussed in Section III, there are two encoding techniques for subband images. The baseband is encoded using DPCM, and higher bands are PCM encoded. Usually the reconstructed output signal \( y(n) \) includes an input signal, \( x(n) \), and the effects of both quantization error, \( q(n) \), and total CDMA interference and noise, \( e(n) \). The total reconstruction error variance for the PCM encoding is defined by

\[
\sigma_{\text{PCM}}^2 = E[(x - y)^2] \tag{33}
\]

where \( x \) is the input signal and \( y \) is the reconstructed output signal.

R. Steele et al. [9] showed that the \( \sigma_{\text{PCM}}^2 \) can be written as

\[
\sigma_{\text{PCM}}^2 = \sigma_{\text{Q}}^2 + \sigma_{\text{M}}^2 + \sigma_{\text{C}}^2 \tag{34}
\]

where \( \sigma_{\text{Q}}^2 \) represents the quantization error variance, \( \sigma_{\text{C}}^2 \) is the mean-square error contribution due solely to channel errors, and finally, the quantity \( \sigma_{\text{M}}^2 \) represents a mutual error term. They also found that the transmission error variance in companded PCM over Rayleigh fading channels when the PCM bit stream is scrambled (or interleaved) prior to its transmission can be expressed in terms of the bit error probability, \( p_e \), and is given by

\[
\sigma_{\text{PCM}}^2 = \sum_{j=1}^{R} T_j p_e \tag{35}
\]

where \( R \) is the number of bits used to represent the quantizer output. The term \( T_j \) is

\[
T_j = \sum_{i=1}^{j} S_i \left( R - i \right) (-1)^{j-i} \quad j = 1, 2, \ldots, R \tag{36}
\]
and the quantity $S_i$ is given in [9]. Note that by the process of interleaving, the burst errors that occur in Rayleigh fading channels are randomized because bursty bit errors are much more difficult to correct than random bit errors.

Jayant and Noll [30] showed, moreover, that the cross-correlation between quantization and channel errors is nearly equal to zero if the quantizer characteristics are close to that of an optimum quantizer. Thus, $\sigma_{m,PCM} = 0$. However, for simplified analysis, they also proposed an alternative formulation which is quite similar to Steele et al.'s expression and can be written as

$$\sigma^2_{e,PCM} = \epsilon^2_e \cdot \sigma^2_x$$

(37)

and

$$\epsilon^2_e = \sum_{j=1}^{B} \zeta_j p_{e,j}$$

(38)

where $\epsilon^2_e$ is called the channel performance factor, and $\zeta_j$ are channel coefficients that reflect the effects on $\sigma^2_e$ of the quantizer characteristics, the chosen binary code and the source statistics. For example, $\zeta_1 = 2.55, \zeta_2 = 4.97, \zeta_3 = 6.91$ when natural binary code is chosen and a nonuniform quantizer is used. The bit error probability for CDMA indoor fading channel without or with convolutional channel coding is shown in Section II. Here, we would apply Jayant and Noll's formulation to the image quality analysis via CDMA channels.

From (34) and (37), it yields

$$\sigma^2_{e,PCM} = (\zeta_{0,PCM}^2 + \epsilon^2_e) \sigma^2_x$$

(39)

where $\epsilon^2_{0,PCM}$ is the PCM quantizer performance factor whose quantizer characteristics are close to that of an optimum quantizer.

### A. Transmission Errors in DPCM over CDMA Fading Channels

The performance analysis of 2-D DPCM image transmission over fading channels was first discussed in [10] by Daut and Modestino who showed that the total reconstruction error variance of the DPCM image based on a 2-D separable second order Gauss–Markov autoregressive (AR) random field model in the presence of fading bursty and AWGN random channel errors can be expressed as the sum of three separate components

$$\sigma^2_{DPCM} = \sigma^2_{e,PCM} + \sigma^2_{m,DPCM} + \epsilon^2_{DPCM}$$

(40)

where $\sigma^2_e$ is the prediction error variance, $\epsilon^2_{DPCM}$ and $\epsilon^2_{m,DPCM}$ denote the DPCM quantizer and channel performance factors respectively, and $\sigma^2_{m,DPCM}$ represents the normalized mutual error term. By the assumption of equal bit error rate for each bit in the R-bit quantizer, in (40), the DPCM channel performance factor can be written as

$$\epsilon^2_{DPCM} = \frac{\Delta^2 p_e}{(1 - \rho^2_1)(1 - \rho^2_2)}$$

where $L$ is the number of quantization levels, $\Delta$ is the normalized step size for optimum uniform quantizer, $\zeta_j$ is the $j$th DPCM channel coefficient, $p_1$ denotes the probability that the input signal falls in the $i$th quantization interval, and $\rho_1$ and $\rho_2$ are the correlation coefficients in the 2-D second order AR model. The typical values for the outdoor scene are $\rho_1 = 0.957$ and $\rho_2 = 0.967$ [10].

Jayant and Noll [30] showed that $\epsilon^2_{DPCM}$ can be approximately expressed as: $\epsilon^2_{DPCM} \approx 2.55 \epsilon^2_{PCM} = \gamma \epsilon^2_e$, where $\gamma$ is the power transfer factor of the decoder filter of the DPCM. Moreover, the quantity $\epsilon^2_{DPCM}$ has been found to be negligible compared to $\epsilon^2_{2,DPCM}$ and $\epsilon^2_{3,DPCM}$. Thus, $\sigma^2_{DPCM}$ of (40) reduces to

$$\sigma^2_{DPCM} \approx \left(\epsilon^2_{2,DPCM} + \epsilon^2_{3,DPCM}\right) G_p^{-1} \sigma^2_x$$

(42)

where $G_p$ is the prediction gain which is defined as the ratio between the input signal variance and the prediction error variance.

Comparing (42) with (39), it may be found that the quantization noise contribution in DPCM is smaller than in PCM by a factor $G_p$; and the channel error contribution in DPCM is smaller than in PCM by a factor $\frac{\epsilon^2_{PCM}}{\epsilon^2_e}$, provided that $\epsilon^2_{DPCM}$ is equal to $\epsilon^2_{2,PCM}$. Note that the ratio between $\epsilon^2_{e,PCM}$ and $\epsilon^2_{DPCM}$ is equal to unity for generalized Gaussian images or $\frac{\epsilon^2_e}{\epsilon^2_e}$ for Laplacian images [30].

### B. Analysis of CDMA Channel Errors in Subband Images

For the transmission of $M$ subbands via the CDMA fading channels, $\sigma^2_{DPCM}$ is treated as the reconstruction error variance for base band, $\sigma^2_{DPCM}$, and $\sigma^2_{PCM}$'s are used to characterize the reconstruction error variances for higher bands, $\sigma^2_{DPCM}$, $k > 1$. In other words, $\sigma^2_{DPCM}$ represents the error variance of the $k$th received subband in the reference image via a virtual connection over the air interface created by its corresponding $k$th spreading code. Furthermore, [31] and [32] showed that the reconstruction error variance of an image via $M$ parallel independent virtual channels can be obtained by performing a weighted sum of total subband reconstruction error variances, that is

$$\sigma^2_{image} = \sum_{k=1}^{M} \alpha_{k} \sigma^2_{DPCMK}$$

(43)

where the weighting value for the $k$th subband is specified by

$$\alpha_{k} = \epsilon_{DPCM}^k \cdot \frac{1}{G_{DPCM}(w_1, w_2)}$$

(44)

where $G_{DPCM}(w_1, w_2)$ is the transfer function of the synthesis filter for the $k$th subband. However, for the case of separable reconstruction filters and $M = 4$, the weighting values are
Fig. 7. Test image "Portrait."

Fig. 8. Test image "Andes."

\[ Q_{ll} = Q_{lp}, Q_{lh} = Q_{hl}, \text{ and } Q_{hh} = Q_{l}Q_{h}, \]

where \( Q_{l} \) and \( Q_{h} \) are the power transfer factors for lowpass and highpass synthesis filters, respectively. Cheong et al. [31] found that both QMF and orthonormal wavelets have a value nearly equal to unity (\( Q_{l} = Q_{h} \approx 0.9999 \)), and SSKF has low values (\( Q_{l} = 0.75 \) and \( Q_{h} = 0.359375 \)). This implies that SSKF achieves much smaller image reconstruction error variance than both QMF and orthonormal wavelet.

Moreover, total quantization error variance in (43), \( \sigma_{q_{l}}^{2} \), is assumed to be much smaller than the total channel error variance, \( \sigma_{e_{c}}^{2} \), and then is negligible for the derivation of the image signal-to-noise ratio. Therefore, from (39), (42), and (43), it yields

\[ \sigma_{image}^{2} \approx \left( \alpha_{l}^{2} c_{l}^{2} G_{p}^{-1} + \sum_{k=2}^{M} \alpha_{k} c_{k}^{2} \right) \sigma_{x}^{2}. \]  

(45)

In (45), each subband may be protected by unequal error correction (UEC) strategy using rate compatible punctured convolutional codes (RCPC). From (45), the signal-to-noise ratio of the output image [30] becomes

\[ \text{SNR}_{\text{image}} = 10 \log_{10} \frac{E(x^2)}{E((x-y)^2)} \]  

(dB)  

(46)

\[ \geq -10 \log_{10} \left( \alpha_{l}^{2} c_{l}^{2} G_{p}^{-1} + \sum_{k=2}^{M} \alpha_{k} c_{k}^{2} \right) \]  

(47)

where \( x \) and \( y \) denote the input and output gray values, respectively.

For simplified analysis, it may be assumed that the bit error probabilities of the subbands in the same image are identical because each of them has the same interpath, intra-image, and inter-image subband interferences and AWGN noise over the CDMA channel when each subband employs equal error protection channel coding. If \( p_{e} \) and \( R \) are sufficiently small, the channel contributes to \( e_{k}^{2} \) only through single errors. Thus, \( e_{k}^{2} \approx \zeta_{k}^{2} p_{e} \) (or \( \approx \zeta_{k}^{2} p_{e} \)) for the \( k \)th subband, \( k \geq 2 \) (or the...
images placed on an equidistance contour via SS-CDMA indoor fading channels with channel coding and EGC combining of $M_d = 4$.

Fig. 11. PSNR performance versus channel SNR for "Portrait" and "Andes" images transmitted from the locations with two different distances, $d^f = 1.5$ via coded SS-CDMA indoor fading channels without power control and with EGC combining of $M_d = 4$.

Fig. 12. PSNR performance versus channel SNR for "Portrait" and "Andes" images transmitted from the locations with two different distances, $d^f = 1.5$ via coded SS-CDMA indoor fading channels without power control and with EGC combining of $M_d = 4$.

First band, and SNR$_{image}$ of (47) becomes

$$SNR_{image} \approx C - 10 \log_{10} p_e \quad (48)$$

where $c_1$ and $c_2$ are the first channel coefficients for the first subband and the $k$th subband, $k \geq 2$, respectively, and $C = -10 \log_{10}(e^{G_p^2} + \sum_{k=0}^{M} a_k c_k^2)$ would be a constant which is independent of bit error probability. In other words, $C$ does not depend on the total interference and noise over CDMA channels. However, the commonly-used subjective measure of the reconstructed image quality is the peak signal-to-noise ratio (PSNR) [30], which can be expressed as a form in terms of $p_e$

$$PSNR = 10 \log_{10} \frac{x_{pp}^2}{E[(x-y)^2]} \quad (dB) \quad (49)$$

$$\approx \hat{C} - 10 \log_{10} p_e \quad (dB) \text{ for } p_e \text{ and } R \text{ are sufficiently small} \quad (50)$$

where $\hat{C} = C + 10 \log_{10} \frac{s^2}{\sigma^2}$ is also independent of the total interference and noise over CDMA channels, $x_{pp}$ is the peak gray value of the input image. Equation (47) shows that PSNR is increasing while $p_e$ is decreasing since $e_{ck} = f_k(p_e)$ is a monotonic increasing function of bit error probability. However, the relationship between PSNR and $p_e$ is quite complicated and cannot be characterized by a function of simple expression. When $p_e$ becomes sufficiently small, from (50), PSNR is inversely related to a simply logarithmic function of $p_e$. However, the expression of (50) may not be valid since $\sigma_{kq}^2$ may be larger than $\sigma_{kk}^2$ when $p_e$ is less than an extremely small prescribed value. In this case, PSNR is dominated by the value of $\sigma_{kq}^2$ and then becomes a constant value of $10 \log_{10} (x_{pp}^2/\sigma_{kq}^2)$ provided that $\sigma_{kq}^2 \ll \sigma_{kk}^2$.

V. SIMULATION RESULTS

To examine the performance of the transmission of subband images via SS-CDMA channels, two monochrome test images, "Portrait" illustrated in Fig. 7 and "Andes" illustrated in Fig. 8, are considered in our system. They are gray scale pictures with $256 \times 256$ pixels and eight bits per pixel. For each picture, the input was first split into four bands using a 2-D separable SSKF (four-tap in each direction) proposed by D. Le Gall et al. [17]. The lowest band image was DPCM encoded using 2-D prediction and a nonuniform quantizer with 14 quantization levels. The details of the quantizer levels and their corresponding threshold values are illustrated in Table I of reference [17]. However, since the samples in the higher frequency bands show little correlation among pixels, these bands are encoded using PCM with a nonuniform quantizer instead of DPCM. According to Le Gall et al.'s suggestions, the PCM quantizer parameters for higher bands are chosen to be: $d = 8, t = 36, Y = 42,$ and $L = 8$.

Next, we consider the transmission of these two test pictures in a eight-user SS-CDMA indoor fading channel with DPSK modulation and EGC combining where each user corresponds to one of the eight decomposed subbands resulted from both pictures. The spreading codes of our SS-CDMA system are chosen as the well-known Kasami code of length 255 and would be assigned to their corresponding subbands of both test images. The indoor radio channel used in performance evaluation is on basis of Saleh and Valenzuela's measurements [19]. The measurements indicate that the maximum delay spread is usually $T_m = 150$ ns. From (7), the maximum number of resolved multipaths is equal to four, i.e., $L_{\text{max}} = 4$. Assume that there are two antennas, e.g., $L_{\text{ant}} = 2$, in the SS-CDMA system. Thus, we have two antennas and four paths per antenna to give a total maximum order of diversity of $M_d = 4 = L_{\text{ant}} \times L_{\text{max}}/2$. Assume that both test images are placed on an equidistance contour of 300 ft around the receiver. Kavehavad et al. [24] showed that the channel with a 300 ft distance can be approximately characterized by their Channel Model-I which is the simple analytically tractable model for the performance evaluation of spread spectrum systems. In contrast to Model-I, they showed that the ray cluster model (Model-II) is the analytically intractable
model which is infeasible for determining the performance of the DPSK system with predetection combining. In Channel Model-I, the average powers of the path gains for these eight subbands are found to be identical and equal to -14 dB (0.038), i.e., $\beta_{ik} = \beta_i = -14$ dB for $1 \leq l \leq 4$ and $1 \leq k \leq 2$. If both test images are transmitted at two locations with different distances, one should apply a perfect average control mechanism to keep the received average powers of these eight subbands almost equal. In other words, $\bar{E}_{b,k} = \bar{E}_b$ for $1 \leq k \leq 2$.

Moreover, the SS-CDMA fading channel output is corrupted by a zero-mean AWGN. In Fig. 9, the bit-error probabilities of both test images without channel coding are plotted versus the channel signal-to-noise ratio of their reference first subbands. It is clear from this figure that the average bit-error probabilities for both test images without performing channel coding are close to a theoretical bit-error probability of $p_e = p(x_i) = f(Y_{\theta})$ shown in (23), where $\gamma_e$ is defined in (25) can be expressed as a function of $\gamma_e, k$. Fig. 10 shows that better BER performances for both test images can be achieved by the SS-CDMA system with channel coding. Observing Figs. 9 and 10, the bit error rate will converge to a constant saturation level since $\gamma_e$ of (25) becomes a constant value of $(3N_c/2aMN)$ when $\bar{E}_b/N_0$ is sufficiently large. For simplicity, each subband is assumed to be protected by (2, 1, 6) convolutional code equally. Fig. 11 illustrates the image PSNR versus channel SNR, $\frac{E_b}{N_0}$, performances of both test images via the coded CDMA systems. These two PSNR curves are almost identical since the power of the reference channel is preserved in all subbands. In Fig. 11, the PSNR curve for Portrait or Andes is inversely related to its bit-error rate curve shown in Fig. 10. This would verify the relationship of (50) when $p_e$ is sufficiently small. However, PSNR is a complicated monotonically decreasing function of $p_e$ when channel signal-to-noise ratio value falls within the interval between 10 dB and 25 dB. The quality of image transmission via coded CDMA systems rapidly breaks down with the image PSNR becoming an unreliable quality measure when the channel SNR value is lower than 10 dB.

The SS-CDMA systems would suffer from a severe near–far problem when the received powers of the system are not controlled. Fig. 12 compares the respective PSNR's for Portrait and Andes achieved by the coded SS-CDMA systems where Portrait and Andes are transmitted at $d_1(=300$ ft) and $d_2(=450$ ft) respectively, where the received power for Portrait is treated as a reference power, $\bar{E}_b$. As expected, the quality of the received image (Portrait) from a nearer position is much better than that of the received image (Andes) from a farther position. Compared Fig. 12 with Fig. 11, the PSNR of Portrait of Fig. 12 is larger than that of Fig. 11 since Andes of Fig. 12 produces smaller interference strength to Portrait than Andes of Fig. 11. However, the PSNR of Andes of Fig. 12 is larger than that of Fig. 11 since it is corrupted by a large interference caused from Portrait of Fig. 12. It should be mentioned that the coded system allows the quality image transmission from the nearer position at a channel SNR value larger than 22 dB. However, the quality image transmission via coded system from the farther position is achieved at a channel SNR value larger than 36 dB. This performance degradation (14 dB) is resulted from the unequal received power difference where these two test images are transmitted at locations with two different distances. Note that the PSNR of 40 dB is a practical performance index which allows quality image transmission [30]. Finally, to further improve the performance of our system, if the subbands have different bit rates, more than one spreading code is assigned to the high bit-rate subband when its bit rate is higher than the peak channel capacity. However, more than one lower bit-rate subband may be combined to share the same spreading code in order to fully utilize the channel capacity. An adaptive "merge and split" strategy is performed by monitoring the bit-rate of each subband. For the issue of implementation, we can use C. L. T.'s subcode concatenation scheme [36] to generate additional codes for the high bit-rate subband.

VI. CONCLUSION

This paper presented an image transmission system over SS-CDMA indoor radio channels interconnecting with the fiber optic CDMA network. The use of subband coding techniques using SSKF's which require very few computations to divide the image information into a number of subbands, instead of transmitting the image over the radio channel directly, enables fully parallel subband image transmission and access. Each subband is transmitted using one of the spreading codes in the SS-CDMA system, and then fits within the narrow radio channel bandwidth. Thus, the throughput of transmitting these images within the allowable radio bandwidth is significantly increased. In addition, DPSK modulation with EGC combining diversity is employed in the SS-CDMA systems in order to counteract multipath fading and avoid the carrier recovery. We also introduced an analysis of transmission error effects in the subband image via SS-CDMA indoor radio channels. Finally, simulation results for two commonly-used test images were presented and compared with the image quality analysis.

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